# The Cecil Language Specification and Rationale

Version 2.1

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## Abstract

Cecil is a purely object-oriented language intended to support rapid construction of high-quality, extensible software. Cecil combines multi-methods with a simple classless object model, a kind of dynamic inheritance, modules, and optional static type checking. Instance variables in Cecil are accessed solely through messages, allowing instance variables to be replaced or overridden by methods and vice versa. Cecil's predicate objects mechanism allows an object to be classified automatically based on its run-time (mutable) state. Cecil's static type system distinguishes between subtyping and code inheritance, but Cecil enables these two graphs to be described with a single set of declarations, streamlining the common case where the two graphs are parallel. Cecil includes a fairly flexible form of parameterization, including explicitly parameterized objects, types, and methods, as well as implicitly parameterized methods related to the polymorphic functions commonly found in functional languages. By making type declarations optional, Cecil aims to allow mixing of and migration between exploratory and production programming styles. Cecil supports a module mechanism that enables independently-developed subsystems to be encapsulated, allowing them to be type-checked and reasoned about in isolation despite the presence of multi-methods and subclassing. Objects can be extended externally with additional methods and instance variables, often encapsulated in separate modules, supporting a kind of rolebased or subject-oriented programming style.

This document mixes the specification of the language with discussions of design issues and explanations of the reasoning that led to various design decisions.

## Table of Contents

| 1 Introduction |     |                                   |  | 1  |  |  |  |  |
|----------------|-----|-----------------------------------|--|----|--|--|--|--|
|                | 1.1 | 1 Design Goals and Major Features |  |    |  |  |  |  |
|                | 1.2 | 2 Overview                        |  |    |  |  |  |  |
| 2              | Dyn | namically-Typed Core              |  |    |  |  |  |  |
|                | 2.1 | Objec                             | 5  |    |  |  |  |  |
|                |     | ,<br>2.1.1                        | Inheritance  | 6  |  |  |  |  |
|                |     | 2.1.2                             | Object Instantiation                               | 7  |  |  |  |  |
|                |     | 2.1.3                             | Extension Declarations                             | 7  |  |  |  |  |
|                |     | 2.1.4                             | Predefined Objects                                 | 7  |  |  |  |  |
|                |     | 2.1.5                             | Closures   | 8  |  |  |  |  |
|                | 2.2 | Metho                             | ods  | 8  |  |  |  |  |
|                |     | 2.2.1                             | Argument Specializers and Multi-Methods            | 9  |  |  |  |  |
|                |     | 2.2.2                             | Method Bodies                                      | 10 |  |  |  |  |
|                |     | 2.2.3                             | Primitive Methods                                  | 11 |  |  |  |  |
|                | 2.3 | Fields                            | 3  | 12 |  |  |  |  |
|                |     | 2.3.1                             | Read-Only vs. Mutable Fields                       | 13 |  |  |  |  |
|                |     | 2.3.2                             | Fields and Methods                                 | 13 |  |  |  |  |
|                |     | 2.3.3                             | Copy-Down vs. Shared Fields                        | 14 |  |  |  |  |
|                |     | 2.3.4                             | Field Initialization                               | 15 |  |  |  |  |
|                | 2.4 | Predic                            | cate Objects                                       | 17 |  |  |  |  |
|                |     | 2.4.1                             | Predicate Objects and Inheritance                  | 18 |  |  |  |  |
|                |     | 2.4.2                             | Predicate Objects and Fields                       | 21 |  |  |  |  |
|                | 2.5 | Statements and Expressions        |  |    |  |  |  |  |
|                |     | 2.5.1                             | Declaration Blocks                                 | 23 |  |  |  |  |
|                |     | 2.5.2                             | Variable Declarations                              | 23 |  |  |  |  |
|                |     | 2.5.3                             | Variable References                                | 24 |  |  |  |  |
|                |     | 2.5.4                             | Assignment Statements                              | 24 |  |  |  |  |
|                |     | 2.5.5                             | Literals   | 24 |  |  |  |  |
|                |     | 2.5.6                             | Message Sends                                      | 24 |  |  |  |  |
|                |     |                                   | Object Constructors                                | 26 |  |  |  |  |
|                |     | 2.5.8                             | Vector Constructors                                | 26 |  |  |  |  |
|                |     | 2.5.9                             | Closures   | 26 |  |  |  |  |
|                | 0.0 |                                   | Parenthetical Subexpressions                       | 27 |  |  |  |  |
|                | 2.6 |                                   | dence Declarations                                 | 27 |  |  |  |  |
|                |     | 2.6.1                             | Previous Approaches                                | 28 |  |  |  |  |
|                |     | 2.6.2                             | Precedence and Associativity Declarations in Cecil | 29 |  |  |  |  |

|   | 2.7  | Metho   | od Lookup   | 30       |  |  |  |
|---|--|---|---|----------|--|--|--|
|   |  | 2.7.1   | Philosophy  | 30       |  |  |  |
|   |  | 2.7.2   | Semantics   | 31       |  |  |  |
|   |  |   | Examples  | 32       |  |  |  |
|   |  | 2.7.4   | 0   | 33       |  |  |  |
|   |  | 2.7.5   | •   | 34       |  |  |  |
|   |  | 2.7.6   | Cyclic Inheritance  | 35       |  |  |  |
|   |  | 2.7.7<br>2.7.8  |   | 35<br>36 |  |  |  |
|   | 2.8  | Reser   |   | 36       |  |  |  |
|   | 2.9  |   |   |          |  |  |  |
|   | -  | Files and Include Declarations 3<br>Pragmas 3           |   |          |  |  |  |
| 2 |  | -   |   |          |  |  |  |
| 3 |  |   | es  |          |  |  |  |
|   | 3.1  | Goals   |   | 40       |  |  |  |
|   | 3.2  | •••   | and Signatures  | 41       |  |  |  |
|   | 3.3  |   | and Signature Declarations  | 43       |  |  |  |
|   |  | 3.3.1   | Type Declarations   | 44       |  |  |  |
|   |  |   | Representation and Object Declarations                                      | 44       |  |  |  |
|   |  | 3.3.3   |   | 46       |  |  |  |
|   |  | 3.3.4<br>3.3.5  | Signature Declarations  | 46<br>47 |  |  |  |
|   |  | 3.3.5<br>3.3.6  | Implementation and Method Declarations<br>Field Implementation Declarations | 47       |  |  |  |
|   |  | 3.3.7   | Other Type Declarations   | 48       |  |  |  |
|   |  | 3.3.8   | Discussion  | 48       |  |  |  |
|   | 3.4  | Speci   | al Types and Type Constructors  | 49       |  |  |  |
|   |  | 3.4.1   | Named Types   | 49       |  |  |  |
|   |  | 3.4.2   | Closure Types   | 50       |  |  |  |
|   |  | 3.4.3   | Least-Upper-Bound Types   | 50       |  |  |  |
|   |  | 3.4.4   | Greatest-Lower-Bound Types  | 50       |  |  |  |
|   | 3.5  | Objec   | t Role Annotations  | 51       |  |  |  |
|   | 3.6  | Туре  | Checking Messages   | 53       |  |  |  |
|   |  | 3.6.1   | Checking Messages Against Signatures  | 53       |  |  |  |
|   |  | 3.6.2   |   | 54       |  |  |  |
|   |  | 3.6.3   |   | 56       |  |  |  |
|   | . –  | 3.6.4   | Type Checking Inherited Methods   | 57       |  |  |  |
|   | 3.7  | Type Checking Expressions, Statements, and Declarations |   |          |  |  |  |
|   | 3.8  |   | Checking Subtyping Declarations   | 64       |  |  |  |
|   | 3.9  |   | Checking Predicate Objects  | 64       |  |  |  |
|   | 3.10 Mixed Statically- and Dynamically-Typed Code 66 |   |   |          |  |  |  |

| 4   | Para | ameter         | ization and Parametric Polymorphism                      | 68       |  |  |  |
|---|------|----------------|--|----------|--|--|--|
|   | 4.1  | Explic         | it Parameterization                                      | 68       |  |  |  |
|   |      |                | Parameterized Declarations and Formal Type Parameters    | 69       |  |  |  |
|   |      |                | Instantiating Parameterized Declarations                 | 69       |  |  |  |
|   |      |                | Parameterized Objects and Types                          | 70       |  |  |  |
|   |      | 4.1.4<br>4.1.5 | Method Lookup<br>Type Checking Instantiations            | 70<br>71 |  |  |  |
|   | 4.2  |                |  | 71       |  |  |  |
|   |      |                |  |          |  |  |  |
|   | 4.3  |                | hing Against Type Patterns                               | 74       |  |  |  |
|   |      | 4.3.1          | Method Formal Type Patterns<br>Upper Bound Type Patterns | 74<br>75 |  |  |  |
|   |      |                | The Matching Algorithm                                   | 75       |  |  |  |
|   |      | 4.3.4          |  | 77       |  |  |  |
|   |      | 4.3.5          | Constraints on Supertype Graphs for Matching             | 78       |  |  |  |
|   |      | 4.3.6          | Matching and Bounded Formal Type Parameters              | 78       |  |  |  |
|   | 4.4  | Implic         | it Type Parameters in Extension Declarations             | 79       |  |  |  |
| 4.5 Parameterized Objects and Method Lookup |      |                |  |          |  |  |  |
|   | 4.6  | Paran          | neterization and Syntactic Sugars                        | 80       |  |  |  |
|   | 4.7  | F-Bou          | 80   |          |  |  |  |
| 4.7.1 Motivation                            |      |                |  |          |  |  |  |
|   |      |                | F-Bounded Polymorphism in Singly-Dispatched Languages    | 81       |  |  |  |
|   |      |                | F-Bounded Polymorphism in Cecil                          | 82       |  |  |  |
|   |      |                | F-Bounded Polymorphism among Multiple Types              | 83       |  |  |  |
| 5   | Mod  | lules.         |  | 85       |  |  |  |
| 6   | Rela | ated W         | ork  | 87       |  |  |  |
| 7   | Con  | clusio         | n  |          |  |  |  |
| Do  |      |                |  |          |  |  |  |
|   |      |                |  |          |  |  |  |
| Ap  | penc | A xib          | Annotated Cecil Syntax                                   | 96       |  |  |  |
|   | A.1  | Gram           | mar  | 96       |  |  |  |
|   | A.2  | Toker          | S  | 101      |  |  |  |
|   | A.3  | White          | Space  | 102      |  |  |  |
|   |      |                |  |          |  |  |  |

## 1 Introduction

This document describes the current design of Cecil, an object-oriented language intended to support the rapid construction of high-quality, reusable, extensible software systems [Chambers 92b, Chambers 93b, Chambers & Leavens 94]. Cecil is unusual in combining a pure, classless object model, multiple dispatching (multi-methods), modules, and mixed static and dynamic type checking. Cecil was inspired initially by Self [Ungar & Smith 87, Hölzle *et al.* 91a], CLOS [Bobrow *et al.* 88, Gabriel *et al.* 91], and Trellis [Schaffert *et al.* 85, Schaffert *et al.* 86]. The current version of Cecil extends the earlier version [Chambers 93a] with predicate objects, modules, and efficient typechecking algorithms.

## 1.1 Design Goals and Major Features

Cecil's design results from several goals:

• Maximize the programmer's ability to develop software quickly and to reuse and modify existing software easily.

In response to this goal, Cecil is based on a pure object model: all data are objects and objects are manipulated solely by passing messages. A pure object model ensures that the power of object-oriented programming is uniformly available for all data and all parts of programs. The run-time performance disadvantage traditionally associated with pure object-oriented languages is diminishing with the advent of advanced implementations.

Our experience also leads us to develop a classless (prototype-based) object model for Cecil. We feel that a classless object model is simpler and more powerful than traditional class-based object models. Cecil's object model is somewhat more restricted than those in other prototype-based languages [Borning 86, Lieberman 86, LaLonde *et al.* 86, Ungar & Smith 87, Lieberman *et al.* 87], in response to other design goals.

Since message passing is the cornerstone of the power of object-oriented systems, Cecil includes a fairly general form of dynamic binding based on multiple dispatching. Multimethods affect many aspects of the rest of the language design, and much of the research on Cecil aims to combine multi-methods with traditional object-oriented language concepts, such as encapsulation and static type checking, not found in other multiple dispatching languages.

Inheritance also plays a key role in organizing software and factoring out commonalities. Cecil extends traditional inheritance mechanisms with predicate objects to support an automatic form of classification of objects into specialized subclasses based on their run-time state. Since this state can be mutable, an object's classification can change over time. This mechanism enables inheritance and classification to be applied even when modelling time-varying properties of an object. For example, a rectangle can be automatically classified as the predicate subobject square whenever it satisfies the predicate that its length equals its width, even if the rectangle's length and width are mutable.

Instance variables (called fields in Cecil) are also accessed solely by sending messages, enabling fields to be replaced or even overridden with methods, and vice versa, without affecting clients. Fields can be given default initial values as part of their declaration. An initialization expression is evaluated lazily, when the field is first referenced, acting as a kind of memoized constant function. By allowing the initialization expression to reference the

object that it will become a part of, circular data structures can be constructed, and more generally, the value of one field can be computed from the values of other fields of an object.

• Support production of high-quality, reliable software.

To help in the construction of high-quality programs, programmers can add staticallycheckable declarations and assertions to Cecil programs. One important kind of static declaration specifies the types of (i.e., the interfaces to) objects and methods. Cecil allows programmers to specify the types of method arguments, results, and local variables, and Cecil performs type checking statically when a statically-typed expression is assigned to a staticallytyped variable or formal argument. The types specified by programmers describe the minimal *interfaces* required of legal objects, not their *representations* or *implementations*, to support maximum reuse of typed code. In Cecil, the subtype graph is distinguished from the code inheritance graph, since type checking has different goals and requirements than have code reuse and module extension [Snyder 86, Halbert & O'Brien 86, Cook *et al.* 90].

To support the independent construction of subsystems, Cecil includes a module system. A module encapsulates its internal implementation details and presents an interface to external clients. This encapsulation mechanism is specially designed to work in the presence of multimethods and inheritance/subtyping across module boundaries. Modules can be used to encapsulate "roles" [Andersen & Reenskaug 92] or "subjects" [Harrison & Ossher 93], programming idioms where pieces of the total interface of an object are split apart into application-specific facets. A given module can include method and field declarations that extend one or more previously-defined objects with additional specialized state and behavior.

Cecil includes other kinds of static declarations. An object can be annotated as an abstract object (providing shared behavior but not manipulable by programs), as a template object (providing behavior suitable for direct instantiation but otherwise not manipulable by the program), or as a concrete object (fully manipulable and instantiated as is). Object annotations inform the type checker how the programmer intends to use objects, enabling the type checker to be more flexible for objects used in only a limited fashion.

Cecil encourages a functional programming style by default, as this is likely to be easier to understand and more robust in the face of programming changes. By default, both local variables and fields are initialize-only; an explicit var keyword is required to assert that a variable or field can be mutated. An object can be created and its fields initialized to desired values in a single atomic operation; there are no partially-initialized states as are found during execution of a constructor in C++.

Finally, Cecil omits certain complex language features that can have the effect of masking programming errors. For example, in Cecil, multiple dispatching and multiple inheritance are both *unbiased* with respect to argument order and parent order; any resulting ambiguities are reported back to the programmer as potential errors. This design decision is squarely at odds with the decision in CLOS and related languages. Additionally, subtyping in Cecil is explicit rather than implicit, so that the behavioral specification information implied by types can be incorporated into the decision about whether one type is a behavioral subtype of another.

• Support both exploratory programming and production programming, and enable smooth migration of parts of programs from one style to the other.

Central to achieving this goal in Cecil is the ability to omit type declarations and other annotations in initial exploratory versions of a subsystem and incrementally add annotations as the subsystem matures to production quality. Cecil's type system is intended to be flexible and expressive, so that type declarations can be added to an existing dynamically-typed program and achieve static type correctness without major reorganization of the program. In particular, objects, types, and methods may be explicitly parameterized by types, method argument and result types may be declared as or parameterized by implicitly-bound type variables to achieve polymorphic function definitions, and (as mentioned above) the subtype graph can differ from the inheritance graph. The presence of multiple dispatching relieves some of the type system's burden, since multiple dispatching supports in a type-safe manner what would be considered unsafe covariant method redefinition in a single-dispatching language.

Additionally, an environment for Cecil could infer on demand some parts of programs that otherwise must be explicitly declared, such as the list of supertypes of an object or the set of legal abstract methods of an object, so that one language can support both exploratory programmers (who use the inferencer) and production programmers (who explicitly specify what they want). This approach resolves some of the tension between language features in support of exploratory programming and features in support of production programming. In some cases, the language supports the more explicit production-oriented feature directly, with an environment expected to provide additional support for the exploratory-oriented feature.

• Avoid unnecessary redundancy in programs.

To avoid requiring the programmer to repeat specifying the interface of an object or method, Cecil allows a single object declaration to define both an implementation and a type (an interface). Similarly, where the subtype hierarchy coincides with the code inheritance hierarchy, a single declaration will establish both relations. This approach greatly reduces the amount of code that otherwise would be required in a system that distinguished subtyping and code inheritance. Without this degree of conciseness, we believe separating subtyping from code inheritance would be impracticably verbose.

Similarly, Cecil's classless object model is designed so that a single object declaration can define an entire data type. This contrasts with the situation in Self, where two objects are needed to define most data types [Ungar *et al.* 91]. Similarly, Cecil's object model supports both concise inheritance of representation and concise overriding of representation, unlike most class-based object-oriented languages which only support the former and most classless object-oriented languages which only support the latter.

Finally, Cecil avoids requiring annotations for exploratory programming. Annotations such as type declarations and privacy declarations are simply omitted when programming in exploratory mode. If this were not the case, the language would likely be too verbose for rapid exploratory programming.

• Be "as simple as possible but no simpler."

Cecil attempts to provide the smallest set of features that meet its design goals. For example, the object model is pure and classless, thus simplifying the language without sacrificing expressive power. However, some features are included in Cecil that make it more complex,

such as supporting multiple dispatching or distinguishing between subtyping and implementation inheritance. Given no other alternative, our preference is for a more powerful language which is more complex over a simpler but less powerful language. Simplicity is important but should not override other language goals.

Cecil's design includes a number of other features that have proven their worth in other systems. These include multiple inheritance of both implementation and interface, closures to implement user-defined control structures and exceptions, and, of course, automatic storage reclamation.

## 1.2 Overview

This document attempts to provide a fairly detailed specification of the Cecil language, together with discussion of the various design decisions. The next section of this document describes the basic object and message passing model in Cecil. Section 3 extends this dynamically-typed core language with a static type system and describes a type checking algorithm, and section 4 discusses parameterization. Section 5 describes Cecil's module system. Section 6 discusses some related work. Appendix A summarizes the complete syntax for Cecil.

## 2 Dynamically-Typed Core

Cecil is a pure object-oriented language. All data are objects, and message passing is the only way to manipulate objects. Even instance variables are accessed solely using message passing. This purity offers the maximum benefit of object-oriented programming, allowing code to manipulate an object with no knowledge of (and hence no dependence on) its underlying representation or implementation.

Each Cecil implementation defines how programs are put together. The UW Cecil implementation defines a program to be a sequence of declaration blocks and statements, optionally interspersed with pragmas:

```
program ::= top_level_file
top_level_file ::= { top_decl_block | stmt | pragma }
```

Declaration blocks are comprised of a set of declarations that are introduced simultaneously; names introduced as part of the declarations in the declaration block are visible throughout the declaration block and also for the remainder of the scope containing the declaration block; the names go out of scope once the scope exits. Because the name of an object is visible throughout its declaration block, objects can inherit from objects defined later within the declaration block and methods can be specialized on objects defined later in the declaration block. In environments where the top-level declaration comprising the program is spread across multiple files, the ability to attach methods to objects defined in some other file is important.

The syntax of declarations is as follows:\*

The next four subsections describe objects, methods, fields, and predicate objects. Subsection 2.5 describes variables, statements, and expressions, and subsection 2.6 explains precedence declarations. Subsections 2.7 and 2.8 detail the semantics of message passing in Cecil. Subsection 2.9 describes include declarations and file structure in the UW Cecil implementation, and subsection 2.10 discusses pragmas.

## 2.1 Objects and Inheritance

The basic features of objects in Cecil are illustrated by the following declarations, which define a simple shape hierarchy. Comments in Cecil either begin with "--" and extend to the end of the line or are bracketed between "(--" and "--)" and can be nested.

<sup>&</sup>lt;sup>\*</sup>Ignoring type and signature declarations (section 3) and module declarations (section 5).

```
object shape;
object circle isa shape;
object rectangle isa shape;
object rhombus isa shape;
object square isa rectangle, rhombus;
```

The syntax of an object declaration, excluding features relating to static type checking and modules, is as follows:<sup>\*</sup>

```
object_decl ::= "object" name {relation} [field_inits] ";"
relation ::= "isa" parents
parents ::= named_object { "," named_object }
named_object ::= name
```

(name is the token for regular identifiers beginning with a letter; see appendix A.2 for more details on the lexical rules of Cecil.)

Cecil has a classless (prototype-based) object model: self-sufficient objects implement data abstractions, and objects inherit directly from other objects to share code. Cecil uses a classless model primarily because of its simplicity, but also because this avoids problems relating to first-class classes and metaclasses and because it makes defining unique named objects with specialized behavior easy. Section 2.2 shows how treating "instance" objects and "class" objects uniformly enables CLOS-style eql specializers to be supported with no extra mechanism.

Section 2.3 describes field initializers.

#### 2.1.1 Inheritance

Objects can inherit from other objects. Informally, this means that the operations defined for parent objects will also apply to child objects. Inheritance in Cecil may be multiple, simply by listing more than one parent object; any ambiguities among methods and/or fields defined on these parents will be reported to the programmer. Inheriting from the same ancestor more than once, either directly or indirectly, has no effect other than to place the ancestor in relation to other ancestors; Cecil has no repeated inheritance as in Eiffel [Meyer 88, Meyer 92]. An object need not have any (explicit) parents; all objects are considered to inherit from the predefined any object (see section 2.1.4). The inheritance graph must be acyclic.

Inheritance in Cecil requires a child to accept all of the fields and methods defined in the parents. These fields and methods may be overridden in the child, but facilities such as excluding fields or methods from the parents or renaming them as part of the inheritance, as found in Eiffel, are not present in Cecil. We have deliberately chosen to experiment with a simpler inheritance semantics.

Finally, it is important to note that inheritance of code is distinct from *subtyping* ("inheritance" of interface or of specification). Section 3 explains Cecil's support for subtyping and static type checking.

<sup>\*</sup> Appendix A gives the complete syntax of the language and explains the notation.

## 2.1.2 Object Instantiation

Rather than introduce a distinct instantiation concept into the language, new "instances" of some object are created solely by inheriting from the object. Object declarations allow statically-known, named "instances" to be defined, while *object constructor expressions* allow new anonymous "instances" to be created at run-time. An object constructor expression is syntactically and semantically similar to an object declaration, except that there is no name for the object being created. For example:

**let** s1 := **object isa** square; -- create a fresh "instance" of square when executed

Section 2.5.7 describes object constructor expressions in more detail. Note that the parent of an object must be statically known; Cecil does not allow objects to be created whose parents are runtime computed expressions. This is a restriction over some other prototype-based languages.

#### 2.1.3 Extension Declarations

The inheritance structure of a named object may be augmented separately from the object declaration through an object extension declaration:

obj\_ext\_decl ::= "extend" named\_object {relation} [field\_inits] ";"

In Cecil, object extension declarations, in conjunction with field and method declarations, enable programmers to extend previously-existing objects. This ability can be important when reusing and integrating groups of objects implemented by other programmers. For example, predefined objects such as int, i\_vector, and m\_vector are given additional behavior and ancestry through separate user code. Similarly, particular applications may need to add application-specific behavior to objects defined as part of other applications. For example, a text-processing application may add specialized tab-to-space conversion behavior to strings and other collections of characters defined in the standard library. Other object-oriented languages such as C++ [Stroustrup 86, Ellis & Stroustrup 90] and Eiffel do not allow programmers to add behavior to existing classes without modifying the source code of the existing classes, and completely disallow adding behavior to built-in classes like strings. Sather is a notable exception, allowing a new class to be defined which is a superclass of some existing classes [Omohundro 93]. Section 3.3.3 explains how object extensions are particularly useful to declare that two objects, provided by two independent vendors, are subtypes of some third abstract type. Section 5 describes how modules can be used to localize extensions to particular regions of code.

#### 2.1.4 Predefined Objects

Several objects are predefined and play special roles.

- The void object is used to represent a lack of a value. It is used as the result of methods or expressions that have no useful result. The system will guarantee (statically in the presence of type checking) that void is never passed as an argument to a method.
- The any object is implicitly the ancestor of all non-void objects. It supports behavior that is shared by all objects.

A Cecil implementation provides other predefined objects, such as integers, floats, characters, booleans, and mutable and immutable vectors and strings, as part of its standard library.

#### 2.1.5 Closures

Cecil includes closure objects which represent first-class anonymous functions. Closures are lexically nested in their enclosing scope. As with methods, a closure can have formal arguments. A closure object is "invoked" by sending it the eval message, with additional actual arguments for each of its formal arguments. Closures are considered to inherit from the closure predefined object.

More details on closures are given throughout the remainder of section 2. In particular, section 2.5.9 describes the syntax and semantics of closure constructor expressions and section 2.2.2 describes the evaluation rules for closure eval methods.

## 2.2 Methods

The following definitions expand the earlier shape hierarchy with some methods:

```
object shape;
method draw(s, d) { (-- draws s on display d --) }
method move_to(s, new_center) { (-- move s to new_center --) }
object circle isa shape;
method area(c@circle) { c.radius * c.radius * pi}
method circum(c@circle) { c.radius * 2 * pi }
object rectangle isa shape;
method area(r@rectangle) { r.length * r.width }
method circum(r@rectangle) { 2 * r.length + 2 * r.width }
method draw(r@rectangle, d@Xwindow) {
(-- override draw for the case of drawing rectangles on X windows --) }
object rhombus isa shape;
cobject square isa rectangle, rhombus; --inherits area method, but overrides circum
method circum(s@square) { 4 * s.length }
```

The syntax for method declarations (again, excluding aspects relating to static typing and encapsulation) is as follows:

| method_decl | ::= | <pre>"method" method_name "("     "{" (body   prim_body</pre> |  |
|-------------|-----|---|--|
| method_name | ::= | msg_name   op_name  |  |
| msg_name    | ::= | name  |  |
| formals     | ::= | <pre>formal { ``," formal }</pre>                             |  |
| formal      | ::= | [name] specializer  | formal names are optional, if never referenced |
| specializer | ::= | "@" named_object<br>empty                                     | specialized formal<br>unspecialized formal     |

(op\_name is the token for infix and prefix operators beginning with a punctuation symbol; see appendix A.2 for more details.)

As a convention, we indent method declarations under the associated object declaration. This has no semantic implication, but it helps to visually organize a collection of object and method declarations in the absence of a more powerful graphical programming environment [Chambers 92b].

## 2.2.1 Argument Specializers and Multi-Methods

In Cecil, a method specifies the kinds of arguments for which its code is designed to work. For each formal argument of a method, the programmer may specify that the method is applicable only to actual arguments that are implemented or represented in a particular way, i.e., that are equal to or inherit from a particular object. These specifications are called *argument specializers*, and arguments with such restrictions are called *specialized arguments*. The r@rectangle notation specializes the r formal argument on the rectangle object, implying that the method is intended to work correctly with any actual argument object that is equal to or a descendant of the rectangle object as the r formal. An unspecialized formal argument (one lacking a @... suffix), such as s and new\_center in the move\_to method above, is treated as being specialized on the predefined object any that is implicitly an ancestor of all other objects; consequently an unspecialized formal can accept any argument object.

Methods may be overloaded, i.e., there may be many methods with the same name, as long as the methods with the same name and number of arguments differ in their argument specializers. Methods with different numbers of arguments are independent; the system considers the number of arguments to be part of the method's name. When sending a message of a particular name with a certain number of arguments, the method lookup system (described in section 2.7) will resolve the overloaded methods to a single most-specific applicable method based on the dynamic values of the actual argument objects and the corresponding formal argument specializers of the methods.

Zero, one, or several of a method's arguments may be specialized, thus enabling Cecil methods to emulate normal undispatched functions (by leaving all formals unspecialized, as in move\_to above) and singly-dispatched methods (by specializing only the first argument, as in the area methods) as well as true multi-methods (as in the specialized version of draw for rectangles on X windows). Statically-overloaded functions and functions declared via certain kinds of patternmatching also are subsumed by multi-methods. Callers which send a particular message to a group of arguments are not aware of the collection of methods that might handle the message or which arguments of the methods are specialized, if any; these are internal implementation decisions that should not affect callers. In particular, a given message can initially be implemented with a single unspecialized procedure and then later extended or replaced with several specialized implementations, without affecting clients of the original method, as occurs with the draw methods in the previous example. In contrast, CLOS has a "congruent lambda list" rule that requires all methods in a particular generic function to specialize on the same argument positions.

Argument specializers are distinct from type declarations. Argument specializers restrict the allowed implementations of actual arguments and are used as part of method lookup to locate a suitable method to handle a message send. Type declarations require that certain operations be supported by argument objects, but place no constraints on how those operations are implemented. Type declarations have no effect on method lookup.

The name of a formal may be omitted if it is not needed in the method's body. Unlike singlydispatched languages, there is no implicit self formal in Cecil; all formals are listed explicitly.

Cecil's classless object model combines with its definition of argument specializers to support something similar to CLOS's eql specializers. In CLOS, an argument to a multi-method in a generic function may be restricted to apply only to a particular *object* by annotating the argument specializer with the eql keyword. Cecil needs no extra language mechanism to achieve a similar effect, since methods already are specialized on particular objects. Cecil's mechanism differs from CLOS's in that in Cecil such a method also will apply to any children of the specializing object, while in CLOS the method will apply only for that object. Dylan, a descendant of CLOS, has a singleton specializer that is analogous to CLOS's eql specializer [Apple 92].

As mentioned in subsection 2.1.3, methods can be added to existing objects without needing to modify those existing objects. This facility, lacking in most object-oriented languages, can make reusing existing components easier since they can be adapted to new uses by adding methods, fields, and even parents to them.

The names of methods and fields are in a name space separate from the name space of objects and variables. A method or field can have the same name as a variable or object without confusion.

## 2.2.2 Method Bodies

The syntax of the body of a method, closure, or parenthetical subexpression is as follows:

| body          | : :=<br>       | <pre>{stmt} result empty</pre>                          | return void  |
|---------------|----------------|---|--|
| result        | ::=<br>        | normal_return<br>non_local_rtn                          | return an expression<br>return from the lexically-enclosing method                 |
| normal_return | : : =<br> <br> | <pre>decl_block [";"] assignment [";"] expr [";"]</pre> | return void<br>return void<br>return result of expression                          |
| non_local_rtn | ::=<br>        | <pre>"^" [";"] "^" expr [";"]</pre>                     | do a non-local return, returning void<br>do a non-local return, returning a result |

(The syntax and semantics of statements and expressions is described in section 2.5.)

When invoked, a method evaluates its statements in a new environment containing bindings for the method's formal parameters and nested in the method's lexically-enclosing environment. (The interactions among nested scopes, method lookup, and other language features is described in more detail in section 2.7.7.)

The result of the message invoking the method is the result of the last statement in the method's body. If the method's body is empty, then the method returns the special void value. Alternatively, a method returns void if the last statement is a declaration block, an assignment statement, or an expression that itself returns void. The void value is used to indicate that the method returns no useful result. The system ensures that void is not accidentally used in later computation by reporting an error (statically in the presence of type checking) if void is passed as an argument to a message.

When a closure's eval method is invoked, evaluation proceeds much like the evaluation of any other method. One difference is that a closure eval method may force a *non-local return* by prefixing the result expression with the ^ symbol; if the result expression is omitted, then void is returned non-locally. A non-local return returns to the caller of the closest lexically-enclosing non-closure method rather than to the caller of the eval method, just like a non-local return in Smalltalk-80<sup>\*</sup> [Goldberg & Robson 83] and Self and similar to a return statement in C. The language currently prohibits invoking a non-local return after the lexically-enclosing scope of a closure has returned; first-class continuations are not supported.

## 2.2.3 Primitive Methods

Low-level operations, such as integer arithmetic, vector indexing, looping, and file I/O, are implemented through the use of primitive methods. A primitive method's body is a list of (language name, implementation source code) pairs. The details of the protocol for writing code in another language inside a Cecil primitive method are implementation-specific. The UW Cecil implementation recognizes the  $c_{++}$  and rtl language names, for primitives written in C++ and the compiler's internal intermediate language, respectively. It is fairly straightforward to make calls to routines written in C++ from Cecil by defining a primitive method whose body is written in C++.

Looping primitive behavior is provided by the loop primitive method specialized on the closure predefined object. This method repeatedly invokes its argument closure until some closure performs a non-local return to break out of the loop. Other languages such as Scheme [Rees & Clinger 86] avoid the need for such a primitive by relying instead on user-level tail recursion and implementation-provided tail-recursion elimination. However, tail-recursion elimination precludes complete source-level debugging [Chambers 92a, Hölzle *et al.* 92] and consequently is undesirable in general. The primitive loop method may be viewed as a simple tail-recursive method for which the implementation has been instructed to perform tail-recursion elimination.

A primitive body may be included at the top-level using a primitive body declaration:

prim\_decl ::= prim\_body ";"

This construct allows code from other languages to be included outside of any compiled routines. Primitive declarations can be used to include global declarations used by primitive methods. Again, the detailed semantics of this construct are implementation-specific.

<sup>\*</sup> Smalltalk-80 is a trademark of ParcPlace Systems.

#### 2.3 Fields

Object state, such as instance variables and class variables, is supported in Cecil through *fields* and associated *accessor methods*. To define a mutable instance variable x for a particular object obj, the programmer can declare a field of the following form:

var field x(@obj);

This declaration allocates space for an object reference in the obj object and constructs two real methods attached to the obj object that provide the only access to the variable:

```
method x(v@obj) { prim rtl { <v.x> } } -- the get accessor method
method set_x(v@obj, value) { prim rtl { <v.x> := value; } } -- the set accessor method
```

The get accessor method returns the contents of the hidden variable. The set accessor method mutates the contents of the hidden variable to refer to a new object, and returns void. Accessor methods are specialized on the object containing the variable, thus establishing the link between the accessor methods and the object. For example, sending the x message to the obj object will find and invoke the get accessor method and return the contents of the hidden variable, thus acting like a reference to obj's x instance variable. (Section 5 describes how these accessor methods can be encapsulated within the data abstraction implementation and protected from external manipulation.)

To illustrate, the following declarations define a standard list inheritance hierarchy:

```
object list isa ordered_collection;
   method is empty(l@list) { l.length = 0 }
   method prepend(x, l@list) { -- dispatch on <u>second</u> argument
      object isa cons { head := x, tail := 1 } }
object nil isa list; -- empty list
   method length(@nil) { 0 }
   method do(@nil, ) {} -- iterating over all elements of the empty list: do nothing
   method pair_do(@nil, , ) {}
   method pair_do(, @nil, ) {}
   method pair do(@nil, @nil, ) {}
object cons isa list; -- non-empty lists
   var field head(@cons); -- defines head(@cons) and set head(@cons,) accessor methods
   var field tail(@cons); -- defines tail(@cons) and set_tail(@cons,) accessor methods
   method length(c@cons) { 1 + c.tail.length }
   method do(c@cons, block) {
      eval(block, c.head); -- call block on head of list
      do(c.tail, block); } -- recur down tail of list
   method pair do(c1@cons, c2@cons, block) {
      eval(block, c1.head, c2.head);
      pair_do(c1.tail, c2.tail, block); }
```

The cons object has two fields, only accessible through the automatically-generated accessor methods.

The syntax of field declarations, excluding static typing aspects and encapsulation, is as follows:

| field_decl | ::= | ["shared"] ["var"] | "field" | method_ | name | " ( ″ | formal | ")" |
|------------|-----|--------------------|---------|---------|------|-------|--------|-----|
|            |     | [":=" expr] ";     | "       |         |      |       |        |     |

#### 2.3.1 Read-Only vs. Mutable Fields

By default, a field is immutable: only the get accessor method is generated for it. To support updating the value of a field, the var prefix must be used with the field declaration. The presence of the var annotation triggers generation of the set accessor method. Immutable fields receive their values either as part of object creation or by an initializing expression associated with the field declaration; see section 2.3.4. Note that the contents of an immutable field can itself be mutable, but the binding of the field to its contents cannot change. (Global and local variables in Cecil similarly default to initialize-only semantics, with an explicit var annotation required to allow updating of the variable's value, as described in section 2.5.2.)

In general, we believe that it is beneficial to explicitly indicate when a field is mutable; to encourage this indication, immutable fields are the default. Programmers looking at code can more easily reason about the behavior of programs if they know that certain parts of the state of an object cannot be side-effected. Similarly, immutable fields support the construction of immutable "value" objects, such as complex numbers and points, that are easier to reason about.

Many languages, including Self and Eiffel, support distinguishing between assignable and constant variables, but few imperative languages support initialize-only instance variables. CLOS can define initialize-only variables in the sense that a slot can be initialized at object-creation time without a set accessor method being defined, but in CLOS the slot-value primitive function can always modify a slot even if the set accessor is not generated.

#### 2.3.2 Fields and Methods

Accessing variables solely through automatically-generated wrapper methods has a number of advantages over the traditional mechanism of direct variable access common in most objectoriented languages. Since instance variables can only be accessed through messages, all code becomes representation-independent to a certain degree. Instance variables can be overridden by methods, and vice versa, allowing code to be reused even if the representation assumed by the parent implementation is different in the child implementation. For example, in the following code, the rectangle abstraction can inherit from the polygon abstraction but alter the representation to something more appropriate for rectangles:

```
object polygon;
var field vertices(@polygon);
method draw(p@polygon, d@output_device) {
    (-- draw the polygon on an output device, accessing vertices --) }
object rectangle isa polygon;
var field top(@rectangle);
var field bottom(@rectangle);
var field left(@rectangle);
var field left(@rectangle);
var field right(@rectangle);
```

```
method vectices(r@rectangle) {
    -- ++ is a binary operator, here creating a new point object
    [r.top ++ r.left, r.top ++ r.right,
    r.bottom ++ r.right, r.bottom ++ r.left] }
method set_vertices(r@rectangle, vs) {
    (-- set corners of rectangle from vs list, if possible --) }
```

Even within a single abstraction, programmers can change their minds about what is stored and what is computed without rewriting lots of code. Syntactically, a simple message send that accesses an accessor method is just as concise as would be a variable access (using the p.x syntactic sugar, described in section 2.5.6), thus imposing no burden on the programmer for the extra expressiveness. Other object-oriented languages such as Self and Trellis have shown the advantages of accessing instance variables solely through special get and set accessor methods. CLOS enables get and/or set accessor methods to be defined automatically as part of the defclass form, but CLOS also provides a lower-level slot-value primitive that can read and write any slot directly. Dylan joins Self and Trellis in accessing instance variables solely through accessor methods.

An object may define or inherit several fields with the same name. Just as with overloaded methods, this is legal as long as two methods, accessor or otherwise, do not have the same name, number of arguments, and argument specializers. A method may override a field accessor method without removing the field's memory location from the object, since a resend within the overriding method may invoke the field accessor method. Implementations may optimize away the storage for a field in an object if it cannot be accessed, as with the vertices field in the rectangle object.

## 2.3.3 Copy-Down vs. Shared Fields

By default, each object inheriting a field declaration receives its own space to hold its version of the field's contents, and the field's accessor methods access the memory space associated with their first argument. Such a "copy-down" field acts much like an instance variable declaration in a classbased language, since each object gets its own local copy of the field. Alternatively, a field declaration may be prefixed with the shared keyword, implying that all inheriting objects should share a single memory location. A shared field thus acts like a class variable.

Supporting both copy-down and shared fields addresses weaknesses in some other prototype-based object-oriented languages relative to class-based languages. In class-based languages, instance variables declared in a superclass are automatically copied down into subclasses; the *declaration* is inherited, not the variable's *contents*. Class variables, on the other hand, are shared among the class, its instances, and its subclasses. In some prototype-based languages, including Self and Actra [Lieberman 86], instance variables of one object are not copied down into inheriting objects; rather, these variables are shared, much like class variables in a class-based language. In Self, to get the effect of object-specific state, most data types are actually defined with two objects: one object, the *prototype*, includes all the instance-specific variables that objects of the data type need, while the other object, the *traits object*, is inherited by the prototype and holds the methods and shared state of the data type [Ungar *et al.* 91]. New Self objects are created by cloning (shallow-copying) a prototype, thus giving new objects their own instance variables while sharing the parent traits object and its methods and state. Defining a data type in two pieces can be awkward, especially

since it separates the declarations of instance variables from the definitions of the methods that access them. Furthermore, inheriting the instance variable part of the implementation of one data type into another is more difficult in Self than in class-based languages, relying on complex inheritance rules and dynamic inheritance [Chambers *et al.* 91] or programming environment support [Ungar 95]. Copy-down fields in Cecil solve these problems in Self without sacrificing the simple classless object model. In Cecil, only one object needs to be defined for a given data type, and the field declarations can be in the same place as the method declarations that access them. This design increases both conciseness and readability, at the cost of some additional language mechanism.

Cecil objects are created only through object declarations and object constructor expressions; these two expressions have similar run-time effects, with the former additionally binding statically-known names to the created objects enabling methods and fields to be associated with them and enabling other objects to inherit from them. Cecil needs no other primitive mechanism to create or copy objects as do other languages. Self provides a shallow-copy (clone) primitive in addition to object literal syntax (analogous to Cecil's object constructor expressions), in part because there are no "copy-down" data slots in Self. Class-based languages typically include several mechanisms for creating instances and classes and relations among them. On the other hand, creating an object by inheriting from an existing object may not be as natural as creating an object by copying an existing object.

## 2.3.4 Field Initialization

Cecil allows a field to be given an initial value when it is declared by suffixing the field declaration with the := symbol and an initializing expression. Additionally, when an object is created, an object-specific initial value may be specified for a non-shared field. The syntax of field initializers for object declarations and object constructor expressions is as follows:

| field_inits | ::= | "{" field_init { ","            | <pre>field_init } "}"</pre> |
|-------------|-----|---------------------------------|-----------------------------|
| field_init  | ::= | <pre>name [location] ":="</pre> | expr                        |
| location    | ::= | "@" named_object                |                             |

For example, the following method produces a new list object with particular values for its inherited fields:

```
method prepend(e, l@list) {
    object isa cons { head := e, tail := 1 } }
```

For a field initialization of the form name := expr, the field to be initialized is found by performing a lookup akin to message lookup to find a field declaration named name, starting with the object being created. Method lookup itself cannot be used directly, since the field to be initialized may have been overridden with a method of the same name. Instead, a form of lookup that ignores all methods is used. If this lookup succeeds in finding a single most-specific matching field declaration, then that field is the one given an initial value; the matching field should not be a shared field. If no matching field or more than one matching field is found, then a "field initializer not understood" or an "ambiguous field initializer" error, respectively, is reported. To resolve ambiguities and to initialize fields otherwise overridden by other fields, an extended name for the field of the form name@obj := expr may be used instead. For these kind of initializers, lookup

for a matching field begins with the object named obj rather than the object being created. The obj object must be an ancestor of the object being created. Extended field names are analogous to a similar mechanism related to directed resends, described in section 2.8.

Immutable shared fields must be initialized as part of the field declaration; there is no other way to give them a value. Immutable copy-down fields may be initialized as part of the field declaration, but often they are initialized as part of object constructor expressions for objects that inherit the field, leading to a more functional programming style where data structures are (largely) immutable.

To avoid pesky problems with uninitialized variables, all fields must be initialized before being accessed, either by providing an initial value as part of the field declaration, by providing an object-specific value as part of the object declaration or object constructor expression, or by assigning to the field before reading from it. The static type checker warns when it cannot prove that at least one of the first two options is taken for each field inherited by an object, as described in section 3.7.

In Cecil, the initializing expression for a field declaration is not evaluated until the field is first read. If the field is a shared field, then the initializer is evaluated and the contents of the field is updated to refer to the initial value; subsequent reads of the shared field will simply return the initial value. This supports functionality similar to once functions in Eiffel and other languages. If the field is a copy-down field, then the initializing expression will be evaluated separately for each object accessed, and the result cached for that object. The initializing expression may name the formal parameter of the field declaration, allowing the initial value of the field to reference the object of which the field is a part. The default initializer is not evaluated if it is not needed, i.e., if the field has already been given a contents as part of object creation or via invocation of the set accessor.

By evaluating field initializers on demand rather than at declaration time, we avoid the need to specify some arbitrary ordering over field declarations or to resort to an unhelpful "unspecified" or "implementation-dependent" rule. It is illegal to try to read the value of a field during execution of the field's initializer; no cyclic dependencies among field initializers are allowed.

Evaluating a copy-down field's initializer expression repeatedly for each inheriting object seems to support common Cecil programming style. This corresponds to CLOS's :initform specifier. An earlier version of Cecil specified caching of the results of field initializer evaluation so that other objects evaluating the same initializer expression would end up sharing the initial value. The initializing expression was viewed as a shared part of the field declaration, not as a separate part copied down to each inheriting object. This earlier semantics corresponded more to CLOS's :default-initargs specifier. The difference in the semantics is exposed if the initializing expression evaluates to a new mutable object. In practice, it seems that each object wants its own mutable object rather than sharing the mutable object among all inheriting objects. Moreover, the old semantics can be simulated with a combination of a copy-down field that accesses a shared field to get the field's initial value.

## 2.4 Predicate Objects

To enable inheritance and classes to be used to capture run-time varying object behavior, Cecil support *predicate objects* [Chambers 93b]. Predicate objects are like normal objects except that they have an associated predicate expression. The semantics of a predicate object is that if an object inherits from the parents of the predicate object and also the predicate expression is true when evaluated on the child object, then the child is considered to also inherit from the predicate object in addition to its explicitly-declared parents. Since methods can be associated with predicate objects, and since predicate expressions can test the value or state of a candidate object, predicate objects allow a form of state-based dynamic classification of objects, enabling better factoring of code. Also, predicate objects and multi-methods allow a pattern-matching style to be used to implement cooperating methods.

For example, predicate objects could be used to implement a bounded buffer abstraction:

```
object buffer isa collection;
field elements(b@buffer); -- a queue of elements
field max_size(b@buffer); -- an integer
method length(b@buffer) { b.elements.length }
method is_empty(b@buffer) { b.length = 0 }
method is_full(b@buffer) { b.length = b.max_size }
predicate empty_buffer isa buffer when buffer.is_empty;
method get(b@empty_buffer) { ... } -- raise error or block caller
predicate non_empty_buffer isa buffer when not(buffer.is_empty);
method get(b@non_empty_buffer) { remove_from_front(b.elements) }
predicate full_buffer isa buffer when buffer.is_full;
method put(b@full_buffer, x) { ... } -- raise error or block caller
predicate non_full_buffer isa buffer when not(buffer.is_full;
method put(b@non_full_buffer, x) { add_to_back(b.elements, x); }
```

predicate partially\_full\_buffer isa non\_empty\_buffer, non\_full\_buffer;

The following diagram illustrates the inheritance hierarchy created by this example (the explicit inheritance link from the buffer object to buffer is omitted):



Predicate objects increase expressiveness for this example in two ways. First, important states of bounded buffers, e.g., empty and full states, are explicitly identified in the program and named. Besides documenting the important conditions of a bounded buffer, the predicate objects remind the programmer of the special situations that code must handle. This can be particularly useful during maintenance phases as code is later extended with new functionality. Second, attaching methods directly to states supports better factoring of code and eliminates *if* and *case* statements, much as does distributing methods among classes in a traditional object-oriented language. In the absence of predicate objects, a method whose behavior depended on the state of an argument object would include an *if* or *case* statement to identify and branch to the appropriate case; predicate objects eliminate the clutter of these tests and clearly separate the code for each case. In a more complete example, several methods might be associated with a particular state or behavior mode, we hope to improve the readability and maintainability of the code.

The syntax for a predicate object declaration is as follows:

```
predicate_decl ::= "predicate" name {relation} [field_inits] ["when" expr] ";"
```

## 2.4.1 Predicate Objects and Inheritance

For normal objects, one object is a child of another object exactly when the relationship is declared explicitly through isa declarations by the programmer. Predicate objects, on the other hand, support a form of automatic property-based classification: an object O is automatically considered a child of a predicate object P exactly when the following two conditions are satisfied:

- the object O is a descendant of each of the parents of the predicate object P, and
- the predicate expression of the predicate object *P* evaluates to true, when evaluated in a scope where each of the predicate object's parent names is bound to the object *O*.

By evaluating the predicate expression in a context where the parent names refer to the object being tested, the predicate expression can query the value or state of the object.

Since the state of an object can change over time (fields can be mutable), the results of predicate expressions evaluated on the object can change. If this happens, the system will automatically reclassify the object, recomputing its implicit inheritance links. For example, when a buffer object

becomes full, the predicates associated with the non\_full\_buffer and full\_buffer predicate objects both change, and the inheritance graph of the buffer object is updated. As a result, different methods may be used to respond to messages, such as the put message in the filled buffer example. Predicate expressions are evaluated lazily as part of method lookup, rather than eagerly as the state of an object changes. Only when the value of some predicate expression is needed to determine the outcome of method lookup is the predicate evaluated. A separate paper describes efficient implementation schemes for predicate objects [Chambers 93].

If a predicate object inherits from another predicate object, it is a special case of that parent predicate object. This is because the child predicate object will only be in force whenever its parent predicate object's predicate evaluates to true. In essence, the parent's predicate expression is implicitly conjoined with the child's predicate expression. A non-predicate object also may inherit explicitly from a predicate object, with the implication that the predicate expression will always evaluate to true for the child object; the system verifies this assertion dynamically. For example, an unbounded buffer object might inherit explicitly from the non\_full\_buffer predicate object.

predicate illustrated Α object need not have a when clause, as by the partially\_full\_buffer predicate object defined above. Such a predicate object may still depend on a condition if at least one of its ancestors is a predicate object. In the above example, the partially\_full\_buffer predicate object has no explicit predicate expression, yet since an object only inherits from partially\_full\_buffer whenever it already inherits from both non\_empty\_buffer and non\_full\_buffer, the partially\_full\_buffer predicate object effectively repeats the conjunction of the predicate expressions of its parents, in this case that the buffer be neither empty nor full.

Predicate objects are intended to interact well with normal inheritance among data abstractions. If an abstraction is implemented by inheriting from some other implementation, any predicate objects that specialize the parent implementation will automatically specialize the child implementation whenever it is in the appropriate state. For example, a new implementation of bounded buffers could be built that used a fixed-length array with insert and remove positions that cycle around the array:<sup>\*</sup>

```
object circular_buffer isa buffer;
field array(b@circular_buffer); -- a fixed-length array of elements
var field insert_pos(b@circular_buffer); -- an index into the array
var field remove_pos(b@circular_buffer); -- another integer index
method max_size(b@circular_buffer) { b.array.length }
method length(b@circular_buffer) {
    -- % is modulus operator
        (b.insert_pos - b.remove_pos) % b.array.length }
```

predicate non\_empty\_circular\_buffer isa circular\_buffer, non\_empty\_buffer;

<sup>\*</sup> This implementation overrides buffer's max\_size field with a method and then ignores the buffer's elements field. In practice a more efficient implementation would break up buffer into an abstract parent object and two child objects for the queue-based implementation and the circular array implementation.

```
method get(b@non_empty_circular_buffer) {
    var x := fetch(b.array, b.remove_pos);
    b.remove_pos := (b.remove_pos + 1) % b.array.length;
    x }
predicate non_full_circular_buffer isa circular_buffer, non_full_buffer;
    method put(b@non_full_circular_buffer, x) {
        store(b.array, b.insert_pos, x);
    }
```

The following diagram illustrates the extended inheritance graph for bounded and circular buffers (the partially\_full\_buffer predicate object is omitted):

b.insert\_pos := (b.insert\_pos + 1) % b.array.length; }



Since the circular\_buffer implementation inherits from the original buffer object, a circular\_buffer object will automatically inherit from the empty\_buffer or full\_buffer predicate object whenever the circular\_buffer happens to be in one of those states. No empty\_circular\_buffer or full\_circular\_buffer objects need to be implemented if specialized behavior is not needed. The non\_empty\_circular\_buffer and non\_full\_circular\_buffer predicate objects are needed to override the default get and put methods in the non-blocking states. Any object that inherits from circular\_buffer and that also satisfies the predicate associated with non\_empty\_buffer will automatically be classified as a non\_empty\_circular\_buffer.

The specification of when an object inherits from a predicate object implicitly places a predicate object just below its immediate parents and after all other normal children of the parents. For example, consider an empty circular buffer object. Both the buffer object and its parent, the circular\_buffer object, will be considered to inherit from the empty\_buffer predicate object. Because circular\_buffer is considered to inherit from empty\_buffer, any methods attached to circular\_buffer will override methods attached to empty\_buffer. Often this is the desired behavior, but at other times it might be preferable for methods attached to

predicate objects to override methods attached to "cousin" normal objects.<sup>\*</sup> If this were the case, then the buffer code could be simplified somewhat, as follows:

```
object buffer isa collection;
   ... -- elements, length, etc.
   method get(b@buffer) { remove from front(b.elements) }
   method put(b@buffer, x) { add_to_back(b.elements, x); }
predicate empty_buffer isa buffer when buffer.is_empty;
   method get(b@empty_buffer) { ... } -- raise error or block caller
predicate full_buffer isa buffer when buffer.is_full;
   method put(b@full_buffer, x) { ... } -- raise error or block caller
object circular_buffer isa buffer;
   ... -- array, insert pos, length, etc.
   method get(b@circular_buffer) {
      var x := fetch(b.array, b.remove_pos);
      b.remove_pos := (b.remove_pos + 1) % b.array.length;
      x }
   method put(b@circular_buffer, x) {
      store(b.array, b.insert_pos, x);
      b.insert_pos := (b.insert_pos + 1) % b.array.length; }
```

The non-blocking versions of get and put would be associated with the buffer object directly, and the non\_empty\_buffer, non\_full\_buffer, and partially\_full\_buffer predicate objects could be removed (if desired). The non-blocking get and put routines for circular buffers would similarly be moved up to the circular\_buffer object itself, with the non\_empty\_circular\_buffer and non\_full\_circular\_buffer predicate objects being removed also. If the methods attached to the empty\_buffer object were considered to override those of the circular\_buffer object, then sending get to a circular buffer that was empty would (correctly) invoke the empty\_buffer implementation. In the current semantics of predicate objects in Cecil, however, the circular\_buffer's implementation of get would be invoked, leading to an error. A third potential semantics would be to consider the predicate object to be unordered with respect to "cousin" objects, and methods defined on two cousins to be mutually ambiguous. More experience with predicate objects is needed to adequately resolve this question.

#### 2.4.2 Predicate Objects and Fields

Fields may be associated with a predicate object. This has the effect of reserving persistent space for the field in any object that might be classified as a descendant of the predicate object. The value stored in the field persists even when the field is inaccessible. At object-creation time, an initial value may be provided for fields potentially inherited from predicate objects, even if those fields may not be visible in the newly-created object. The semantics of accessing a field attached to a predicate object is governed by the semantics of accessing its corresponding accessor methods.

<sup>\*</sup> One object is a cousin of another if they share a common ancestor but are otherwise unrelated.

The following example exploits this semantics to implement a graphical window object that can be either expanded or iconified. Each of the two important states of the window remembers its own screen location (using a field named position in both cases), plus some other mode-specific information such as the text in the window and the bitmap of the icon, and this data persists across openings and closings of the window:

```
object window isa interactive_graphical_object;
   var field iconified(@window) := false;
   method display(w@window) {
      -- draw window using w.position
      method erase(w@window) {
      -- clear space where window is
      method move(w@window, new_position) {
      -- works for both expanded and iconified windows!
      w.erase; w.position := new position; w.display; }
predicate expanded_window isa window when not(window.iconified);
   var field position(@expanded window) := upper left;
   field text(@expanded window);
   method iconify(w@expanded_window) {
      w.erase; w.iconified := true; w.display; }
predicate iconified_window isa window when window.iconified;
   var field position(@iconfied_window) := lower_right;
   field icon(@iconified window);
   method open(w@iconified_window) {
      w.erase; w.iconified := false; w.display; }
method create_window(open_position, iconified_position,
                      text, icon) {
   object isa window {
      iconified := false,
      position@open_window := open_position,
      position@iconified_window := iconified_position,
      text := text, icon := icon } }
```

A window object has two position fields, but only one is visible at a time. This allows the display, erase, and move routines to send the message position as part of their implementation, without needing to know whether the window is open or closed. The create\_window method initializes both position fields when the window is created, even though the position of the icon is not visible initially. The position@object notation used in the field initialization resolves the ambiguity between the two position fields.

#### 2.5 Statements and Expressions

A statement is a declaration block, an assignment, or an expression:

```
stmt ::= decl_block
    assignment ";"
    expr ";"
```

An expression is either a literal, a reference to a variable or a named object, an object constructor expression, a vector constructor expression, a closure constructor expression, a message, a resend, or a parenthetical subexpression:

```
expr
               ::= binop_expr
binop_expr
               ::= binop_msg | unop_expr
unop_expr
               ::= unop_msg | dot_expr
dot_expr
               ::= dot_msg | simple_expr
simple_expr
               ::= literal
                    ref expr
                    vector_expr
                    closure expr
                    object expr
                    message
                    resend
                    paren expr
```

All of these constructs are described below, except for resends which are described later in section 2.8 and declarations other than variable declarations which are described in other sections.

## 2.5.1 Declaration Blocks

A declaration block is an unbroken sequence of declarations. Names introduced as part of the declarations in the declaration block are visible throughout the declaration block and also for the remainder of the scope containing the declaration block; the names go out of scope once the scope exits. Because the name of an object is visible throughout its declaration block, objects can inherit from objects defined later within the declaration block and methods can be specialized on objects defined later in the declaration block. Similarly, methods declared within a single declaration block can be mutually recursive and there is no need for forward declarations or the like. In environments where the top-level declaration block comprising the program is spread across multiple files, as in the UW Cecil implementation, the ability to attach methods to objects defined later in some other file is important.

#### 2.5.2 Variable Declarations

Variable declarations have the following syntax:

```
let_decl ::= "let" ["var"] name ":=" expr ";"
```

If the var annotation is used, the variable may be assigned a new value using an assignment statement. Otherwise, the variable binding is constant. (The contents of the variable may still be mutable.) Formal parameters are treated as constant variable bindings and so are not assignable. The initializing expression is evaluated in a context where the name of the variable being declared and any variables declared later within the same declaration block are considered undefined. This avoids potential misunderstandings about the meaning of apparently self-referential or mutually recursive initializers while still supporting a kind of let\* [Steele 84] variable binding sequence.

Variable declarations may appear at the top level as well as inside a method. However, the ordering of variable declarations at the top level (and consequently the order of evaluation of the initializing expressions) is less well defined. In the current UW Cecil implementation, the textual ordering of variable declarations is used to define an ordering for evaluating variable initializers. We would prefer a semantics that was independent of the "order" of variable declarations at the top level, so that all top-level declarations are considered unordered. Possible alternative semantics which have this property include restricting variable initialization expressions to be simple expressions without side-effects (thereby making the issue of evaluation order unimportant), eliminating variable declarations at the top level entirely, or supporting a form of on-demand at-most-once evaluation of top-level variable initializers akin to the lazy evaluation semantics of field initializers (see section 2.3.4).

## 2.5.3 Variable References

A variable or named object is referenced simply by naming the variable or object:

ref\_expr ::= name

The names of objects and variables are in the same name space. Lexical scoping is used to locate the closest lexically-enclosing variable or object binding for the name.

## 2.5.4 Assignment Statements

Assignment statements have the following syntax:

| assignment | ::= name ":=" expr | assignment to a variable            |
|------------|--------------------|-------------------------------------|
|            | assign_msg         | assignment-like syntax for messages |

If the left-hand-side is a simple name, then the closest lexically-enclosing binding of the name is located and changed to refer to the result of evaluating the right-hand-side expression. It is an error to try to assign to an object, a formal parameter, or to a variable declared without the var keyword.

If the left-hand-side has the syntax of a message, then the assignment statement is really syntactic sugar for a message send, as described in section 2.5.6.

#### 2.5.5 Literals

Cecil literal constants can be integers, floating point numbers, characters, or strings:

literal ::= integer | float | character | string

Literals are immutable objects.

#### 2.5.6 Message Sends

The syntax of a message send is as follows:

| message   | ::= | <pre>msg_name "(" [exprs] ")"</pre> |
|-----------|-----|-------------------------------------|
| exprs     | ::= | expr { "," expr }                   |
| unop_msg  | ::= | op_name unop_expr                   |
| binop_msg | ::= | binop_expr op_name binop_expr       |

A message is written in one of three forms:

- named prefix form, with the name of the message followed by a parenthesized list of expressions,\*
- unary operator prefix form, with the message name listed before the argument expression, or
- infix form, with the message name in between a pair of argument subexpressions.

Normally, a message whose name begins with a letter is written in named prefix form, while a message whose name begins with a punctuation symbol is written in unary prefix form or in infix form.<sup>†</sup> To invoke a named message as an operator, or to invoke an operator as a named message, the name of the message is prefixed with an underscore (the leading underscore is not considered part of the message name). For example, the following two expressions both send the + message to 3 and 4:

3 + 4 \_+(3, 4)

and the following two expressions both send the bit\_and message to 3 and 4:

bit\_and(3, 4)
3 \_bit\_and 4

The precedence and associativity of infix messages is specified through precedence declarations, described in section 2.6. The semantics of method lookup is described in section 2.7. Resends, a special kind of message send, are described in section 2.8.

Syntactic sugar exists for several common forms of messages. Dot notation allows the first argument of the message to be written first:

dot\_msg ::= dot\_expr "." msg\_name ["(" [exprs] ")"]

If the message takes only one argument, the trailing parentheses can be omitted. Consequently, the following three expressions all send the x message to p:

```
x(p)
p.x()
p.x
```

The following two expressions both send the bit\_and message to 3 and 4:

```
bit_and(3, 4)
3.bit_and(4)
```

This syntax may suggest that the first argument is more important than the others, but in fact the semantics is still that all arguments are treated uniformly, and any subset of the arguments might be dispatched at method-lookup time.

Other syntactic sugars support message sends written like assignments. Any message can appear on the left-hand-side of an assignment statement:

assign\_msg ::= lvalue\_msg ":=" expr sugar for set\_msg (exprs..., expr)

<sup>\*</sup> All arguments to the message must be listed explicitly; there is no implicit self argument.

<sup>&</sup>lt;sup>†</sup>Named prefix form is always used for method declarations.

In each of these cases, the name of the message sent to carry out the "assignment" is set\_ followed by the name of the message in the lvalue\_msg expression, and the arguments to the real message are the arguments of the lvalue\_msg expression followed by the expression on the right-hand-side of the "assignment." So the following three expressions are all equivalent:

```
set_foo(p, q, r);
foo(p, q) := r;
p.foo(q) := r;
```

as are the following two expressions:

set\_top(rectangle, x);
rectangle.top := x; -- frequently used for set accessor methods

as are the following two expressions:

```
set_!(v, i, x);
v!i := x;
```

Note that these syntactic sugars are assignments in syntax only. Semantically, they are all messages.

#### 2.5.7 Object Constructors

New objects are created either through object declarations (as described in section 2.1) or by evaluating object constructor expressions. The syntax of an object constructor expression is as follows:

object\_expr ::= "object" {relation} [field\_inits]

This syntax is the same as for an object declaration except that no object name is specified. Object constructor expressions are analogous to object instantiation operations found in class-based languages. The only difference between named objects introduced through object declarations and anonymous objects created through object constructor expressions is that named objects have statically-known names. As a consequence, only named objects can have methods and fields attached to them and can have descendants.

#### 2.5.8 Vector Constructors

A vector constructor expression is written as follows:

vector\_expr ::= "[" [exprs] "]"

The result of evaluating a vector constructor expression is a new immutable object that inherits from the predefined i\_vector object and is initialized with the corresponding elements.

#### 2.5.9 Closures

The syntax of a closure constructor expression is as follows:

closure\_expr ::= [ "&" "(" [closure\_formals] ")" ] "{" body "}"

closure\_formals::= closure\_formal { "," closure\_formal }
closure\_formal ::= [name] formal names are optional, if never referenced

This syntax is identical to that of a method declaration, except that the method keyword and message name are replaced with the & symbol (intended to be suggestive of the  $\lambda$  symbol). If the closure takes no arguments, then the &() prefix may be omitted. When evaluated, a closure constructor produces two things:

- a new closure object that inherits from the predefined closure object, which is returned as the result of the closure constructor expression, and
- a method named eval whose anonymous first argument is specialized on the newly-created closure object and whose remaining arguments are those listed as formal parameters in the closure constructor expression.

As with other nested method declarations, the body of a closure's eval method is lexically-scoped within the scope that was active when the closure was created. However, unlike nested method declarations, the eval method is globally visible (as long as the connected closure object is reachable). Closures may be invoked after their lexically-enclosing scopes have returned.<sup>\*</sup>

All control structures in Cecil are implemented at user level using messages and closures, with the sole exception of the loop primitive method described in section 2.2.3. Additionally, closures can be used to achieve much the same effect as exceptions and multiple results, so these other constructs are currently omitted from the Cecil language. Sometimes the use of closures is syntactically more verbose than a built-in language construct might be, and we are considering various alternatives for allowing programmers to define syntactic extensions to the language to provide a cleaner syntax for their user-defined control structures.

#### 2.5.10 Parenthetical Subexpressions

A parenthesized subexpression has the same syntax as the body of a method:

paren\_expr ::= "(" body ")"

Like the body of a method or a closure, a parenthetical subexpression introduces a new nested scope and may contain statements and local declarations.

#### 2.6 Precedence Declarations

Cecil programmers can define their own infix binary operators. Parsing expressions with several infix operators becomes problematic, however, since the precedence and associativity of the infix operators needs to be known to parse unambiguously. For example, in the following Cecil expression

```
foo ++ bar *&&! baz *&&! qux _max blop
```

the relative precedences of the ++, &&, and  $\max$  infix operators is needed, as is the associativity of the && infix operator. For a more familiar example, we'd like the following Cecil expression (\*\* represents exponentiation)

x + y \* z \*\* e \*\* f \* q

<sup>\*</sup> In the current UW Cecil implementation, there are some caveats to the use of such non-LIFO closures. See the system documentation for additional details.

to parse using standard mathematical rules, as if it were parenthesized as follows:

x + ((y \* (z \*\* (e \*\* f))) \* q)

#### 2.6.1 Previous Approaches

Most languages restrict infix operators to a fixed set, with a fixed set of precedences and associativities. This is not appropriate for Cecil, since we'd like the set of infix messages to be user-extensible.

Smalltalk defines all infix operators to be of equal precedence and left-associative. While simple, this rule differs from standard mathematical rules, sometimes leading to hard-to-find bugs. For example, in Smalltalk, the expression  $3 + 4 \times 5$  returns 35, not 23.

Self attempts to rectify this problem with Smalltalk by specifying the relative precedence of infix operators to be undefined, requiring programmers to explicitly parenthesize their code. This avoids problems with Smalltalk's approach, but leads to many unsightly parentheses. For example, the parentheses in the following Self code are all required:

(x <= y) && (y <= (z + 1))

Self makes an exception for the case where the same binary operator is used in series, treating that case as left-associative. For example, the expression

x + y + z

parses as expected in Self. Even so, the expression

x \*\* y \*\* z

would parse "backwards" in Self, if **\*\*** were defined. (Self uses power: for exponentiation, perhaps to avoid problems like this.) Also, expressions like

x + y - z

are illegal in Self, requiring explicit parenthesization.

Standard ML [Milner *et al.* 90] allows any operator to be declared prefix (called "nonfix" in SML) or infix, and infix operators can be declared left- or right-associative. Infix declarations also specify a precedence level, which is an integer from 0 (loosest binding) to 9 (tightest binding), with 0 being the default. For example, the following SML declarations are standard:

```
infix 7 *, /, div, mod;
infix 6 +, -;
infix 4 = <> < > <= >=;
infix 3 :=;
nonfix ~;
```

SML also provides special syntax to use an infix operator as a prefix operator, and vice versa.

A fixity declaration can appear wherever any other declaration can appear, and affect any parsing of expressions while the fixity declaration is in scope. Fixity declarations can be spread throughout a program, and multiple declarations can add independent operators to the same precedence level. Fixity declarations in one scope override any fixity declarations of the same operator from enclosing scopes.

One disadvantage of SML's approach is that is supports only 10 levels of precedence. It is not possible to add a new operator that is higher precedence than some operator already defined at level 9, nor is it possible to squeeze a new operator in between operators at adjacent levels. Finally, all operators at one level bind tighter than all operators at lower levels, even if the programmer might

have preferred that expressions mixing operators from completely different applications be explicitly parenthesized, for readability.

#### 2.6.2 Precedence and Associativity Declarations in Cecil

Cecil allows the precedence and associativity of infix operators to be specified by programmers through precedence declarations. The syntax of these declarations is as follows:

```
prec_decl ::= "precedence" op_list [associativity] {precedence} ";"
associativity ::= "left_associative" | "right_associative" | "non_associative"
precedence ::= "below" op_list | "above" op_list | "with" op_list
op_list ::= op_name { "," op_name }
```

For example, the following declarations might appear as part of the standard prelude for Cecil:

```
precedence ** right_associative; -- exponentiation
precedence *, / left_associative below ** above +;
precedence +, - left_associative below * above =;
precedence =, !=, <, <=, >=, > non_associative below * above;
precedence & left_associative below = above |;
precedence | left_associative below &;
precedence % with *;
precedence ! left_associative above =; -- array indexing
```

By default, an infix operator has its own unique precedence, unrelated to the precedence of any other infix operator, and is non-associative. Expressions mixing operators of unrelated precedences or multiple sequential occurrences of an operator that is non-associative must be explicitly parenthesized.

The effect of a precedence declaration is to declare the relationship of the precedences of several binary operators and/or to specify the associativity of a binary operator. Like SML, the information provided by a precedence declaration is used during the scope of the declaration, and declarations of the same operator at one scope override any from an enclosing scope. Two precedence declarations cannot define the precedence of the same operator in the same scope.

A precedence declaration of the form

```
precedence bin \cdot op_1, ..., bin \cdot op_n
associativity
below bin \cdot op_{B1}, ..., bin \cdot op_{Bn}
above bin \cdot op_{A1}, ..., bin \cdot op_{An}
with bin \cdot op_{W1}, ..., bin \cdot op_{Wn};
```

declares that all the *bin-op<sub>i</sub>* belong to the same precedence group, and that this group is less tightly binding than the precedence groups of any of the *bin-op<sub>Bi</sub>* and more tightly binding than those of the *bin-op<sub>Ai</sub>*. If any *bin-op<sub>Wi</sub>* are provided, then the *bin-op<sub>i</sub>* belong to the same precedence group as the *bin-op<sub>Wi</sub>*; all the *bin-op<sub>Wi</sub>* must already belong to the same precedence group. Otherwise, the *bin-op<sub>i</sub>* form a new precedence group. The associativity of the *bin-op<sub>i</sub>* is as specified by *associativity*, if present. If absent, then the associativity of the *bin-op<sub>i</sub>* is the same as the *bin-op<sub>Wi</sub>*, if provided, and non-associative otherwise. As illustrated by the example above, the ordering of two precedence groups may be redundantly specified. Cycles in the tighter-binding-than relation on precedence groups are not allowed. All operators in the same precedence group must have the same associativity.

Taken together, precedence declarations form a partial order on groups of infix operators. Parentheses may be omitted if adjacent infix operators are ordered according to the precedence declarations, or if adjacent infix operators are from the same precedence group and the precedence group has either left- or right-associativity. Otherwise, parentheses must be included. For example, in the expression

v ! (i + 1) < (v ! i) + 1

the parentheses around i+1 and v!i are required, since ! and + are not ordered by the above precedence declarations. However, both ! and + are more tightly binding than <, so no additional parentheses are required.

In Cecil, a declaration within a declaration block is visible throughout the block, including during textually earlier declarations within the block. This applies to precedence declarations as well, somewhat complicating parsing. The implementation strategy used in the UW Cecil system parses expressions involving binary operators into a list of operators and operands, and these lists are converted into a traditional parse tree form only after all visible declarations have been processed.

Precedence declarations apply to infix message names, not to individual methods. Multiple methods may implement the same infix message, for different kinds of arguments, but all methods with a particular name share the same precedence in a given scope.

## 2.7 Method Lookup

This section details the semantics of multi-method lookup, beginning with a discussion of the motivations and assumptions that led to the semantics.

## 2.7.1 Philosophy

All computation in Cecil is accomplished by sending messages to objects. The lion's share of the semantics of message passing specifies method lookup, and these method lookup rules typically reduce to defining a search of the inheritance graph. In single inheritance languages, method lookup is straightforward. Most object-oriented languages today, including Cecil, support multiple inheritance to allow more flexible forms of code inheritance and/or subtyping. However, multiple inheritance introduces the possibility of ambiguity during method lookup: two methods with the same name may be inherited along different paths, thus forcing either the system or the programmer to determine which method to run or how to run the two methods in combination. Multiple dispatching introduces a similar potential ambiguity even in the absence of multiple inheritance, since two methods with differing argument specializers could both be applicable but neither be uniformly more specific than the other. Consequently, the key distinguishing characteristic of method lookup in a language with multiple inheritance and/or multiple dispatching is how exactly this ambiguity problem is resolved.

Some languages resolve all ambiguities automatically. For example, Flavors [Moon 86] linearizes the class hierarchy, producing a total ordering on classes, derived from each class' local left-toright ordering of superclasses, that can be searched without ambiguity just as in the single inheritance case. However, linearization can produce unexpected method lookup results, especially if the program contains errors [Snyder 86]. CommonLoops [Bobrow *et al.* 86] and CLOS extend this linearization approach to multi-methods, totally ordering multi-methods by prioritizing argument position, with earlier argument positions completely dominating later argument positions. Again, this removes the possibility of run-time ambiguities, at the cost of automatically resolving ambiguities that may be the result of programming errors. Cecil takes a different view on ambiguity, motivated by several assumptions:

- We expect programmers will sometimes make mistakes during program development. The language should help identify these mistakes rather than mask or misinterpret them.
- Our experience with Self leads us to believe that programming errors that are hidden by such automatic language mechanisms are some of the most difficult and time-consuming to find.
- Our experience with Self also encourages us to strive for the simplest possible inheritance rules that are adequate. Even apparently straightforward extensions can have subtle interactions that make the extensions difficult to understand and use [Chambers *et al.* 91].
- Complex inheritance patterns can hinder future program evolution, since method lookup can depend on program details such as parent ordering and argument ordering, and it usually is unclear from the program text which details are important for a particular application.

Accordingly, we have striven for a very simple system of multiple inheritance and multiple dispatching for Cecil.

## 2.7.2 Semantics

Method lookup in Cecil uses a form of Touretzky's inferential distance heuristic [Touretzky 86], where children override parents. The method lookup rules interpret a program's inheritance graph as a partial ordering on objects, where being less in the partial order corresponds to being more specific: an object A is less than (more specific than) another object B in the partial order if and only if A is a proper descendant of B. This ordering on objects in turn induces an analogous ordering on the set of methods specialized on the objects, reflecting which methods override which other methods. In the partial ordering on methods with a particular name and number of arguments, one method M is less than (more specific than) another method N if and only if each of the argument specializers of M is equal to or less than (more specific than) the corresponding argument specializer of N. Since two methods cannot have the same argument specializers, at least one argument specializer of M must be strictly less than (more specific than) the corresponding specializer of A and unspecialized argument is considered specialized on the any object which is an ancestor of all other objects; a specialized argument therefore is strictly less than (more specific than) an unspecialized argument. The ordering on methods is only partial since ambiguities are possible.

Given the partial ordering on methods, method lookup is straightforward. For a particular message send, the system constructs the partial ordering of methods with the same name and number of arguments as the message. The system then throws out of the ordering any method that has an argument specializer that is not equal to or an ancestor of the corresponding actual argument passed in the message; such a method is not applicable to the actual call. Finally, the system attempts to locate the single most-specific method remaining, i.e., the method that is least in the partial order over applicable methods. If no methods are left in the partial order, then the system reports a "message not understood" error. If more than one method remains in the partial order, but there is no single method that overrides all others, then the system reports a "message ambiguous" error. Otherwise, there is exactly one method in the partial order that is strictly more specific than all other methods, and this method is returned as the result of the message lookup.
#### 2.7.3 Examples

For example, consider the following inheritance graph (containing only singly-dispatched methods for the moment):



The partial ordering on objects in this graph defines ABC to be more specific than either AB or AC, and both AB and AC are more specific than A. Thus, methods defined for ABC will be more specific (will override) methods defined in A, AB, or AC, and methods defined in either AB or AC will be more specific (will override) methods defined in A. The AB and AC objects are mutually unordered, and so any methods defined for both AB and AC will be unordered.

If the message ml is sent to the ABC object, both the implementation of ml whose formal argument is specialized on the ABC object and the implementation of ml specialized on A will apply, but the method specialized on ABC will be more specific than the one specialized on A (since ABC is more specific than A), and so ABC's ml will be chosen. If instead the ml message were sent to the AB object, then the version of ml specialized on the A object would be chosen; the version of ml specialized on ABC would be too specific and so would not apply.

If the m2 message is sent to ABC, then both the version of m2 whose formal argument is specialized on A and the one whose formal is specialized on AC apply. But the partial ordering places the AC object ahead of the A object, and so AC's version of m2 is selected.

If the m3 message is sent to ABC, then both AB's and AC's versions of m3 apply. Neither AB nor AC is the single most-specific object, however; the two objects are mutually incomparable. Since the system cannot select an implementation of m3 automatically without having a good chance of being wrong and so introducing a subtle bug, the system therefore reports an ambiguous message error. The programmer then is responsible for resolving the ambiguity explicitly, typically by writing a method in the child object which resends the message to a particular ancestor; resends are described in section 2.8. Sends of m3 to either AB or AC would be unambiguous, since the other method would not apply.

To illustrate these rules in the presence of multi-methods, consider the following inheritance graph (methods dispatched on two arguments are shown twice in this picture):



Methods m1 in A and m3 in AB illustrate that multiple methods with the same name and number of arguments may be associated with (specialized on) the same object, as long as some other arguments are specialized differently. The following table reports the results of several message sends using this inheritance graph.

| message      | invoked method or error  | explanation  |
|--------------|--------------------------|--|
| m1(ABC, XYZ) | m1(i@A, j@XZ)            | XZ overrides X   |
| m2(ABC, XYZ) | m2(j@AB, k)              | AB overrides A   |
| m3(ABC, XYZ) | m3(j@AB, k@XY)           | XY overrides unspecialized   |
| m4(AB, XY)   | "message not understood" | ABC too specific for AB $\Rightarrow$ no applicable method   |
| m5(ABC, XYZ) | "message ambiguous"      | AB overrides A but XZ overrides $X \Rightarrow$<br>no single most-specific applicable method               |
| m6(ABC, XYZ) | "message ambiguous"      | AC overrides unspecialized but XYZ overrides<br>unspecialized $\Rightarrow$ no single most-specific method |

### 2.7.4 Strengths and Limitations

The partial ordering view of multiple inheritance has several desirable properties:

• It is simple. It implements the intuitive rule that children override their parents (they are lesser in the partial ordering), but does not otherwise order parents or count inheritance links or invoke other sorts of complicated rules.

- Ambiguities are not masked. These ambiguities are reported back to the programmer at message lookup time before the error can get hidden. If the programmer has included static type declarations, the system will report the ambiguity at type-check-time.
- This form of multiple inheritance is robust under programming changes. Programmers can change programs fairly easily, and the system will report any ambiguities which may arise because of programming errors. More complex inheritance rules tend to be more brittle, possibly hindering changes to programs that exploit the intricacies of the inheritance rules and hiding ambiguities that reflect programming errors.
- Cecil's partial ordering view of multiple inheritance does not transform the inheritance graph prior to determining method lookup, as does linearization. This allows programmers to reason about method lookup using the same inheritance graph that they use to write their programs.

Of course, there may be times when having a priority ordering over parents or over argument positions would resolve an ambiguity automatically with no fuss. For these situations, it might be nice to be able to inform the system about such preferences. Self's prioritized multiple inheritance strategy can blend ordered and unordered inheritance, but it has some undesirable properties (such as sometimes preferring a method in an ancestor to one in a child) and interacts poorly with resends and dynamic inheritance.<sup>\*</sup> It may be that Cecil could support something akin to prioritized multiple inheritance (and perhaps even a prioritized argument list), but use these preferences as a last resort to resolving ambiguities; only if ambiguities remain after favoring children over parents would preferences on parents or argument position be considered. Such as design appears to have fewer drawbacks than Self's approach or CLOS's approach while gaining most of the benefits.

An alternative approach might be to support explicit declarations that one method is intended to override another method. These declarations would add relations to the partial order over methods, potentially resolving ambiguities. This approach has the advantage that it operates directly on the method overriding relationship rather than on parent order or the like which only indirectly affects method overriding relationships. Moreover, this approach can only resolve existing ambiguities, not change any existing overriding relationships, thereby making it easier to reason about the results of method lookup. To implement this approach, a mechanism for naming particular methods (e.g., the method's name and its specializers) must be added.

### 2.7.5 Multiple Inheritance of Fields

In other languages with multiple inheritance, in addition to the possibility of name clashes for methods, the possibility exists for name clashes for instance variables. Some languages maintain separate copies of instance variables inherited from different classes, while other languages merge like-named instance variables together in the subclass. The situation is simpler in Cecil, since all access to instance variables is through field accessor methods. An object (conceptually at least) maintains space for each inherited copy-down field, independently of their names (distinct fields with the same name are not merged automatically). Accesses to these fields are mediated by their accessor methods, and the normal multiple inheritance rules are used to resolve any ambiguities

<sup>&</sup>lt;sup>\*</sup> Recently, Self's multiple inheritance semantics has been greatly simplified, eliminating prioritized inheritance. Self's rules are now similar to Cecil's, except that Self omits the "children-override-parents" global rule. This has the effect of declaring as ambiguous messages such as m2 (ABC) in the first example in section 2.7.3.

among like-named field accessor methods. In particular, a method in the child with the same name as a field accessor method could send directed resend messages (described later in section 2.8) to access the contents of one or the other of the ambiguous fields.

### 2.7.6 Cyclic Inheritance

In the current version of Cecil, inheritance is required to be acyclic. However, cycles in the inheritance graph would be easy to allow. Instead of defining a partial order over objects, inheritance would define a preorder, where all objects participating in a cycle are considered to inherit from all other objects in the cycle, but not be more specific than any of them. This preorder on inheritance induces a corresponding preorder on methods. The same rules for successful method lookup still apply: a single most specific method must be found. If two methods are in a cycle in the method specificity preorder, then neither is more specific than the other. In effect, objects can participate in inheritance cycles if they define disjoint sets of methods. This design of "mutually-recursive" objects could be used to factor a single large object into multiple separate objects, each implementing a separate facet of the original object's implementation.

### 2.7.7 Method Lookup and Lexical Scoping

Since methods may be declared both at the top level and nested inside of methods, method lookup must take into account not only which methods are more specialized than which others but also which methods are defined in more deeply-nested scopes. The interaction between lexical scoping and inheritance becomes even more significant in the presence of modules as described in section 5.

The view of lexically-nested methods in Cecil is that nested methods *extend* the inheritance graph defined in the enclosing scope, rather than *override* it. We call this "porous" lexical scoping of methods, since the enclosing scope filters through into the nested scope. When performing method lookup for a message within some nested scope, the set of methods under consideration are those declared in the current scope plus any methods defined in lexically-enclosing scopes. If a local method has the same name, number of arguments, and argument specializers as a method defined in an enclosing scope, then the local method shadows (replaces) the method in the enclosing scope. Additionally, any object declarations or object extension declarations in the local scope are added to those declarations and extensions defined in enclosing scopes. Once this augmented inheritance graph is constructed, method lookup proceeds as before without reference to the scope in which some object or method is defined.

Other languages, such as BETA [Kristensen *et al.* 87], take the opposite approach, searching for a matching method in one scope before proceeding to the enclosing scope. If a matching method is found in one scope, it is selected even if a more specialized method is defined in an enclosing scope. More experience is needed to judge which of these alternatives is preferable. Cecil's approach gets some advantage by distinguishing variable references, which always respect only the lexical scope, from field references, which always are treated as message sends and primarily respect inheritance links. BETA uses the same syntax to access both global variables and inherited instance variables, making the semantics of the construct somewhat more complicated.

Nested methods can be used to achieve the effect of a typecase statement as found in other languages, including Trellis and Modula-3 [Nelson 91, Harbison 92]. For example, to test the implementation of an object, executing different code for each case, the programmer could write something like the following:

```
method test(x) {
    method typecase(z@obj1) { (-- code for case where x inherits from obj1 --) }
    method typecase(z@obj2) { (-- code for case where x inherits from obj2 --) }
    method typecase(z@obj3) { (-- code for case where x inherits from obj3 --) }
    method typecase(z) { (-- code for default case --) }
    typecase(x);
}
```

In the example, obj1, obj2, and obj3 may be related in the inheritance hierarchy, in which case the most-specific case will be chosen. If no case applies or no one case is most specific, then a "message not understood" or an "ambiguous message" error will result. These results fall out of the semantics of method lookup. By nesting the typecase methods inside the calling method, the method bodies can access other variables in the calling method through lexical scoping, plus the scope of the temporary typecase methods is limited to that particular method invocation. Eiffel's reverse assignment attempt and Modula-3's NARROW operation can be handled similarly.

### 2.7.8 Method Invocation

If method lookup is successful in locating a single target method without error, the method is invoked. A new activation record is created, formals in the new scope are initialized with actuals, the statements within the body of the method are executed in the context of this new activation record (or the primitive method is executed, or the field accessor method is executed), and the result of the method (possibly void) is returned to the caller.

### 2.8 Resends

Most existing object-oriented languages allow one method to override another method while preserving the ability of the overriding method to invoke the overridden version: Smalltalk-80 has super, CLOS has call-next-method, C++ has qualified messages using the :: operator, Trellis has qualified messages using the ' operator, and Self has undirected and directed resend (integrating unqualified super-like messages and qualified messages). Such a facility allows a method to be defined as an incremental extension of an existing method by overriding it with a new definition and invoking the overridden method as part of the implementation of the overriding method. This same facility also allows ambiguities in message lookup to be resolved by explicitly forwarding the message to a particular ancestor.

Cecil includes a construct for resending messages that adapts the Self undirected and directed resend model to the multiply-dispatched case. The syntax for a resend is as follows:

| resend      | ::= | "resend" [ "(" resend_arg            | gs ``)″]   |
|-------------|-----|--------------------------------------|--|
| resend_args | ::= | <pre>resend_arg { "," resend_a</pre> | arg }  |
| resend_arg  | ::= | expr                                 | corresponding formal of sender must be<br>unspecialized  |
|             |     | name<br>name ``@″ named_object       | undirected resend (name is a specialized formal)<br>directed resend (name is a specialized formal) |

The purpose of the resend construct is to allow a method to invoke one of the methods that the resending method overrides. Consequently, only methods with the same name and number of arguments as the resending method whose argument specializers are ancestors of the resending method's argument specializers are considered possible targets of a resend.

To invoke an overridden method, the normal prefix message sending syntax is used but with the following changes and restrictions:

- Syntactically, the name of the message is the keyword resend; semantically, the name of the message is implicitly the same as the name of the sending method.
- The number of arguments to the message must be the same as for the sending method.
- All specialized formal arguments of the resending method must be passed through unchanged as the corresponding arguments to the resend.

As a syntactic convenience, if all formals of the sender are passed through as arguments to the resend unchanged, then the simple resend keyword without an argument list is sufficient.

The semantics of a resent message are similar to a normal message, except that only methods that are less specific than the resending method in the partial order over methods are considered possible matches; this has the effect of "searching upwards" in the inheritance graph to find the single most-specific method that the resending method overrides. The restrictions on the name, on the number of arguments, and on passing specialized objects through unchanged ensures that the methods considered as candidates are applicable to the name and arguments of the send. Single-dispatching languages often have similar restrictions: Smalltalk-80 requires that the implicit self argument be passed through unchanged with the super send, and CLOS's call-next-method uses the same name and arguments as the calling method.

For example, the following illustrates how resends may be used to provide incremental extensions to existing methods:

```
object colored_rectangle isa rectangle;
field color(@colored_rectangle);
method display(r@colored_rectangle, d@output_device) {
    d.color := r.color; -- set the right color for this rectangle
    resend; -- do the normal rectangle drawing; sugar for resend(r, d)
}
```

Resends may also be used to explicitly resolve ambiguities in the method lookup by filtering out undesired methods. Any of the required arguments to a resend (those that are specialized formals of the resending method) may be suffixed with the @ symbol and the name of an ancestor of the corresponding argument specializer. This restricts methods considered in the resulting partial order to be those whose corresponding argument specializers (if present) are equal to or ancestors of the object named as part of the resend.

To illustrate, the following method resolves the ambiguity of height for vlsi\_cell in favor of the rectangle version of height:<sup>\*</sup>

<sup>\*</sup> This example was adapted from Ungar and Smith's original Self paper [Ungar & Smith 87].

```
object rectangle;
field height(@rectangle);
object tree_node;
method height(t@tree_node) { 1 + height(t.parent) }
object vlsi_cell isa rectangle, tree_node;
method height(v@vlsi_cell) { resend(v@rectangle) }
```

This model of undirected and directed resends is a simplification of the Self rules, extended to the multiple dispatching case. Self's rules additionally support prioritized multiple inheritance and dynamic inheritance, neither of which is present in Cecil. Self also allows the name and number of arguments to be changed as part of the resend. In some cases, it appears to be useful to be able to change the name of the message as part of the resend. For example, it might be useful to be able to provide access to the tree\_node version of the height method under some other name, but this currently is not possible in Cecil. We are investigating possible semantics for resends where the name of the message is changed, so that both ambiguously-inherited methods can be invoked.

As demonstrated by Self, supporting both undirected and directed resends is preferable to just supporting directed resends as does C++ and Trellis, since the resending code does not need to be changed if the local inheritance graph is adjusted. Since CLOS does not admit the possibility of ambiguity, it need only support undirected resends (i.e., call-next-method); there is no need for directed resends.

### 2.9 Files and Include Declarations

The current UW Cecil implementation is file-based. The compiler is given a single file name, naming the file containing the program to compile. To include other files into the program, a file can include an include declaration, at the global scope:

include\_decl ::= "include" file\_name ";"
file\_name ::= string
included\_file ::= top\_decl\_block

The effect of an include declaration is to include the declarations from the named file into the current scope. The named file must have the syntax of a single declaration block. File inclusion is idempotent: redundant inclusions of a file into a particular scope have no effect.

#### 2.10 Pragmas

Pragmas can be used by the Cecil programmer to provide additional information and implementation directives to the Cecil implementation. The set of recognized pragmas and their interpretation is implementation-dependent. A description of some of the pragmas supported by the UW Cecil implementation is provided in its documentation.

Pragmas are written as follows:

pragma ::= "(\*\*" expr "\*\*)"

The body of a pragma uses the syntax of a Cecil expression, but its interpretation is different (and implementation-dependent). Currently, pragmas may appear as part of most Cecil declarations. In the future, pragmas will likely be able to be provided for any declaration and any expression.

# 3 Static Types

Cecil supports a static type system which is layered on top of the dynamically-typed core language. The type system's chief characteristics are the following:

- Type declarations specify the interface required of an object stored in a variable or returned from a method, without placing any constraints on its representation or implementation.
- Argument specializers for method dispatching are separate from type declarations, enabling the type system to contain as special cases type systems for traditional single-dispatching and non-object-oriented languages.
- Code inheritance can be distinct from subtyping, but the common case where the two are parallel requires only one set of declarations.
- The type checker can detect statically when a message might be ambiguously defined as a result of multiple inheritance or multiple dispatching. It does not rely on the absence of ambiguities to be correct.
- The type system can check programs statically despite Cecil's classless object model.
- Type declarations are optional, providing partial language support for mixed exploratory and production programming.
- Parameterized objects, types, and methods support flexible forms of parametric polymorphism, complementing the inclusion polymorphism supported through subtyping.

This section describes Cecil's static type system in the absence of parameterization; section 4 extends this section to cope with parameterized objects and methods. Section 3.1 presents the major goals for the type system. Section 3.2 presents the overall structure of the type system. Sections 3.3, 3.4, and 3.5 describe the important kinds of declarations provided by programmers that extend the base dynamically-typed core language described in section 2. Sections 3.6, 3.7, 3.8, and 3.9 detail the type-checking rules for the language. Section 3.10 describes how the language supports mixed statically- and dynamically-typed code.

### 3.1 Goals

Static type systems historically have addressed many concerns, ranging from program verification to improved run-time efficiency. Often these goals conflict with other goals of the type system or of the language, such as the conflict between type systems designed to improve efficiency and type systems designed to allow full reusability of statically-typed code.

The Cecil type system is designed to provide the programmer with extra support in two areas: machine-checkable documentation and early detection of some kinds of programming errors. The first goal is addressed by allowing the programmer to annotate variable declarations, method arguments, and method results with explicit type declarations. These declarations help to document the interfaces to abstractions, and the system can ensure that the documentation does not become out-of-date with respect to the code it is documenting. Type inference may be useful as a programming environment tool for introducing explicit type declarations into untyped programs.

The Cecil type system also is intended to help detect programming errors at program definition time rather than later at run-time. These statically-detected errors include "message not understood," "message ambiguous," and "uninitialized field accessed." The type system is designed to verify that there is no possibility of any of the above errors in programs, guaranteeing type safety but possibly reporting errors that are not actually a problem for any particular execution of the program. To make work on incomplete or inconsistent programs easier, type errors are considered warnings, and the programmer always is able to run a program that contains type errors. Dynamic type checking at run-time is the final arbiter of type safety.

Cecil's type system is not designed to improve run-time efficiency. For object-oriented languages, the goal of reusable code is often at odds with the goal of efficiency through static type declarations; efficiency usually is gained by expressing additional representational constraints as part of a type declaration that artificially limit the generality of the code. Cecil's type system strives for specification only of those properties of objects that affect program correctness, i.e., the interfaces to objects, and not of how those properties are implemented. To achieve run-time efficiency, Cecil relies on advanced implementation techniques [e.g., Dean & Chambers 94, Dean *et al.* 95b, Grove *et al.* 95, Grove 95].

Finally, Cecil's type system is *descriptive* rather than *prescriptive*. The semantics of a Cecil program are determined completely by the dynamically-typed core of the program. Type declarations serve only as documentation and partial redundancy checks, and they do not influence the execution behavior of programs. This is in contrast to some type systems, such as Dylan's, where an argument type declaration can mean a run-time type check in some contexts and act as a method lookup specializer in other contexts.

The design of the Cecil type system is affected strongly by certain language features. Foremost of these is multi-methods. Type systems for single dispatching languages are based on the first argument of a message having control, consulting its static type to determine which operations are legal. In Cecil, however, any subset of the arguments to a method may be specialized, leaving the others unspecialized. This enables Cecil to easily model both procedure-based non-object-oriented languages and singly-dispatched object-oriented languages as important special cases, but it also requires the type system to treat specialized arguments differently than unspecialized arguments.

# 3.2 Types and Signatures

A *type* in Cecil is an abstraction of an object. A type represents a machine-checkable interface and an implied but unchecked behavioral specification, and all objects that *conform* to the type must support the type's interface and promise to satisfy its behavioral specification. One type may claim to be a *subtype* of another, in which case all objects that conform to the subtype are guaranteed also to conform to the supertype. The type checker verifies that the interface of the subtype conforms to the interface of the supertype, but the system must accept the programmer's promise that the subtype satisfies the implied behavioral specifications can be indicated. A type may have multiple direct supertypes, and in general the explicit subtyping relationships form a partial order. As

described in subsection 3.4, additional type constructors plus a few special types expand the type partial order to a full lattice.

A *signature* in Cecil is an abstraction of a collection of overloaded methods, specifying both an interface (a name, a sequence of argument types, and a result type) and an implied but uncheckable behavioral specification. The interface of a type is defined as the set of signatures that mention that type as one of their argument or result types.

For example, the following types and signatures describe the interface to lists of integers:

```
type int_list subtypes int_collection;
signature is_empty(int_list):bool;
signature length(int_list):int;
signature do(int_list, &(int):void):void;
signature pair_do(int_list, int_list, &(int,int):void):void;
signature prepend(int, int_list):int_list;
```

Types and signatures represent a contract between clients and implementors that enable message sends to be type-checked. The presence of a signature allows clients to send messages whose argument types are subtypes of the corresponding argument types in the signature, and guarantees that the type of the result of such a message will be a subtype of the result type appearing in the signature. Any message not covered by some signature will produce a "message not understood" error. Signatures also impose constraints on the implementations of methods, in order to make the above guarantees to clients. The collection of methods implementing a signature must be *conforming, complete*, and *consistent*:

- Conformance implies that each method implementing a signature has unspecialized argument types that are supertypes of the corresponding argument types of the signature and a result type that is a subtype of the signature's result type; conformance is Cecil's version of the standard contravariance rule found in singly-dispatched statically-typed languages.
- Completeness implies that the methods must handle all possible argument types that might appear at run-time as an argument to a message declared legal by the signature.
- Consistency implies that the methods must not be ambiguous for any combination of run-time arguments.

Checking completeness and consistency is the subject of section 3.6.2.

In a singly-dispatched language, each type has an associated set of signatures that defines the interface to the type. This association relies on the asymmetry of message passing in such languages, where only the receiver argument impacts method lookup. When type-checking a singly-dispatched message, the type of the receiver determines the set of legal operations, i.e., the set of associated signatures. If a matching signature is found, then the message will be understood at run-time; the static types of the remaining message arguments is checked against the static argument types listed in the signature. For Cecil, we wish to avoid the asymmetry of this sort of type system. Consequently, we view a signature as associated with each of its argument types, not just the first, much as a multi-method in Cecil is associated with each of its argument specializer

objects. For example, the prepend signature above is considered part of both the int type and the int\_list type.

In most object-oriented languages, the code inheritance graph and the subtyping graph are joined: a class is a subtype of another class if and only if it inherits from that other class. Sometimes this constraint becomes awkward [Snyder 86], for example when a class supports the interface of some other class or type, but does not wish to inherit any code. Other times, a class reusing another class's code cannot or should not be considered a subtype; covariant redefinition as commonly occurs in Eiffel programs is one example of this case [Cook 89].

To increase flexibility and expressiveness, Cecil separates subtyping from code inheritance. Types and signatures can be declared independently of object representations and method implementations. However, since in most cases the subtyping graphs and the inheritance graphs are parallel, requiring programmers to define and maintain two separate hierarchies would become too onerous to be practical. To simplify specification and maintenance of the two graphs, in Cecil the programmer can specify both a type and a representation, and the associated subtyping, conformance, and inheritance relations, with a single declaration. Similarly, a single declaration can be used to specify both a signature and a method implementation. In this way we hope to provide the benefits of separating subtyping from code inheritance when it is useful, without imposing additional costs when the separation is not needed.

# 3.3 Type and Signature Declarations

Variable declarations and formal arguments and results of methods, closures, and fields may be annotated with type declarations. The syntax of declarations is extended to include some new declarations:

decl

```
::= let decl
    tp decl
    type_ext_decl
    object_decl
    obj ext decl
    predicate_decl
    disjoint decl
    cover decl
    divide decl
    signature_decl
    method decl
    field_sig_decl
    field decl
    precedence decl
    include_decl
    prim decl
```

In this and subsequent syntax specifications, changes to specifications as described in section 2 are in boldface.

The following example illustrates some of the extensions:

```
object list;
method is_empty(l@:list):bool { l.length = 0 }
signature length(l:list):int;
```

```
signature do(l:list, closure:&(int):void):void;
signature pair_do(l1:list, l2:list, closure:&(int,int):void):void;
method prepend(x:int, l@:list):list {
    object inherits cons { head := x, tail := 1 } }
method copy_reverse(l:list):list {
    let var l2:list := nil;
    do(l, &(x:int){ l2 := prepend(x, l2); };
    l2 }
representation cons isa list;
field head(@:cons):int;
field tail(@:cons):list;
```

#### 3.3.1 Type Declarations

New user-defined types are introduced with type declarations of the following form (ignoring parameterization and encapsulation aspects):

```
tp_decl ::= "type" name {type_relation} ";"
type_relation ::= "subtypes" types
types ::= type { "," type }
```

The new type is considered to be a subtype of each of the types listed in the subtypes clause. The induced subtype relation over used-defined types must be a partial order (i.e., it cannot contain cycles).\*

Type names are interpreted in a name space distinct from that of objects and variables and that of message names. A type, an object, and a method may all be named list unambiguously.

#### 3.3.2 Representation and Object Declarations

New user-defined objects are introduced with representation declarations of the following form (again, ignoring parameterization and encapsulation):

| object_decl | ::= rep_role rep_kind name  | e {relation} [field_inits] ``;"   |
|-------------|---|---|
| rep_kind    | ::= "representation"<br>  "object"  | declares an object implementation<br>declares an object type and implementation   |
| relation    | ::= <b>"subtypes" types</b><br>  <b>"inherits" parents</b><br>  "isa" parents | impl conforms to type, type subtypes from type<br>impl inherits from impl<br>impl inherits from impl, type subtypes from type |

Representation roles will be described in section 3.5.

If the representation keyword is used, the declaration introduces a new object representation. This object inherits from the objects named in each inherits clause and conforms to the types named in each subtypes clause. As mentioned in section 2.1.1, the inheritance graph cannot have cycles.

An isa clause is syntactic sugar for both a subtypes clause and an inherits clause, i.e., sugar for the case where inheritance and subtyping are parallel. So the following declaration

<sup>&</sup>lt;sup>\*</sup> It is not strictly necessary to restrict subtyping to a partial order. Cycles in the subtypes relation could be allowed, producing a preorder over types instead of a partial order. This would have any type in a cycle being a subtype of and therefore substitutable for every other type in the cycle. In essense, all types in a cycle would be equivalent as far as the type checker was concerned.

```
representation cons isa list;
```

is syntactic sugar for the declaration

```
representation cons inherits list subtypes typeof(list);
```

where *typeof*(list) represents the most-specific type(s) to which the list object conforms (*typeof* is not legal Cecil syntax).

If the object keyword is used, then the declaration is syntactic sugar for the pair of an object representation declaration and a type declaration. A declaration of the form

```
object name inherits name_{i1}, name_{i2}, ..., name_{in}
subtypes name_{s1}, name_{s2}, ..., name_{sm}
isa name_{b1}, name_{b2}, ..., name_{bk};
```

is syntactic sugar for the following two declarations:

```
type name subtypes name_{s1}, name_{s2}, ..., name_{sm},

typeof(name_{b1}), typeof(name_{b2}), ..., typeof(name_{bk});

representation name

inherits name_{i1}, name_{i2}, ..., name_{in}, name_{b1}, name_{b2}, ..., name_{bk}

subtypes name ;
```

Both the object and the type have the same name, but there is no potential for ambiguity since object and type names are resolved in separate name spaces. The new type subtypes from all the types listed in the subtypes clause and from the types to which the objects in the isa clause of the original declaration conform. The new object representation conforms to the new type and inherits from the object representations listed in the inherits and isa clauses of the original declaration.

The object and isa syntactic sugars are designed to make it easy to specify the inheritance and subtyping properties of an object/type pair for the common case that code inheritance and subtyping are parallel. We expect that in most programs, only object and isa declarations will be used; type, representation, inherits, and subtypes declarations are intended for relatively rare cases where finer control over inheritance and subtyping are required.

Object constructor expressions are similarly extended with representation roles, representation kinds, and subtyping relationships:

object\_expr ::= rep\_role rep\_kind {relation} [field\_inits]

In an object constructor expression, both the representation keyword and the object keyword have the same effect; the presence or absence of an anonymous type is immaterial.

Representations often add new, implementation-specific operations. For example, the cons representation defined earlier introduced the head and tail fields. To be able to send messages that access these new features, a type must exist that includes the appropriate signatures. If cons were only a representation, then a separate type would need to be defined that included signatures for head and tail. To avoid this extra step, a representation declaration, like an object declaration, introduces a corresponding type. Unlike an object declaration, however, the type derived from a representation declaration is anonymous. It can only be referenced indirectly through the *typeof* internal function that specifies the semantics of the isa and @: syntactic sugars

(section 3.3.5 describes the @: sugar). Consequently, no variables or unspecialized formals may be declared to be of the anonymous type, and no types may be declared to be subtypes of the anonymous type. This enables object representations to be defined that are not treated as first-class types; the programmer has control over which types are intended to be used in type declarations.

### 3.3.3 Type and Object Extension Declarations

As described in section 2.1.3, objects can be extended with new inheritance relations after they have been defined. In a similar fashion, types can be extended with new subtyping relations using type extension declarations of the following form:

type\_ext\_decl ::= "extend" "type" named\_type {type\_relation} ";"

The syntax of object extension declarations is extended to support augmenting either just an object representation or both an representation and a type:

| obj_ext_decl | ::= | <pre>"extend" extend_kind nam {relation} [field_in</pre> |  |
|--------------|-----|--|--|
| extend_kind  |     | "representation"<br>["object"]                           | extend representation<br>extend both type and representation |

If the extension uses the representation keyword, then the named representation is extended with the appropriate inheritance and conformance relations. Otherwise, both the representation and the type that are named by the extension are updated. A declaration of the form

```
extend object name inherits name_{i1}, name_{i2}, ..., name_{in}
subtypes name_{s1}, name_{s2}, ..., name_{sm}
isa name_{b1}, name_{b2}, ..., name_{bk};
```

is syntactic sugar for the following two declarations:

It is an error if there does not exist both a representation and a type with the corresponding name.

Allowing types to be extended externally to have additional supertypes allows third-parties to integrate separately-developed libraries without modifying the separate libraries directly [Hölzle 93].

#### 3.3.4 Signature Declarations

Signatures can be declared using the following syntax:

The names of formals in a signature are for documentation purposes only; they do not impact the meaning of the signature nor do they have any effect during type checking.

Signatures can also be declared in a field-like notation, as follows:

A field signature declaration of the form

```
var field signature name(type):type<sub>R</sub>;
```

is syntactic sugar for the following two declarations:

```
signature name(type):type<sub>R</sub>;
signature set_name(type,type<sub>R</sub>):void;
```

A field signature declaration does not require that implementations of the resulting signatures be fields, only that their interface "looks" like they could be implemented by fields. If the var keyword is omitted, then the second set accessor signature is not generated.

3.3.5 Implementation and Method Declarations

The syntax of method implementations is extended in the following way to accommodate static types:

| method_decl | ::=     | <pre>impl_kind method_name     "(" [formals] ")" [ty     "{" (body   prim_body</pre> |   |
|-------------|---------|--|---|
| impl_kind   | ::=<br> | ["method"] "implementatic"<br>"method"   | n" declares a method implementation<br>declares a method signature and implementation |
| specializer | ::=<br> | <pre>[location] [type_decl] "@" ":" object</pre>                                     | specialized formal<br>sugar for @object :object                                       |

Formal parameters of the method implementation and the result of the method implementation can be given explicit type declarations.

If the implementation keyword is used, the declaration introduces a new method implementation. If, however, the method keyword alone is used, the declaration is syntactic sugar for both a method implementation declaration and a signature declaration. A declaration of the form

```
method name(x_1@obj_1:type_1, ..., x_N@obj_N:type_N):type_R \{ body \}
```

is syntactic sugar for the following two declarations:

As explained in section 2.2.1, if any of the  $obj_i$  are omitted, they default to any.

A formal in a method or field declaration can be specified with the x@:object syntax. This syntax is shorthand for x@object:typeof(object).

#### 3.3.6 Field Implementation Declarations

Field implementation declarations are similarly extended to accommodate static types:

declare accessor method impl(s) and sig(s) declare just accessor method implementation(s)

If the implementation keyword is used, then the declaration introduces a field get accessor method implementation, and also a set accessor method implementation if the field is declared with the var keyword. The result type of the field is used as the type of the second argument of the set accessor method; the result type of the set accessor method is void.

If the plain field keyword is used, then the field declaration is syntactic sugar for a field implementation declaration and a field signature declaration. A field declaration of the form

```
shared? var? field name(x@obj:type):type<sub>R</sub> := expr;
```

where *shared*? is either the shared keyword or empty and *var*? is the var keyword or empty, is syntactic sugar for the following declarations:

shared? var? field implementation name(x@obj:type):type<sub>R</sub> := expr; var? field signature name(type):type<sub>R</sub>;

The field signature declaration is itself syntactic sugar for one or two signature declarations, depending on whether the var keyword was used.

### 3.3.7 Other Type Declarations

In addition to allowing the formals and results of methods and fields to be annotated with explicit type declarations, variable declarations and closure arguments and results can be annotated with explicit type declarations:

```
let_decl ::= "let" ["var"] name [type_decl] ":=" expr ";"
closure_expr ::= [ "&" "(" [closure_formals] ")" [type_decl] ] "{" body "}"
closure_formal ::= [name] [type_decl] formal names are optional, if never referenced
```

If the result type of a closure is omitted, instead of defaulting to dynamic as described in section 3.4.1, the result type is inferred from the type of the result expression in the closure's body. Similarly, if the type of a constant local variable is omitted, it is inferred from the type of its initializing expression; mutable variables and global variables should be given explicit types to avoid dynamic type checking.

### 3.3.8 Discussion

Subtyping and conformance in Cecil is explicit, in that the programmer must explicitly declare that an object conforms to a type and that a type is a subtype of another type. These explicit declarations are verified as part of type checking to ensure that they preserve the required properties of conformance and subtyping. Explicit declarations are used in Cecil instead of implicit inference of the subtyping relations (*structural subtyping*) for two reasons. One is to provide programmers with error-checking of their assumptions about what objects conform to what types and what types are subtypes of what other types. Another is to allow programmers to encode additional semantic information in the use of a particular type in additional to the information implied by the type's purely syntactic interface. Both of these benefits are desirable as part of Cecil's goal of supporting production of high-quality software. To make exploratory programming easier, a programming environment tool could infer the greatest possible subtype relationships (i.e., the implicit "structural" subtyping relationships) for a particular object and add the appropriate explicit subtype declarations automatically.

Separating subtyping from implementation inheritance increases the complexity of Cecil. A simpler language might provide only subtyping, and restrict objects to inherit code only from their supertypes; Trellis takes this approach, for example. However, there is merit in clearly separating the two concepts, and allowing inheritance of code from objects which are not legal supertypes. Studies have found this to be fairly common in dynamically-typed languages [Cook 92]. With the current Cecil design, the only way that an object might not be a legal (structural) subtype of an object from which it inherits is if the child overrides a method of the parent and restricts at least one argument type declaration, a relatively rare occurrence. However, Cecil may eventually support filtering and transforming operations as part of inheritance, such as the ability to exclude operations, to rename operations, or to systematically adjust the argument types of operations, and so would create more situations in one object would inherit from another without being a subtype.

Types cannot have default implementations; only object representations can have methods attached. In other languages, such as Axiom (formerly Scratchpad II) [Watt *et al.*, Jenks & Sutor 92], default implementations can be stored with the type (called the *category* in Axiom). However, in Axiom method lookup rules are complicated by the possibility of methods being inherited both from superclasses and from categories, i.e., along both inheritance and subtyping links. Cecil's inheritance rules are simplified by only searching the inheritance graph. We expect that most type-like entities will actually be declared using the object form so that there is a corresponding representation to hold any default method implementations.

# 3.4 Special Types and Type Constructors

The syntax of types (excluding parameterization) is as follows:

```
type ::= named_type
    closure_type
    lub_type
    glb_type
    "(" type ")" just for grouping
```

# 3.4.1 Named Types

Types with names can be directly named:

named\_type ::= name

As described in section 3.3.1, type names are resolved in a name space distinct from the names of variables and objects and of methods.

In addition to user-defined types introduced through type and object declarations, the Cecil type system includes four special predefined types:

• The type void is used as the result type of methods and closures that do not return a result. All types are subtypes of void, enabling a method that returns a result to be used in a context where none is required. The type void may only be used when declaring the result type of a method or closure. The predefined object void has type void.

- The type any is implicitly a supertype of all types other than void; any may be used whenever a method does not require any special operations of an object.
- The type none is implicitly a subtype of all other types, thus defining the bottom of the type lattice. It is the result type of a closure that terminates with a non-local return, since such a closure never returns to its caller. It also is the result type of the primitive loop method, which also never returns normally. Finally, none is an appropriate argument type for closures that will never be called.
- The type dynamic is used to indicate run-time type checking. Wherever type declarations are omitted, dynamic is implied (with the exception of closure results and constant local variable declarations, as described in section 3.3.7). The dynamic type selectively disables static type checking, in support of exploratory programming, as described in section 3.10.

#### 3.4.2 Closure Types

The type of a closure is described using the following syntax:

```
closure_type ::= "&" "(" [arg_types] ")" [type_decl]
```

(The syntax of arg\_types is specified along with signatures in section 3.3.4.)

A closure type of the form

 $\&(t_1, ..., t_N): t_R$ 

describes a closure whose eval method has the signature:

**signature** eval(&( $t_1, \ldots, t_N$ ): $t_R, t_1, \ldots, t_N$ ): $t_R$ 

Closure types are related by implicit subtyping rules that reflect standard contravariant subtyping: a closure type of the form  $\&(t_1, \dots, t_N) : t_R$  is a subtype of a closure type of the form  $\&(s_1, \dots, s_N) : s_R$  iff each  $t_i$  is a supertype of the corresponding  $s_i$  and  $t_R$  is a subtype of  $s_R$ .

### 3.4.3 Least-Upper-Bound Types

The least upper bound of two types in the type lattice is notated with the following syntax:

```
lub_type ::= type "|" type
```

The type  $type_1 | type_2$  is a supertype of both  $type_1$  and  $type_2$ , and a subtype of all types that are supertypes of both  $type_1$  and  $type_2$ . Least-upper-bound types are most useful in conjunction with parameterized types, described in section 4.

### 3.4.4 Greatest-Lower-Bound Types

The greatest lower bound of two types is notated with the following syntax:

glb\_type ::= type "&" type

The type  $type_1 \& type_2$  is a subtype of both  $type_1$  and  $type_2$ , and a supertype of all types that are subtypes of both  $type_1$  and  $type_2$ . Syntactically, the greatest-lower-bound type constructor has higher precedence than the least-upper-bound type constructor.

Note that the greatest-lower-bound of two types is different than a named type that is a subtype of the two types. For example,

type1 & type2

is a different type than the type introduced by the declaration

```
type type3 subtypes type1, type2;
```

The type 1 is a subtype of type1 & type2 (all types that subtype both type1 and type2 are automatically subtypes of type1 & type2), but not identical to it. The reason is that the programmer might later define a type4 type:

type type4 subtypes type1, type2;

The type type4 is also a subtype of type1 & type2, but type3 and type4 are different and in fact mutually incomparable under the subtype relation. The two types are different because named types include implicit behavioral specifications, and the implication of the two separate type declarations is that the implied behavioral specifications of type3 and type4 are different.

The void, any, and none special types and the greatest-lower-bound and least-upper-bound type constructors serve to extend the explicitly-declared type partial order generated from type and object declarations to a full lattice.

#### 3.5 Object Role Annotations

Because Cecil is classless, objects are used both as run-time entities and as static, program structure entities. Some objects, such as nil and objects created at run-time through object constructor expressions, are manipulated at run-time and can appear as arguments to messages at run-time. Such *concrete* objects are required to have all the signatures in their types be supported by corresponding method implementations and all their fields be initialized. In contrast, objects such as cons and list are not directly manipulated at run-time. Instead, they help organize programs, providing repositories for shared methods and defining locations in the type lattice. In return for restricted usage, such *abstract* objects are not required to have their fields fully initialized nor their signatures fully implemented.

To inform the type checker about the part played by an object, its declaration is prefixed with an object representation role annotation:

| rep_role | ::= | "abstract"  | only inherited from by named objects;<br>allowed to be incomplete    |
|----------|-----|-------------|--|
|          |     | "template"  | only inherited from or instantiated;<br>uninitialized fields allowed |
|          |     | "concrete"  | directly usable;<br>must be complete and initialized                 |
|          |     | ["dynamic"] | directly usable;<br>no static checks                                 |

Each of these role annotations appears in the list hierarchy:

```
abstract object list isa collection;
template representation cons isa list;
concrete representation nil isa list;
```

Abstract objects are potentially incomplete objects designed to be inherited from and fleshed out by other objects. Abstract objects need not have all their signatures fully implemented nor their fields initialized. For example, the list object is not required to implement the do signature defined for the type list; the implementation of this operation is deferred to children. Because an abstract object may be incomplete, it cannot be used directly at run-time, nor can it appear as a parent in an object constructor declaration. Abstract objects are similar to abstract classes in class-based languages.

Template objects are complete objects suitable for direct "instantiation" by object constructor expressions, but are not allowed to be used directly as a value at run-time. Because new method implementations cannot be specified for anonymous objects, all the signatures specified as part of the type of a template object are required to be fully implemented. For example, the cons object is required to fully implement all list operations, including do. However, because template objects will not be sent messages at run-time, they are not required to have their fields initialized. The cons object is not required to have its head and tail fields initialized. Template objects are analogous to concrete classes in class-based languages.

Concrete objects are complete, initialized objects that can be manipulated at run-time. Like template objects, all signatures must be implemented, and in addition all fields must be initialized, either as part of the field declaration or as part of the object declaration or object constructor expression. Like other named objects, named concrete objects can be inherited from as well. (The child object's role can revert to abstract or template.) Anonymous concrete objects correspond to instances in class-based languages; named concrete objects have no direct analogue and are a feature of Cecil's object model.

If the object role annotation is dynamic or omitted, the object is considered fully manipulable by programs but no static checks for incomplete implementation of signatures or uninitialized fields are performed. (The appropriate checks will be made dynamically, as messages are sent and fields accessed.) Dynamic objects are designed to support exploratory programming, as discussed in section 3.10.

Since object constructor expressions create objects to be used at run-time, neither abstract nor template annotations are allowed on object constructor expressions.

Object role annotations help document explicitly the programmer's intended uses of objects. Other languages provide similar support. C++ indirectly supports differentiating abstract from concrete classes through the use of pure virtual functions and private constructors. Eiffel supports a similar mechanism through its deferred features and classes mechanism. Cecil's abstract annotation is somewhat more flexible than these approaches, since an object can be labeled abstract explicitly, even if it has no abstract methods. Such a declaration can be useful to prevent direct instantiation of the object, perhaps because the method implementations are mutually recursive in a way where subclasses are expected to override at least one of the methods to break the recursion.

In an earlier version of Cecil, a fifth annotation, unique, could be used to document the fact that an object was unique. For example, nil, true, and false all were annotated as unique objects. While the exact semantics of unique was unclear, a plausible interpretation could be that a unique object is like a concrete object except that it could not be used as a parent in an object constructor expression (i.e., it could not be "instantiated" or "copied"). Unique objects could still be inherited from in object declarations, since they might have useful code to be inherited. Unique objects were removed because it was felt that the extra language mechanism was not worthwhile. The template annotation may be removed for a similar reason, since it is not strictly necessary for the type checker, but the distinction between abstract and template objects appears to be useful for documenting the programmer's intentions. The distinction between abstract objects and concrete objects, however, is crucial to being able to write and type-check realistic Cecil code.

# 3.6 Type Checking Messages

This section describes Cecil's type checking rules for message sends and method declarations. Section 3.7 describes type checking for other, simpler kinds of expressions. Parameterized types are described in section 4.

In Cecil, all control structures, instance variable accesses, and basic operators are implemented via message passing, so messages are the primary kind of expression to type-check. For a message to be type-correct, there must be a single most-specific applicable method implementation defined for all possible argument objects that might be used as an argument to the message. However, instead of directly checking each message occurring in the program against the methods in the program, in Cecil we check messages against the set of signatures defined for the argument types of the message, and then check that each signature in the program is implemented conformingly, completely, and consistently by some group of methods.

Using signatures as an intermediary for type checking has three important advantages. First, the type-checking problem is simplified by dividing it into two separable pieces. Second, checking signatures enables all interfaces to be checked for conformance, completeness, and consistency independent of whether messages exist in the program to exercise all possible argument types. Finally, signatures enable the type checker to assign blame for a mismatch between implementor and client. If some message is not implemented completely, the error is either "message not understood" or "message not implemented correctly." If the signature is absent, it is the former, otherwise the latter. Signatures inform the type checker (and the programmer) of the intended interfaces of abstractions, so that the system may report more informative error messages. Of course, the "missing signature" error is sometimes the appropriate message to report, but the type checker cannot accurately distinguish this from the "message not understood" alternative.

Subsection 3.6.1 describes checking messages against signatures, and subsection 3.6.2 describes checking signatures against method implementations.

### 3.6.1 Checking Messages Against Signatures

Given a message of the form *name* ( $expr_1, ..., expr_N$ ), where each  $expr_i$  type-checks and has static type  $T_i$ , the type checker uses the  $T_i$  to locate all signatures of the form *name* ( $S_1, ..., S_N$ ) :  $S_R$  where each type  $S_i$  is a supertype of the corresponding  $T_i$ . If this set of applicable signatures is empty, the checker reports a "message not understood" error. Otherwise, the message send is considered type-correct.

To determine the type of the result of the message send, the type system calculates the mostspecific result type of any applicable signature. This most-specific result type is computed as the greatest lower bound of the result types of all applicable signatures. In the absence of other type errors, this greatest lower bound will normally correspond to the result type of the most-specific signature.

To illustrate, consider the message copy(some\_list), where the static type of some\_list is list. The following types and signatures are assumed to exist:

```
type collection;
type list subtypes collection;
type array subtypes collection;
signature copy(collection):collection;
signature copy(list):list;
signature copy(array):array;
```

The signature copy(array):array is not applicable, since list, the static type of some\_list, is not a subtype of array. The dynamic type of some\_list might turn out to conform to array at run-time (e.g., if there were some data structure that was both a list and an array), but the static checker cannot assume this and so must ignore that signature. The first two signatures do apply, so the copy message is considered legal. The type of the result is known to be both a list and a collection. The greatest lower bound of these two is list, so the result of the copy message is of type list.

Unlike method dispatching, it is acceptable for more than one signature to be applicable to a message. Signatures are contracts that clients can assume, and if more than one signature is applicable, then the client can assume more guarantees about the type of the result. The greatest lower bound is used to calculate the message's result type, rather than the least upper bound, because each signature can be assumed to be in force. At run-time, a method will be selected, and that method will be required to honor the result type guarantees of all the applicable signatures, and so the target method implementation will return an object that conforms to the result types of all the applicable signatures, i.e., the greatest lower bound of these signatures. In common practice, some most-specific signature's result type will be the greatest lower bound, such as the list type selected above.

### 3.6.2 Checking Signatures Against Method Implementations

The type checker ensures that, for every signature in the program, all possible messages that could be declared type-safe by the signature would in fact locate a single most-specific method with appropriate argument and result type declarations, given the current set of representation and type declarations in the program. This involves locating all methods to which the signature is applicable (i.e., all those that could be invoked by a message covered by the signature) and ensuring that they conformingly, completely, and consistently implement the signature.

More precisely:

• A signature is considered *applicable* to a method iff they have the same name and number of arguments and there exists some sequence of argument objects that both inherits from the specializers of the method and conforms to the argument types of the signature. Abstract objects are not included when considering possible argument objects, since they are not required to be complete implementations and are restricted from being manipulated at run-

time. (This is the key distinction between abstract and non-abstract objects.) Template objects are included, since they are required to fully implement all applicable signatures.

- A method *conforms* to a signature iff
  - for each formal, all objects that inherit from the formal's specializer and conform to the signature's corresponding argument type also conform to the formal's declared type (for unspecialized formals, this constraint amounts to requiring that the formal's type is a supertype of the signature argument's type), and
  - the method's result type is a subtype of the signature's result type.
- A set of methods *completely* implement a signature iff, for each possible sequence of argument objects that conforms to the argument types in the signature, there exists at least one method in the set that is applicable to the argument objects, i.e., where the argument objects inherit from the method's specializers.
- A set of methods *consistently* implement a signature iff, for each possible sequence of argument objects that conforms to the argument types in the signature, there exists a single most-specific applicable method in the set.

Conformance of a method against a signature can be checked in isolation of any other methods and signatures in the program. However, in the presence of multi-methods, it is not possible to check individual methods in isolation for completeness and consistency, since interactions among multi-methods can introduce ambiguities where none would exist if the multi-methods were not jointly defined within one program.

To type-check in the presence of Cecil's prototype-based object model, *object representatives* are extracted from the program. Each named template, concrete, and dynamic object is considered a distinct object representative, and each static occurrence of an object constructor expression is considered an object representative. A finite number of representatives are extracted from any given program. Representatives are then used as the potential run-time argument objects when testing whether a signature is applicable to a method and whether a set of methods completely and consistently implement a signature. The object representative for an object constructor expression acts as a proxy for all the objects created at run-time by executing that object constructor expression. Since each object created by a particular object constructor expression inherits the same set of methods and has the same type, only one representative need be checked to ensure type safety of all objects created by the object constructor expression at run-time. Object representatives are analogous to concrete classes in a class-based language and maps in the Self implementation [Chambers *et al.* 89].

Conceptually, for each signature, the type checker enumerates all possible *message representatives* that are covered by the signature, where the arguments to the message representative are object representatives that conform to the signature's argument types. (A much more efficient algorithm to perform this checking is described elsewhere [Chambers & Leavens 94].) For each message representative, the type checker simulates method lookup and checks that the simulated message would locate exactly one most-specific method. If no method is found, the type checker reports a "signature implemented incompletely" error. If multiple mutually ambiguous methods are found, the type checker reports a "signature implemented inconsistently" error. Otherwise, the single

most-specific method has been found for the message representative. In this case, the type checker also verifies that the argument object representatives conform to the declared argument types of the target method and that the declared result type of the method is a subtype of the signature's result type. If all these tests succeed, then all run-time messages matching the message representative are guaranteed to execute successfully.

For example, consider type-checking the implementation of the following signature:

```
signature pair_do(collection, collection, &(int,int):void):void;
```

The type checker would first collect all object representatives that conform to collection and all those that conform to &(int,int):void. For a small system, the collection-conforming object representatives might be the following:

```
representation nil inherits list;
representation cons inherits list;
representation inherits cons;
representation array inherits collection;
```

The list and collection objects are not enumerated because they are abstract. The third representative is extracted from the object constructor expression in the prepend method. A single object representative stands for the closure object.

Once the applicable object representatives are collected, the type checker enumerates all possible combinations of object representatives conforming to the argument types in the signature to construct message representatives. These message representatives are the following:

```
pair_do(nil,nil,closure);
pair_do(nil,cons,closure);
pair_do(nil,representation inherits cons,closure);
pair_do(nil,array,closure);
pair_do(cons,nil,closure);
pair_do(cons,cons,closure);
...
pair_do(array,representation inherits cons,closure);
pair_do(array,array,closure);
```

For each message representative, method lookup is simulated to verify that the message is understood, that the declared argument types are respected, and that the target method returns a subtype of the signature's type.

### 3.6.3 Comparison with Other Type Systems

For singly-dispatched languages, most type systems apply contravariant rules to argument and result types when checking that the overriding method can safely be invoked in place of the overridden method: argument types in the overriding method must be supertypes of the corresponding argument types of the overridden method, while the result type must be a subtype. Cecil's type system does not directly compare one method against another to enforce contravariant redefinition rules, but instead compares one method against an applicable signature to enforce contravariant rules for non-specialized arguments. In Cecil terms, in a singly-dispatched language

a signature is inferred from the superclass's method, and then all subclass methods (i.e., those methods that are applicable to the signature) are checked for conformance to the signature.

Specialized arguments need not obey contravariant restrictions. The type of a specialized argument for one method can be a subtype of the type of the corresponding argument for a more general method. This does not violate type safety because run-time dispatching will guarantee that the method will only be invoked for arguments that inherit from the argument specializer, and the static type checker has verified that all objects that inherit from the specializer also conform to the specialized argument's type. Unspecialized arguments cannot safely be covariantly redefined, because there is no run-time dispatching on such arguments ensuring that the method will only be invoked when the type declaration is correct.

Singly-dispatched languages make the same distinction between specialized and unspecialized arguments implicitly in the way they treat the type of the receiver. For most singly-dispatched languages, the receiver argument is omitted from the signatures being compared, leaving only unspecialized arguments and hence the contravariant redefinition rule. If the receiver type were included as an explicit first argument, it would be given special treatment and allowed to differ covariantly. (In fact, it must, since the receiver's type determines when one method overrides another!) For Cecil, any of the arguments can be specialized or unspecialized, requiring us to make the distinction explicit. If all methods in a Cecil program specialized on their first argument only, Cecil's type checking rules would reduce to those found in a traditional singly-dispatched language.

Few multiply-dispatched languages support static type systems. Two that are most relevant are Polyglot [Agrawal *et al.* 91] and Kea [Mugridge *et al.* 91]. In both of these systems, type checking of method consistency and completeness requires that all "related" methods (all methods in the same generic function in Polyglot and all variants of a function in Kea) be available to the type checker, just as does Cecil. Neither Polyglot nor Kea distinguishes subtyping from inheritance nor interfaces from implementations. Additionally, neither Polyglot nor Kea supports a notion of abstract classes that are not required to be completely implemented but that include some notion of an operation that is expected to be implemented by subclasses; signatures play this role in Cecil.

#### 3.6.4 Type Checking Inherited Methods

Cecil does not require that a method be re-type-checked when inherited by a descendant, even if that descendant is not a subtype. This feat is accomplished by verifying that all descendant objects conform to the declared type of the corresponding formal of the inherited method. If the declared type is the type of the specializer, such as would arise with a type declaration using the @: syntax, then all descendant objects are required to be subtypes of the specializer as well. This may be constraining. For example, consider the following set and bag implementation fragments:

```
template object bag isa unordered_collection;
field elems(@:bag):list;
method add(b@:bag, x:int):void {
    b.elems := cons(b.elems, x); }
method includes(b@:bag, x:int):bool {
    b.elems.includes(x) }
...
```

```
template object set isa unordered_collection inherits bag;
method add(s@:set, x:int):void {
    if_not(includes(s, x), { resend(s, x) }) }
```

Here the type checker would report an error, since set inherits from bag but is not a subtype, violating the conformance requirements for bag's elems, add, and includes methods.<sup>\*</sup> In this case, a new type bag\_like\_object could be created that understood the elems and set\_elems messages and the b formal of the bag add and includes methods should be changed to be of this type:

```
abstract object bag_like_object;
field elems(@:bag_like_object):list;
template object bag isa unordered_collection, bag_like_object;
method add(b@bag:bag_like_object, x:int):void {
    b.elems := cons(b.elems, x); }
method includes(b@bag:bag_like_object, x:int):bool {
    b.elems.includes(x) }
    ...
template object set isa unordered_collection, bag_like_object inherits bag;
method add(s@set:bag_like_object, x:int):void {
    if_not(includes(s, x), { resend(s, x) }) }
```

The programmer could go further and move many of the bag operations into the bag\_like\_object. Eventually, set would simply inherit from bag\_like\_object, not bag. In this situation, all inheritance links would parallel subtyping links, and the two would not need to be distinguished.

If such reorganizations can always be made satisfactorily, with the resulting inheritance and subtyping graphs parallel, then it may not be necessary to separate inheritance from subtyping in the language. However, such an approach may not always be feasible. Creating the intermediate bag\_like\_object is somewhat tedious; the original code was easy to read and dynamically type-safe. Moreover, the implementation of bag might be written independently and not under control of the programmer building set. In these cases, simply reusing the implementation of bag for set is convenient. Unfortunately, Cecil's type rules currently seem to prevent the simple solution. One alternative would simply be to re-type-check a method whenever it was inherited by an object that was not also a subtype. The @: notation could be interpreted as indicating that this sort of re-type-checking was to be done. Re-type-checking would require access to at least part of the inherited method's source code, however. Another alternative would be to relax the conformance constraint for any object that inherited an overriding method. In this example, the bag add method would not need to be rewritten, since the set add method "shadows" it for the only descendant object that is not also a subtype; the includes method would still need to be rewritten. Also, the resend in the set add method would become type-incorrect, since it is passing an argument of type set to a method expecting an argument of type bag. This alternative is close to the idea of encapsulating the use of inheritance from clients, as with private inheritance in C++.

<sup>\*</sup> Sets are not subtypes of bags since sets do not support the behavioral specification of bags. A client could detect the difference between a set and a bag by adding the same element twice to an unordered collection and testing how much the size of the collection changed.

We consider the separation of subtyping from inheritance, when coupled with the desire to avoid retypechecking methods when inherited, to be an important area for future work.

# 3.7 Type Checking Expressions, Statements, and Declarations

Type checking an expression or statement determines whether it is type-correct, and if type-correct also determines the type of its result. Type checking a declaration simply checks for type correctness. All constructs are type-checked in a typing context containing the following information:

- a binding for each variable or object name in scope to either:
  - the variable's declared type and an indication of whether the variable binding is assignable or constant, or
  - to an object with a role annotation and a set of conformed-to types.
- the set of inheritance relations currently in scope;
- a binding for each type name in scope to the corresponding type;
- the set of subtyping relations currently in scope;
- the set of signatures currently in scope (for type checking messages);
- the set of method declarations currently in scope (for type checking resends).

The type checking rules for expressions are as follows:

- A literal constant is always type-correct. The type of the result of a literal constant is the corresponding predefined type.
- A reference *name* is type-correct iff *name* is defined in the typing context (i.e., if there exists a declaration of that name earlier in the same scope or in a lexically-enclosing scope) as either a variable or an object. If a variable, then the reference is type-correct, with the type of the result being the associated type of the variable in the typing context. If an object, then the reference is type-correct iff the object is a concrete or dynamic object, with the type of the result being the type of the named object.
- An object constructor expression of the general form

is type-correct iff:

- each *parent*<sub>i</sub> name is bound to a non-abstract non-void object in the typing context;
- each *supertype<sub>i</sub>* notates a type other than none in the current typing context;
- each *parent-and-supertype<sub>j</sub>* name is bound to a non-abstract non-void object in the typing context;
- if @*obj<sub>i</sub>* is present, then *obj<sub>i</sub>* names an ancestor of the newly created object (if absent, it is considered to be the same as the newly created object);
- each *field*<sub>i</sub> names a field  $F_i$  specialized on or inherited unambiguously by  $obj_i$ , ignoring any overriding methods, and  $F_i$  is not shared;

- each  $expr_i$  is type-correct, returning an object of static type  $T_i$ , and  $T_i$  is a subtype of the type of the contents of the field  $F_i$ ;
- no field  $F_i$  is initialized more than once;
- role-annotation is neither abstract nor template; and
- if *role-annotation* is concrete, then there do not exist any fields specialized on or inherited by the newly created object that do not have a default initial value and are not initialized as part of the object creation expression.

The representation keyword may be used in place of the object keyword without effect. The type of the result of an object constructor expression is a new anonymous type that is a subtype of each of the *supertype*<sub>i</sub> types and each of the types of the *parent-and-supertype*<sub>j</sub> objects.

• A closure constructor expression of the general form

 $\& (x_1: type_1, \dots, x_N: type_N): type_R \{ body \}$ 

is type-correct iff:

- the  $x_i$ , where provided, are distinct;
- each of the *type<sub>i</sub>*, if provided, notates a non-void type in the current typing context;
- *type<sub>R</sub>*, if provided, notates a type in the current typing context;
- *body* is type-correct, checked in a typing context constructed by extending the current typing context with constant variable bindings for each of the  $x_i$  to the corresponding type  $type_i$ ; and
- the type of the result of *body* is a subtype of  $type_R$ , if provided; if  $:type_R$  is omitted, then  $type_R$  is inferred to be the type of the result of *body*.

The type of the result of a closure constructor expression of the above form is

&  $(type_1, ..., type_N)$ :  $type_R$ .

- A vector constructor expression of the general form  $[expr_1, ..., expr_N]$  type-correct iff each of the  $expr_i$  is type-correct, with static type  $T_i$  which is not void. The type of the result of a vector constructor expression is the predefined parameterized type i\_vector instantiated with the least upper bound of the  $T_i$ . (See section 4 for information on parameterized types.)
- A message expression of the general form  $name(expr_1, ..., expr_N)$  is type-correct iff:
  - each of the  $expr_i$  is type-correct, with static type  $T_i$  which is not void;<sup>\*</sup> and
  - the set  $S = \{S_1, ..., S_M\}$  of applicable signatures is non-empty, where S is the set of signatures in the current typing context of the form  $S_i = \text{signature } name(t_{i1}, ..., t_{iN}) : t_{iR}$  where each  $T_i$  is a subtype of  $t_i$ .

The type of the result of a message is the greatest lower bound of each of the result types  $t_{iR}$  of the applicable signatures. Verifying correctness of the implementation of signatures is described in subsection 3.6.2.

• A resend expression of the general form

 $resend(..., x_i@parent_i, ..., expr_j, ...)$ 

is type-correct iff:

<sup>\*</sup> The check that the argument type is not void is not strictly necessary, since no signature will have an argument type that is a supertype of void.

- each of the arguments  $x_i$  or  $expr_i$  is type-correct, with static type  $T_i$  which is not void;
- the resend is nested textually in the body of a method *M*;
- *M* takes the same number of arguments, *N*, as does the resend;
- for each specialized formal parameter  $formal_i$  of M, specialized on  $object_i$ , the  $i^{th}$  argument to the resend is  $formal_i$ , possibly suffixed with @parent\_i, and  $formal_i$  is not shadowed with a local variable of the same name;
- for each unspecialized formal parameter *formal*<sub>j</sub> of *M*, the *j*<sup>th</sup> argument to the resend is not be suffixed with @*parent*<sub>j</sub>;
- for each resend argument of the form *formal<sub>i</sub>@parent<sub>i</sub>*, *parent<sub>i</sub>* is a proper ancestor of *object<sub>i</sub>*, the specializer of *formal<sub>i</sub>*, other than void; and
- when method lookup is simulated with a message name the same as M and with N arguments, where argument i is either any (if *formal*<sub>i</sub> of M is unspecialized), *parent*<sub>i</sub> (if the argument of the resend is directed using the @*parent*<sub>i</sub> suffix notation), or *object*<sub>i</sub>, the specializer of *formal*<sub>i</sub> (otherwise), and where the resending method M is removed from the set of applicable methods in the current typing context, exactly one most-specific target method R is located, and the argument type declarations of this target method  $S_i$  are supertypes of the corresponding  $T_i$ .

The type of the result of a resend expression is the declared result type of the target method *R*.

• A parenthetical expression of the form ( *body* ) is type-correct iff *body* is type-correct. The type of the result of a parenthetical expression is the type of the result of *body*.

The following rules define type-correctness of statements:

- An assignment statement of the form *name* := *expr* is type-correct iff:
  - *expr* is type-correct, with static type *T<sub>expr</sub>*;
  - *name* is bound to an assignable variable of type  $T_{name}$  in the current typing context; and
  - $T_{expr}$  is a subtype of  $T_{name}$ .

The type of the result of an assignment statement is void.

- A declaration block is type-correct iff its declarations are type-correct, when checked in a typing context where all names in the declaration block are available throughout the declaration block. The type of the result of a declaration block is void.
- An expression statement is type-correct iff the expression is type-correct, with static type *T*. The type of the result of the expression statement is *T*.
- A non-local return statement, of the form ^ *expr*, is type-correct iff:
  - *expr* is type-correct, with static type *T*;
  - the non-local return statement is nested textually inside the body of a method *M*; and
  - *T* is a subtype of the declared result type of *M*.

The type of the (local) result of a non-local return is none.

The body of a method, closure, or parenthetical expression is type-correct iff its statements are type-correct. The type of the result of a body is the type of its last statement, if present, or void, otherwise.

The following rules define type-correctness of declarations:

- A variable declaration of the form **let** *var name*:*type* := *expr*, where *var* is either var or empty, is type-correct iff:
  - *name* is not otherwise defined in the same scope;
  - *type* notates a type in the current typing context; and
  - *expr* is type-correct in a typing context where *name* and all variables defined later in the same declaration block are unbound, resulting in static type *T*, and *T* is a subtype of *type*.

The typing context is extended to include a variable binding for *name* to the type *type* that is assignable if *var* is var and constant otherwise.

• A type declaration of the form

type name subtypes  $supertype_1, ..., supertype_N$ 

is type-correct iff each of the  $supertype_i$  notates a type other than none in the current typing context and no cycles are introduced into the subtyping graph as a result of the declaration. As a result of the declaration, the typing context is extended to include a type binding from *name* to a new type that is a subtype of each of the  $supertype_i$  types.

• A representation declaration of the form

```
role-annotation kind name inherits parent_1, ..., parent_K

subtypes supertype_1, ..., supertype_L

isa parent-and-supertype_1, ..., parent-and-supertype_M

{ field_1@obj_1 := expr_1, ..., field_N@obj_N := expr_N }
```

is type-correct under the same conditions as the analogous object constructor expression, with the following changes:

- abstract objects may be named in inherits and isa clauses;
- the abstract and template role annotations are allowed; and
- no cycles are allowed to be introduced into the inheritance and subtyping graphs.

The typing context is extended to include an object binding from *name* to a new object with role *role-annotation* that inherits from the *parent*<sub>i</sub> objects and the *parent-and-supertype*<sub>j</sub> objects. If *kind* is the representation keyword, then the new object conforms to the *supertype*<sub>k</sub> types. Otherwise, *kind* is the keyword object, and the typing context is also extended with a type binding from *name* to a new type that is a subtype of each of the *supertype*<sub>i</sub> types, and the new object conforms to the new type.

• A type extension declaration of the form

```
extend type name subtypes supertype_1, ..., supertype_N
```

is type-correct iff:

- *name* is bound in the typing context to a type other than void, any, none, and dynamic; and
- the same constraints on the subtypes clause as with the type declaration are satisfied.

As a result of the declaration, the typing context is extended to reflect that the type *name* is a subtype of each of the *supertype*<sub>i</sub> types.

• A representation extension declaration of the form

```
extend kind name inherits parent<sub>1</sub>, ..., parent<sub>K</sub>

subtypes supertype<sub>1</sub>, ..., supertype<sub>L</sub>

isa parent-and-supertype<sub>1</sub>, ..., parent-and-supertype<sub>M</sub>

\{ field_1@obj_1 := expr_1, ..., field_N@obj_N := expr_N \}
```

is type-correct iff:

- *name* is bound in the typing context to an object other than void and any;
- if *kind* is object or omitted, then *name* also is bound in the typing context to a type other than void, any, none, and dynamic;
- the same constraints on the inherits, subtypes, isa, and field initialization clauses as with the object representation declaration are satisfied; and
- none of the *field*<sub>i</sub>@obj<sub>i</sub> initialize fields already specialized on or inherited by the object before the extension.

As a result of the declaration, the typing context is extended to reflect that the object *name* inherits from the *parent<sub>i</sub>* objects and the *parent-and-supertype<sub>j</sub>* objects. If *kind* is the representation keyword, then the typing context is extended to reflect that the object conforms to the *supertype<sub>k</sub>* types. Otherwise, *kind* is the keyword object, and the typing context is extended to reflect that the *name* type is a subtype of each of the *supertype<sub>i</sub>* types and that the *name* object conforms to the *name* type.

• A signature declaration of the form

```
signature name(x_1:type_1, ..., x_N:type_N):type_R
```

is type-correct iff:

- the *x<sub>i</sub>*, when provided, are distinct;
- each of the  $type_i$  notates a type other than void in the typing context; and
- $type_R$  notates a type in the typing context.

The typing context is extended to include the corresponding signature.

• A field signature declaration of the form

```
var field signature name(x:type):type_R
```

is type-correct iff:

- *type* notates a type other than void in the typing context; and
- $type_R$  notates a type other than void in the typing context.

The typing context is extended to include the signature

**signature**  $name(type):type_R$ 

and, if var is var, the signature

```
signature set_name(type,type<sub>R</sub>):void
```

• A method implementation declaration of the general form

```
method kind name(x_1 @ obj_1 : type_1, ..., x_N @ obj_N : type_N) : type_R \{ body \}
```

is type-correct iff:

- the *x<sub>i</sub>*, when provided, are distinct;
- each of the *type<sub>i</sub>* notates a type other than void in the typing context;
- if @*obj<sub>i</sub>* is present, then *obj<sub>i</sub>* conforms to *type<sub>i</sub>*;
- $type_R$  notates a type in the typing context;
- *body* is type-correct when checked in a typing context constructed by extending the current typing context with constant variable bindings for each of the  $x_i$  to the corresponding type  $type_i$ ; and
- the type of the result of *body* is a subtype of  $type_R$ .

The typing context is extended to include the declared method implementation. If *kind* is not implementation, then the typing context is also extended to include the signature

```
signature name(type_1, ..., type_N):type_R
```

• A field implementation declaration of the general form

```
shared var field kind name(x@obj:type):type_R := expr;
```

is type-correct iff:

- *type* notates a type other than void in the typing context;
- if @obj is present, then obj conforms to type;
- *type*<sub>R</sub> notates a type other than void in the typing context;
- if := expr is provided, then *expr* is type-correct, with static type *T*, and *T* is a subtype of  $type_R$ ; and
- if *shared* is shared, then := *expr* is provided.

The typing context is extended to include the declared field get accessor method implementation, plus the set accessor method implementation if *var* is *var*, plus the get (and possibly set) signature(s) if *kind* is not implementation.

# 3.8 Type Checking Subtyping Declarations

When the programmer declares that an object conforms to a type (via a subtypes or isa clause), the type system trusts this declaration and uses it when checking conformance and subtyping. However, it is possible that the programmer's claim is wrong, and that the object in fact does not faithfully implement the interface of the types to which it supposedly conforms. In this case, the signature implementation checking, described in section 3.6.2, is sufficient to detect and report the error, so no additional checking is required. When enumerating and checking message representatives matching a signature defined on the supertype, the object in question, if not abstract, will be enumerated, and the error will be detected because some signature will not be implemented properly for that object. If the object is abstract, no type error will be reported. This will not affect running programs since the abstract object cannot be used in a message. Also, since abstract objects are allowed to be incomplete, it is unclear whether a type error really exists.

# 3.9 Type Checking Predicate Objects

Predicate objects are intended to represent alternative ways of implementing an object's interface. Accordingly, it should be possible to type-check programs using predicate objects, under the assumption that the particular state of the object does not affect its external interface. In particular, to guarantee type safety in the presence of predicate objects, the type checker must verify that for each message declared in the interface of some object *O*:

- at all times there is an implementation of the message inherited by the object O; and
- at no time are there several mutually ambiguous implementations of the message inherited by the object *O*.

These two tests correspond to extending the tests of completeness and consistency of method implementations to cope with the presence of predicate objects.

The set of methods inherited by the object *O* from normal objects is fixed at program-definition time and can be type-checked in the standard way. Methods inherited from predicate objects pose more of a problem. If two predicate objects might be inherited simultaneously by an object, either one predicate object must be known to override the other or they must have disjoint method names. For example, in the bounded buffer implementation described in section 2.4, since an object can inherit from both the non\_empty\_buffer and the non\_full\_buffer predicate objects, the two predicate objects should not implement methods with the same name. Similarly, if the only implementations of some message are in some set of predicate objects, then one of the predicate objects must always be inherited for the message to be guaranteed to be understood. In other words, the checker needs to know when one predicate object *implies* another, when two predicate objects are *mutually exclusive*, and when a group of predicate objects is *exhaustive*. Once these relationships among predicate objects are determined, the rest of type-checking becomes straightforward.

Ideally, the system would be able to determine all these relationships automatically by examining the predicate expressions attached to the various predicate objects. However, predicate expressions in Cecil can run arbitrary user-defined code, and consequently the system would have a hard time automatically inferring implication, mutual exclusion, and exhaustiveness. Consequently, we rely on explicit user declarations to determine the relationships among predicate objects; the system can verify dynamically that these declarations are correct.

A declaration already exists to describe when one predicate object implies another: the isa declaration. If one predicate object explicitly inherits from another, then the first object's predicate is assumed to imply the second object's predicate. Any methods in the child predicate object override those in the ancestor, resolving any ambiguities between them.

Mutual exclusion and exhaustiveness are specified using declarations of the following form:

```
disjoint_decl ::= "disjoint" named_objects ";"
cover_decl ::= "cover" named_object "by" named_objects ";"
divide_decl ::= "divide" named_object "into" named_objects ";"
named_objects ::= named_object { "," named_object }
```

The disjoint declaration

```
disjoint object<sub>1</sub>, ..., object<sub>n</sub>;
```

implies to the static type checker that the predicate objects named by each of the  $object_i$  will never be inherited simultaneously, i.e., that at most one of their predicate expressions will evaluate to true at any given time. Mutual exclusion of two predicate objects implies that the type checker should not be concerned if both predicate objects define methods with the same name, since they cannot both be inherited by an object. To illustrate, the following declarations extend the earlier bounded buffer example with mutual exclusion information:

disjoint empty\_buffer, non\_empty\_buffer; disjoint full\_buffer, non\_full\_buffer;

The system can infer that empty\_buffer and full\_buffer are mutually exclusive with partially\_full\_buffer. Note that empty\_buffer and full\_buffer are not necessarily mutually exclusive.

The cover declaration

**cover** object **by** object<sub>1</sub>, ..., object<sub>n</sub>;

implies that whenever an object O descends from *object*, the object O will also descend from at least one of the *object<sub>i</sub>* predicate objects; each of the *object<sub>i</sub>* are expected to descend from *object* already. Exhaustiveness implies that if all of the *object<sub>i</sub>* implement some message, then any object inheriting from *object* will understand the message. For example, the following coverage declaration extends the bounded buffer predicate objects:

```
cover buffer by empty_buffer, partially_full_buffer, full_buffer;
```

Often a group of predicate objects divide an abstraction into a set of exhaustive, mutually-exclusive subcases. The divide syntactic sugar makes specifying such situations easier. A declaration of the form

```
divide object into object<sub>1</sub>, ..., object<sub>n</sub>;
```

is syntactic sugar for the following two declarations:

```
disjoint object<sub>1</sub>, ..., object<sub>n</sub>;
cover object by object<sub>1</sub>, ..., object<sub>n</sub>;
```

Since fields are accessed solely through accessor methods, checking accesses to fields in predicate objects reduces to checking legality of messages in the presence of predicate objects, as described above. To ensure that fields are always initialized before being accessed, the type checker simply checks that the values of all fields potentially inherited by an object are initialized either at the declaration of the field or at the creation of the object.

# 3.10 Mixed Statically- and Dynamically-Typed Code

One of Cecil's major design goals is to support both exploratory programming and production programming and in particular to support the gradual evolution from programs written in an exploratory style to programs written in a production programming style. Both styles benefit from object-oriented programming, a pure object model, user-defined control structures using closures, and a flexible, interactive development environment. The primary distinction between the two programming styles relates to how much effort programmers want to put into polishing their systems. Programmers in the exploratory style want the system to allow them to experiment with partially-implemented and partially-conceived systems, with a minimum of work to construct and subsequently revamp systems; rapid feedback on incomplete and potentially inconsistent designs is crucial. The production programmer, on the other hand, is concerned with building reliable, high-quality systems, and wants as much help from the system as possible in checking and polishing systems.

To partially support these two programming styles within the same language, type declarations and type checking are optional. Type declarations may be omitted for any argument, result, or local variable. Programs without explicit type declarations are smaller and less redundant, maximizing the exploratory programmer's ability to rapidly construct and modify programs. Later, as a program (or part of a program) matures, the programmer may add type declarations incrementally to evolve the system into a more polished and reliable production form.

Omitted type declarations are treated as dynamic; dynamic may also be specified explicitly as the type of some argument, result, or variable. An expression of type dynamic may legally be passed as an argument, returned as a result, or assigned to a variable of any type. Similarly, an expression of any type may be assigned to, passed to, or returned from a variable, argument, or result, respectively, of type dynamic. This approach to integrating dynamically-typed code with statically-typed code has the effect of checking type safety statically wherever two statically-typed expressions interact (assuming that at run-time the objects resulting from evaluating the staticallytyped expressions actually conform to the given types), and deferring to run-time checking at message sends whenever a dynamically-typed expression is used.

A consequence of this semantics for the dynamic type is that the static type safety of staticallytyped expressions can be broken by passing an incorrect dynamically-typed value to a staticallytyped piece of the program. Dynamic type checking will catch errors eventually, but run-time type errors can occur inside statically-typed code even if the code passes the type checker. An alternative approach would check types dynamically at the "interface" between dynamically- and statically-typed code: whenever a dynamically-typed value is assigned to (or passed to, or returned as) a statically-typed variable or result, the system could perform a run-time type check of the dynamically-typed value as part of the assignment. This approach would then ensure the integrity of statically-typed code: no run-time type errors can occur within statically-typed code labeled type-correct by the typechecker, even when mixed with buggy dynamically-typed code. Unfortunately, this approach has some difficulties. One problem is that objects defined in exploratory mode should not be required to include explicit subtyping declarations; such declarations could hinder the free-flowing nature of exploratory programming. However, if such an object were passed to statically-typed code, the run-time type check at the interface would fail, since the object had not been declared to be a subtype of the expected static type. We have chosen for the moment to skip the run-time check at the interface to statically-typed code in order to support use of statically-typed code from exploratory code, relying on dynamic checking at each message send to ensure that the dynamically-typed object supports all required operations. An alternative might be to perform some form of inference of the subtyping relationships of dynamically-typed objects, like that incorporated in object-oriented systems based on implicit structural subtyping, and use these inferred subtyping relationships for the run-time type check.

Cecil supports the view that static type checking is a useful tool for programmers willing to add extra annotations to their programs, but that all static efficiently-decidable checking techniques are ultimately limited in power, and programmers should not be constrained by the inherent limitations of static type checking. The Cecil type system has been designed to be flexible and expressive (in particular by supporting multi-methods, separating the subtype and code inheritance graphs, and supporting explicit and implicit parameterization) so that many reasonable programs will successfully type-check statically, but we recognize that there may still be reasonable programs that either will be awkward to write in a statically-checkable way or will be difficult if not impossible to statically type-check in any form. Accordingly, error reports do not prevent the user from executing the suspect code; users are free to ignore any type checking errors reported by the system, relying instead of dynamic type checks. Static type checking is a useful tool, not a complete solution.
# 4 Parameterization and Parametric Polymorphism

Practical statically-typed languages need some mechanism for parameterizing objects and methods. Without some mechanism for parameterization or parametric polymorphism, programmers must resort to multiple similar implementations for abstractions such as list and array that differ only in the declared type of the collection's elements. Similarly, control structures such as if and map can be reused for a variety of argument types. Accordingly, Cecil supports the definition of parameterized object representations, method and field implementations, types, and signatures.

The next section describes Cecil's mechanism for explicit parameterization. Section 4.2 introduces Cecil's mechanism for implicit parameterization, and sections 4.3 and 4.4 describe aspects of this feature in more depth. Section 4.5 explains the interaction between parameterized objects and method lookup, section 4.6 explains the interaction between parameterized constructs and the object and method syntactic sugars. Section 4.7 discusses Cecil's version of F-bounded polymorphism.

Note: the mechanisms for parameterization in Cecil are being redesigned, using a more explicit and expressive constraint-based core. Programs using the mechanisms described in this section continue to be supported by the new type system. Part of the work on the new parameterization mechanism includes a more precise description of the type system and its checking rules.

## 4.1 Explicit Parameterization

Cecil allows object, type, method, field, and signature declarations to be parameterized by a sequence of types, as the following examples illustrate:

```
abstract object collection[T];
abstract object list[T] isa collection[T];
signature do[T](list[T], &(T):void):void;
concrete representation nil[T] isa list[T];
field head[T](@:cons[T]):T;
field tail[T](@:cons[T]):list[T] := nil[T];
method prepend[T](h:T, t:list[T]):list[T] {
    concrete object isa cons[T] { head := h, tail := t } }
abstract object table[Key,Value] isa collection[Value];
template object array[T] isa table[int,T];
method new_array[T](size:int, initial_value:T):array[T] {
    concrete object isa array[T] {
    size := size, initial_value := initial_value } }
```

## 4.1.1 Parameterized Declarations and Formal Type Parameters

The syntax of type, object, predicate object, method, field, and signature declarations is extended to allow explicit parameterization as follows:

The number of formal type parameters is considered part of the "name" of the declared entity. For example, multiple objects can be declared with the same name, as long as they are declared with different numbers of formal type parameters.<sup>\*</sup>

The formal type parameter of the form `*name* <= *type* is quantified over all types that are subtypes of *type*; the leading back-quote symbol is optional. If the <= *type* upper bound is omitted, then <= any is assumed. Similar facilities appear under the name of bounded quantification [Cardelli & Wegner 85] and constrained genericity [Meyer 86].<sup>†</sup>

Type parameters are scoped over the whole declaration; type parameters must have distinct names. Within its scope, a type parameter may be used in a type declaration or as an instantiating type for some other parameterized type or method; a type parameter cannot be used in a subtypes clause, as this context requires a statically-known type. Cycles are not allowed in the dependency graph of formal type parameters and their upper bound types (e.g., ['A <= B, 'B <= A] is illegal), but no other orderings are required. For example, ['A <= B, 'B <= int] is legal, with the first occurrence of B referring to the instantiating type of the second type parameter.

A parameterized declaration can be typechecked in isolation, independently of any instantiating clients. This is in contrast with languages such as C++ and Modula-3 where typechecking of a parameterized class or module must in general be deferred and repeated for each instantiation. When typechecking the body of a parameterized method or the initialization expression of a parameterized field, all that can be assumed of a variable whose type is declared to some formal type parameter is that the variable is some subtype of the upper bound of the type parameter. For most purposes, this is equivalent to assuming the variable conforms to the upper bound type itself.

#### 4.1.2 Instantiating Parameterized Declarations

A parameterized entity is not a first-class entity that can be manipulated directly, but rather it is an "entity generator:" a function from a tuple of types to an (instantiated) entity. To use a

<sup>\*</sup> This feature does not interact well with mixed dynamic and static typing, since the number of parameters affects the execution behavior of the program, violating the principle that static types do not affect the execution semantics. In the future, the number of parameters may be removed from the "name" of an object or method, so that parameters are confined to the (optional) static type system. Omitted type parameters would default to dynamic, in keeping with the default for omitted type declarations.

<sup>&</sup>lt;sup>†</sup>Lower bounds on type parameters can also be useful, for example to model the case where a more specific closure type is required to have at least as general argument types.

parameterized entity, a client must first instantiate it with actual types for each of its parameters, at which point the instantiated entity can be used as if it were a regular unparameterized entity where the formal type parameters have been replaced with the actual type parameters. The syntax of object references, type references, and messages is extended as follows to allow instantiating parameters to be provided:

| named_object | ::= | name [params]   |
|--------------|-----|---|
| named_type   | ::= | name [params]   |
| message      | ::= | <pre>msg_name [params] "(" [exprs] ")"</pre>                |
| dot_msg      | ::= | <pre>dot_expr "." msg_name [params] ["(" [exprs] ")"]</pre> |
| params       | ::= | "[" types "]"   |

All instantiations of a parameterized entity with the same actual parameter types name the same instantiated entity; e.g. two distinct static occurrences of array[int] name the same instantiated object. This semantics is a form of structural type equivalence, patterned after CLU and Trellis, and contrasts with some other languages where parameterized entities must be instantiated explicitly and given names before they can be used by client code.

#### 4.1.3 Parameterized Objects and Types

It is not possible to inherit directly from a parameterized object representation, nor to subtype directly from a parameterized type. However, it is possible (and common) to inherit from an instantiation of a parameterized object and to subtype from an instantiation of a parameterized type. A particularly common idiom is for a parameterized object or type to inherit or subtype from another parameterized object or type instantiated with (some function of) the first parameterized object or type's type parameters. For example:

```
abstract object collection[T];
abstract object table[Key,Value] isa collection[Value];
template object array[T] isa table[int,T];
type printable_array[T <= printable] subtypes array[T], printable;</pre>
```

#### 4.1.4 Method Lookup

Method lookup is extended to include the number of explicit parameters of candidate methods as the method selection process. Α message part of of the form name [type<sub>1</sub>,..., type<sub>M</sub>] (expr<sub>1</sub>,..., expr<sub>N</sub>), with M and N zero or greater, will only match methods named *name* with M explicit formal type parameters and N formal arguments. Method lookup does not depend on the constraints placed on legal instantiating types of explicit formal type parameters. For example,

```
method foo[T <= integer]():void { ... }</pre>
```

does not override

```
method foo[T <= number]():void { ... }</pre>
```

In fact, these two methods could not legally be defined in the same system, since they have the same name, same number of explicit type parameters, same number of arguments, and same argument specializers.

# 4.1.5 Type Checking Instantiations

To type-check a message with explicit type parameters, signatures with matching names, number of parameters, and number of arguments are located. For each signature, the actual type parameters are bound to the formal type parameters of the signature, and then the formal argument types of the signature are compared to the actual argument types at the call site. A signature is applicable to the call site if the actual types are subtypes of the corresponding formal argument types, as described in section 3.6.1. Once a signature is deemed applicable, then the actual type parameters are compared against the upper bounds of the formal type parameters; if these actual parameters are not subtypes of the corresponding upper bounds, then an "illegal instantiation" error is reported.

To type-check the implementation of a parameterized signature, all methods with the same name, number of type parameters, and number of arguments as the signature are collected. The same rules on conformance, completeness, and consistency as given in section 3.6.2 are verified, with the modification that, when checking the formal argument types of the method against those in the signature, occurrences of the method's formal type parameters are substituted with the signature's corresponding formal type parameters. In addition, the upper bound of a formal type parameter of the signature must be a subtype of the corresponding upper bound of the method; this is a kind of contravariance requirement for type parameter constraints.

All instantiations of parameterized objects and types are checked that the instantiating types are subtypes of the upper bounds of the corresponding formal type parameters.

It can be tricky to verify that an instantiating type parameter is a subtype of the upper bound of the corresponding formal type parameter, if one formal type parameter is used as the upper bound of another formal type parameter. In this case, the instantiator must be able to show statically that the bounded actual type parameter is indeed a subtype of the bounding actual type parameter. If these actual types are themselves formal type parameters in the caller, then such a relationship may be difficult to show. For example, consider the following four methods:

```
method base[T1, T2 <= T1](x:T1, y:T2):void { ... }
method client1() { base[num,int](4.5, 3); }
method middle[S1, S2 <= num](a:S1, b:S2):void { base[S1,S2](a, b); }
method client2() { middle[int,num](3, 4.5); }</pre>
```

The base method requires that its second type parameter always be a subtype of its first type parameter. The clientl method satisfies this requirement, assuming that int is a subtype of num. However, the middle method does not meet this requirement: even though the upper bound of S2 (num) is known to be a subtype of the upper bound of S1 (any), a particular instantiation of middle may not preserve such a relationship. The method client2 illustrates such an instantiation. Consequently, the static type checker will flag the invocation of base in middle as type-unsafe.

# 4.2 Implicit Parameterization

While explicit parameterization and instantiation is sufficient for programming parameterized objects and types, it is frequently inconvenient. For example, consider the implementation of an explicitly-parameterized pair\_do method:

Singly-dispatched languages do not face this verbosity, because methods are defined within a class and within the scope of the parameterized class's type parameters. Additionally, invocations of methods on a parameterized object, such as the head message above, would not need to specify an instantiating parameter because it can be derived from the instantiating parameter of the distinguished receiver object. The following pseudo-code is representative of the kind of support found in singly-dispatched languages:

```
class cons[T] {
  field head:T;
  field tail:list[T];
  method length():int { 1 + tail.length() }
  ...
}
```

In this code, the formal type parameter T is introduced in the cons class declaration and is scoped over all fields and methods defined on the class. Consequently, none of these fields and methods need be explicitly parameterized, and the recursive length call need not pass any explicit type parameters, since it is implied by the type of the receiver expression.

To regain much of the conciseness of parameterization in singly-dispatched languages while still supporting multi-methods, object extensions, and other of Cecil's more flexible constructs, Cecil allows *implicit type parameter bindings* to be present in the type declarations of formal arguments of a method or field. These implicit type parameters are instantiated automatically with the corresponding type of the actual argument in each call site. A binding occurrence of such an implicit type variable is indicated by prefixing the type name with a back-quote character; other occurrences of the type variable simply name the bound type.

The operations on parameterized cons objects can be rewritten with implicit type parameters as follows:

Like explicit formal type parameters, an implicit formal type parameter may be bounded from above by some type using the <= *type* notation, and an implicit formal parameter is quantified over all types that are subtypes of its upper bound (where any is used as the default upper bound). Like explicit type parameters, implicit type parameters are scoped over the entire declaration. An

implicit type parameter must have a name that is distinct from any other implicit or explicit type parameters. Like explicit type parameters, implicit type parameters may be used in the type declarations of earlier formal arguments, as in the prepend method above, as long as no cyclic dependencies result. Implicit type parameters are akin to polymorphic type variables in languages like ML [Milner *et al.* 90]. Note that unlike 'a type variables in ML, the back-quote in Cecil's 'T is not part of the type name, but rather identifies that the use of the type T is a binding occurrence as opposed to a simple use of a previously-defined type.

Implicit type parameters are useful not only for parameterized types but also for performing simple calculations on argument types to compute appropriate result types. For example, the following method describes its result type in terms of its argument types: \*

```
method min(x1:`T1 <= comparable, x2:`T2 <= comparable):T1|T2 {
    if(x1 < x2, { x1 }, { x2 }) }</pre>
```

User-defined control structures often compute the types of their results from the types of their arguments:

```
signature if(condition:bool, true_case:&():`T1, false_case:&():`T2):T1|T2;
method if(condition@:true, true_case:&():`T1, false_case:&():void):T1 {
    eval(true_case) }
method if(condition@:false, true_case:&():void, false_case:&():`T2):T2 {
    eval(false_case) }
```

As illustrated by the above examples, least-upper-bound types over implicit type parameters are relatively common when expressing the type of a method's result in terms of its arguments' types.

Implicit type parameter bindings can only appear in the declared type of a formal parameter or variable, as the upper bound type of another type parameter, or as the instantiating parameter of a parameterized object or type being augmented in an extension declaration. A type that can contain an implicit type parameter binding is called a type pattern. The syntax of several constructs is updated to reflect where implicit type parameter bindings are legal:

| type_pattern   | ::= | <pre>binding_type named_type_p closure_type_p lub_type glb_type paren_type</pre>                  |
|----------------|-----|---|
| binding_type   | ::= | "`" name ["<=" type_pattern]  |
| named_type_p   | ::= | name [param_patterns]   |
| closure_type_p | ::= | "&" "(" [arg_type_ps] ")" [type_decl_p]   |
| signature_decl | ::= | "signature" method_name<br>"(" [ <b>arg_type_ps</b> ] ")" [type_decl] ";"                         |
| field_sig_decl | ::= | ["var"] "field" "signature" msg_name [formal_params]<br>"(" <b>arg_type_p</b> ")" [type_decl] ";" |
| arg_type_ps    | ::= | arg_type_p {  |
| arg_type_p     | ::= | [name ":"] type_pattern   |

<sup>\*</sup> Section 4.7 will revise this version of min to use a more sophisticated comparable type.

```
specializer
               ::= location [type_decl_p]
                                              specialized formal
                   [type_decl_p]
                                              unspecialized formal
                    "@" ":" named object p
                                              sugar for @named obj p : named obj p
closure_formal ::= [name] [type_decl_p]
                                              formal names are optional, if never referenced
type_ext_decl ::= "extend" "type" named_type_p {type_relation} ";"
               ::= "extend" extend_kind named_object_p
obj_ext_decl
                        {relation} [field_inits] ";"
type_relation ::= "subtypes" type_patterns
               ::= named_object_p { ", " named_object_p }
parents
named_object_p ::= name [param_patterns]
type_decl_p
               ::= ":" type_pattern
formal_param
               ::= ["`'] name [ "<=" type_pattern ]
param patterns ::= "[" type patterns "]"
type patterns ::= type pattern { "," type pattern }
```

# 4.3 Matching Against Type Patterns

If the type of a method's formal contains a binding occurrence of an implicit type parameter, i.e., a type of the form T, then the system is responsible for automatically inferring the right instantiating actual type for each call of the method. Once bound, implicit type parameters are just like explicit type parameters. Matching has two parts: message sends are compared against signatures that may contain implicit type parameters, and method implementations are compared against signatures, either of which may have implicit type parameters. The first case is easier, since it requires matching a regular type against a type pattern, while the second case requires the ability to compare two patterns. Below we describe somewhat informally the process of matching a type against a type pattern; precise descriptions of both processes remain future work.

#### 4.3.1 Method Formal Type Patterns

In general, formal argument type patterns are of the form

```
T \le type[param_1, ..., param_N]
```

where *N* may be zero. If the  $T \leq Prefix$  is omitted, a fresh type variable is supplied to represent the type of the argument. Every formal parameter can thus be considered to have an associated implicit type variable bound to the dynamic type of the corresponding actual. If the  $\leq type[...]$  upper bound is omitted, it defaults to any.

The type variable for the formal is bound to the dynamic type of the actual, not the static type of the actual. Since during typechecking of the caller, only the static type of the actual is known, this situation can be modeled by treating the type of an actual as some fresh type variable that is known only to be a subtype of the static type computed for the argument. Normally, this distinction between the static and dynamic type is not important, but it can be in some situations. In particular, if the corresponding type variable is used an as upper bound of some other type variable, as in section 4.1.5, there can be a great difference between the static and dynamic type. This point is discussed more in section 4.3.4.

## 4.3.2 Upper Bound Type Patterns

If the upper bound type of a formal or (explicit or implicit) type parameter is parameterized, each parameter type may itself contain an implicit type binding; upper bound types are themselves type patterns. In general, each  $param_i$  has the same form as a formal type:

 $T_i \le type_i[param_1, \dots, param_N]$ 

Like a formal type, if the  $\langle = type[...]$  upper bound is omitted, it defaults to any. Also like a formal type, the leading ` $T \langle = prefix$  can be omitted. However, there is an important semantic distinction between a parameter of the form ` $T \langle = type[...]$  and a parameter of the form type[...]. If the ` $T \langle = prefix$  is omitted, then argument types matching the type pattern must have parameters that match type[...] exactly; for parameters of the form ` $T \langle = type[...]$ , matching types need only be a subtype of type[...]. To illustrate the distinction, consider the following two methods:

```
method detabify_all_1(s:array[string]):void { ... }
method detabify_all_2(s:array[`T <= string]):void { ... }</pre>
```

The first method takes an argument s that is a subtype of array of string, i.e., any object that satisfies the interface of array of string. In particular, if array supports a store operation, then any value of type string must be able to be stored into the array s.

The second method places different constraints on its argument. It takes an array of things of some type T, where T is a subtype of string. So a value of type array[m\_string], where m\_string is some subtype of string, would be a legal argument to the second method. Such an argument would *not* be legal to the first method, however, since mutable arrays of mutable strings is *not* a subtype of mutable arrays of generic strings; a generic string cannot safely be stored into an array of mutable strings. For the second method, any value of type T can be stored safely into the argument array. Deciding the exact form of a parameterized type declaration can be rather subtle, and we need to gather more experience with the language to assess how well programmers are able to pick an appropriate type declaration. Type inference could help suggest the mostgeneral type for a method, given its implementation.

#### 4.3.3 The Matching Algorithm

When a method with implicit type parameters is invoked, the system first binds any explicit type parameters to their corresponding actual type parameters and, for each formal with a declared type with a  $T_i \leq prefix$ , binds the  $T_i$  type parameter to the dynamic type of the corresponding actual argument. Then the system attempts to match each actual explicit type parameter and each actual argument dynamic type D against its corresponding upper bound type  $type[param_1, ..., param_N]$  (where N may be zero). If the upper bound is a type variable bound elsewhere in the method's header, checking this upper bound constraint is deferred until the type variable is bound. Otherwise, the system searches the supertypes of D to locate one of the form  $type[ptype_1, ..., ptype_N]$ , i.e., one with the same "head" type and the same number of parameters, if any, with the additional constraint that if any of the  $param_i$  is a simple type without a  $T \leq prefix$ , then  $ptype_i = param_i$ . After finding these matching types for each upper bound, the system binds type variables: for each parameter  $param_j$  with a  $T_j <= prefix$  binding,  $T_j$  is bound to  $ptype_j$ . Then the system recursively matches each  $ptype_i$  against its upper bound, which may bind

additional type parameters. Finally, any formal parameter whose upper bound was a type variable is checked. If any of the matches fail, then a type error results. This matching process subsumes subtyping checks: if any of the upper bounds are types with no embedded type variable bindings, the matching process reduces to a simple subtyping check.

For example, consider the following code:

```
abstract object printable;
   signature print(@:printable):void;
abstract object number isa printable;
abstract object collection[T];
   signature do(c@:collection[`T], closure:&(T):void):void;
   method print(c@:collection['T <= printable]):void {</pre>
      "[ ".print;
      do(c, &(x:T){ x.print; " ".print; });
      "]".print;
   }
   method expand_tabs(c@:`T <= collection[char]):T {</pre>
      -- return a copy of c, where tab characters have been replaced with spaces
   }
abstract object list[T] isa collection[T];
concrete representation nil[T] isa list[T];
template representation cons[T] isa list[T];
abstract object table[Key,Value] isa collection[Value];
abstract object indexed[T] isa table[int,T];
template object array[T] isa indexed[T];
template object string isa indexed[char];
```

If the message print is sent to an object of dynamic type cons[number], then the print method defined on collection will be found. Then the dynamic type cons[number] will be matched against the pattern collection[`T <= printable] to bind the implicit type parameter T. The supertype graph of cons[number] will be searched for a type of the form collection[something]. This search will locate the type collection[number], binding T to the type number. The system then verifies that the binding for T is a subtype of its upper bound printable.

If, on the other hand, the message expand\_tabs is sent to an object of dynamic type string, the method defined for collection[char] will be found. The dynamic type string will be matched against the static formal argument type `T <= collection[char]. This match will succeed, since string is declared as a subtype of collection[char], and the implicit type parameter T will be bound to string.

It is illegal for a type variable to be bound more than once in a particular scope, e.g., in a method's list of explicit type parameters and in the types of its formals. It is also illegal to use a bound type variable as a parameter of an upper bound type before that type variable has been bound by the

matching process. This implies that uses of a type variable as parameters must occur at greater "depth" than the binding occurrence of that type variable.

This matching process forms the heart of the semantics of implicit type parameters, and it needs to be formalized in a clearer and less algorithmic way.

## 4.3.4 Static vs. Dynamic Matching

At run-time, the dynamic type of the actual argument is used to compute the instantiation of any implicitly-bound type parameters. During static type checking, however, the type checker does not know the dynamic type of its arguments. Fortunately, the static type checker can perform a similar matching process using the static types of the arguments to the call to verify type-correctness of the call and to compute the static type of the result. The static checker uses type variables to stand for the dynamic types of the arguments to the call, and these type variables are statically known to be subtypes of the static type of the arguments. If the matching process succeeds using these static type variables, then the match is guaranteed to succeed at run-time.

Usually, the distinction between the dynamic and the static type is unimportant. For example, with the simple min method defined above, the caller will know that the type of the result is a subtype of the least-upper-bound of the dynamic types of the two arguments. Given the static knowledge that both arguments are of some dynamic type that is a subtype of a particular static type, the caller can infer the static knowledge that the result is some subtype of that static type. Static type information already implies only that the dynamic type of some expression is some subtype of the static type, so calculating static approximations to implicitly-bound type variables is what the type checker has been doing all along.

In two circumstances, however, the distinction between instantiating a type parameter with a dynamic type versus a static type is important. If a implicitly-bound type parameter is used as a normal type for another declaration, i.e., as an upper bound type, then legal actual parameters must be known to be equal to or subtypes of the implicitly bound type variable. For example, if min were rewritten as follows:

```
method min(x1:`T <= comparable, x2:T):T {
    if (x1 < x2, { x1 }, { x2 })}</pre>
```

the second argument would be required to be a subtype of the *dynamic* type of the first argument. This requirement could be quite difficult to guarantee statically and is probably not what the programmer meant. Type parameters are usually used directly as type declarations when they are bound to the instantiating parameter of a parameterized type, as in the following method:

```
method store(a:array[`T], index:int, value:T):void {
    -- store value as the index<sup>th</sup> element of the array a
}
```

Here, T will be bound to the type of the elements of the array, specified when the array was created, and usually the value argument will be known to be a subtype of that type at the call site, perhaps because it had just been extracted from an array of similar type.

The distinction between dynamic types and static types for instantiation also appears when instantiating a parameterized object. For example, one way to write the new\_array method might be the following:

```
method new_array(size:int, initial_value:`T):array[T] {
    concrete object isa array[T] {
        size := size, initial_value := initial_value } }
```

Given an initial value of dynamic type T, an array is returned with the type T as the instantiating value. Because of the fetch and store operations defined on arrays, this array will only be able to contain elements that are subtypes of the *dynamic* type of its initial value. Usually, this would be too restrictive. To correct this problem, the real method to create a new array is explicitly parameterized with the desired type of the elements:

```
method new_array[T](size:int, initial_value:T):array[T] {
    concrete object isa array[T] {
        size := size, initial_value := initial_value } }
```

Instantiations of parameterized objects record their instantiating types as part of their dynamic runtime state. The instantiating types are used to determine the subtyping relation of the object and when matching the parameterized object's type against a type pattern of the form  $type[..., T_i <= type_i, ...].$ 

# 4.3.5 Constraints on Supertype Graphs for Matching

The process for matching a dynamic type against a static type declaration containing implicit type parameter bindings depends on locating a single most-specific binding type. This may not always be possible without additional constraints. For example, in the following declaration:

```
concrete object strange isa collection[int], collection[string];
```

if the strange object is sent the do message, its type will be matched against the type pattern collection[`T]. Both collection[int] and collection[string] will match, but the system needs to locate a single type to bind to the variable T. Binding T to int&string might seem reasonable, but then a type error will result, because strange is not a subtype of collection[int&string] (such a relationship would have to be explicitly declared). To avoid this sort of problem at method invocation time, objects like strange are disallowed.

For an object declaration to be legal, there must be at most one most-specific instantiation for any of its parameterized supertypes. This check is made when type-checking an object declaration or constructor expression.

# 4.3.6 Matching and Bounded Formal Type Parameters

When instantiating a parameterized type with a binding occurrence of an implicit type parameter, any upper bounds specified at the declaration of the parameterized type are inherited automatically by the bound type variable. For example, hash tables can require that their keys must be hashable:

```
template object hash_table[Key <= hashable, Value] isa collection[Value];</pre>
```

Methods defined on hash tables can bind type parameters to the types of the keys and values of the table:

```
method fetch(t@:hash_table[`Key, 'Value], key:Key):Value { ... }
```

Since all hash tables must take hashable keys, when type checking the body of the fetch method, the type checker can assume that the Key type variable is a subtype of hashable.

# 4.4 Implicit Type Parameters in Extension Declarations

An extension declaration can augment either an instance of a parameterized type or a collection of instances using an implicit type parameter. For example, the following declaration extends a single instance of a parameterized type:

extend array[char] subtypes string;

and the following declaration extends a collection of related types:

```
extend collection[`T <= printable] isa printable;</pre>
```

To extend a parameterized type itself, not just some instances, an extension declaration that updates all instances is used:

extend list[`T] subtypes variable\_length\_collection[T];

#### 4.5 Parameterized Objects and Method Lookup

A method can be attached either to a parameterized object itself, to a group of instances of the parameterized object, or to a single instance. The form of the instantiating type pattern determines the scope of the method implementation. For example, the following method is attached to a parameterized object (i.e., to all instances of the parameterized object), since the parameter to the parameterized object is universally quantified:

```
method length(c@:cons['T]):int { ... }
```

To attach a method to a subset of the instances, a bounded implicit type variable is used as the instantiating parameter:

```
method hash(c@:cons[`T <= hashable]):int { ... }</pre>
```

If the instantiating type contains no implicit type parameter bindings, then the method is attached to a particular instance of the parameterized object:

```
method detabify(c@:cons[char]):cons[char] { ... }
```

If multiple method implementations with the same name are defined on the same parameterized object, but with different degrees of quantification:

```
method print(c@:collection[`T]):void { ... }
method print(c@:collection[`T <= printable]):void { ... }
method print(c@:collection[`T <= hashable]):void { ... }
method print(c@:collection[char]):void { ... }</pre>
```

then the issue of which method to invoke arises. One reasonable choice would be to declare such redundant method implementations ambiguous: more than one print method of one argument is defined for collections of characters. An alternative semantics would be to choose the most-specific matching method implementation, where a method is more specific than another if it is associated with a subset of the instances of the other. We have little experience with attaching multiple versions of the same method to different subsets of a parameterized types, so initially we have selected the more-conservative position of allowing only a single version of a method to be provided for any given instance of a parameterized type; the above declarations are illegal.

#### 4.6 Parameterization and Syntactic Sugars

When desugaring a parameterized object declaration, the implied representation and type declarations are parameterized with the same formal type parameters. Similarly, when a method declaration is desugared, the implied implementation and signature declarations have the same explicit type parameters and formal argument types, including any implicit type parameter bindings. For example, the declarations

```
abstract object collection[T];
method print(c@:collection[`T <= printable]):void {...}
method expand_tabs(c@:`T <= collection[char]):T {...}
abstract object table[Key,Value] isa collection[Value];
abstract object indexed[T] isa table[int,T];
template object array[T] isa indexed[T];
method new_array[T](size:int, initial_value:T):array[T] {...}
```

are syntactic sugar for the following declarations:

```
type collection[T];
abstract representation collection[T] subtypes collection[T];
   signature print(collection[`T <= printable]):void;</pre>
   implementation print(c@:collection['T <= printable]):void {...}</pre>
   signature expand_tabs('T <= collection[char]):T;</pre>
   implementation expand_tabs(c@:'T <= collection[char]):T {...}</pre>
type table[Key,Value] subtypes collection[Value];
abstract representation table[Key,Value] inherits collection[Value]
                                          subtypes table[Key,Value];
type indexed[T] subtypes table[int,T];
abstract representation indexed[T] inherits table[int,T]
                                    subtypes indexed[T];
type array[T] subtypes indexed[T];
template representation array[T] inherits indexed[T]
                                  subtypes array[T];
   signature new_array[T](int, T):array[T];
   implementation new_array[T](size:int, initial_value:T):array[T] {...}
```

## 4.7 F-Bounded Polymorphism

#### 4.7.1 Motivation

In section 4.2, the min method was defined as follows:

```
method min(x1:`T1 <= comparable, x2:`T2 <= comparable):T1|T2 {
    if (x1 < x2, { x1 }, { x2 })}</pre>
```

The type comparable might be defined as follows:

```
abstract object comparable;
```

```
signature = (x@:comparable, y@:comparable):bool;
method !=(x@:comparable, y@:comparable):bool { not(x = y) }
signature < (x@:comparable, y@:comparable):bool;
method <=(x@:comparable, y@:comparable):bool { x = y | x < y }
method >=(x@:comparable, y@:comparable):bool { x = y | x > y }
method > (x@:comparable, y@:comparable):bool { y < x }</pre>
```

Numbers could be declared to be comparable as follows:

extend number isa comparable;

With this declaration, any pair of numbers could be used as arguments to the min method. We would also like to state that collections of comparable things are also comparable:

extend collection[`T <= comparable] isa comparable;</pre>

Unfortunately, these declarations are not likely to both appear in the same Cecil program, because this would require that numbers could be compared against collections of numbers. Subtyping as used in the declaration `T <= comparable in the min method only constrains a single object. What we need to do for this case is to be able to describe that two objects come from related types, e.g., that both arguments to min are subtypes of number or that both are subtypes of the collection type instantiated with related types.

#### 4.7.2 F-Bounded Polymorphism in Singly-Dispatched Languages

F-bounded polymorphism [Canning *et al.* 89, Cook *et al.* 90] supports parameterization where the upper bound constraint of a type parameter can be a function of the type parameter itself. This enables parameterized types to be used to describe patterns of types that are not necessarily subtypes of one another. Versions of F-bounded polymorphism have appeared in single-dispatching languages such as Emerald [Black & Hutchinson 90], Axiom (formerly Scratchpad II) [Watt *et al.* 88, Jenks & Sutor 92], Strongtalk [Bracha & Griswold 93], and k-bench [Santas 93].

In a singly-dispatched language with F-bounded polymorphism, the comparable type could be defined as follows:

```
class comparable[T] {
    signature =(y:T);
    method !=(y:T):bool { not(x = y) }
    signature < (y:T):bool;
    method <=(y:T):bool { x = y | x < y }
    method >=(y:T):bool { x = y | x > y }
    method > (y:T):bool { y < x }
};</pre>
```

Then comparable types could be declared as subtypes of instances of this parameterized type:

```
extend num isa comparable[num];
extend collection['T <= comparable[T]] isa comparable[collection[T]];</pre>
```

Functions that are polymorphic over comparable types could be written using explicit parameterization as follows:

```
method min[T <= comparable[T]](x1:T, x2:T):T {
    if (x1 < x2, { x1 }, { x2 })}</pre>
```

The seemingly recursive nature of the explicit type parameter of both collection and min is not a problem. For a type of the form  $T \le type[T]$ , first the actual instantiating type parameter is bound to the type variable *T*, then this type is checked against *type* instantiated with the type bound to *T*. For example, for the following call:

min[num](3, 4.5)

first T is bound to num, then the system checks that num is a subtype of comparable[num], which holds.

#### 4.7.3 F-Bounded Polymorphism in Cecil

In Cecil, F-bounded polymorphism needs to be extended to support multi-methods and implicit type parameters. Straightforward translation of the parameterized comparable class into Cecil, introducing an explicit formal parameter for the implied self argument, might lead to the following declarations:

```
abstract object comparable[T];
signature = (x@:comparable[`T], y@:T):bool;
method !=(x@:comparable[`T], y@:T):bool { not(x = y) }
signature < (x@:comparable[`T], y@:T):bool;
method <=(x@:comparable[`T], y@:T):bool { x = y | x < y }
method >=(x@:comparable[`T], y@:T):bool { x = y | x > y }
method > (x@:comparable[`T], y@:T):bool { y < x }</pre>
```

Unfortunately, each of these definitions of operations on comparable objects is asymmetric: the first argument determines the instantiating type for comparable, which then constrains the type of the second argument. This is contrary to the Cecil philosophy of treating arguments symmetrically. Additionally, the body of the > method does not typecheck, since the signature <(T, comparable[T]) is not defined, only <(comparable[T], T).

The following revised implementation of comparable treats arguments uniformly:

```
abstract object comparable[T];
signature = (x@:comparable[`T], y@:comparable[`T]):bool;
method !=(x@:comparable[`T], y@:comparable[`T]):bool { not(x = y) }
signature < (x@:comparable[`T], y@:comparable[`T]):bool;
method <=(x@:comparable[`T], y@:comparable[`T]):bool { x = y | x < y }
method >=(x@:comparable[`T], y@:comparable[`T]):bool { x = y | x > y }
method > (x@:comparable[`T], y@:comparable[`T]):bool { x = y | x > y }
method > (x@:comparable[`T], y@:comparable[`T]):bool { y < x }</pre>
```

Unfortunately, it is not legal Cecil: it binds the same type variable twice in the same scope. If such as facility were legal, with the semantics that the system would find a single most-specific type to bind to T that enables both formal type patterns to match, then mixed-type comparisons would work correctly. The system would locate a single type to which both argument comparable types can be instantiated. For the case of comparing integers to reals, this common type is num.

In a similar fashion, if multiple bindings of the same type variable were allowed, min could be written using only implicit type parameters:

```
method min(x1:`T1 <= comparable[`T], x2:`T2 <= comparable[`T]):T1|T2 {
    if (x1 < x2, { x1 }, { x2 })}</pre>
```

This definition of min is more convenient than the earlier definition because it does not require the caller to provide an explicit type parameter.

Since these kinds of non-linear type patterns appear to resolve several problems with types such as comparable, we are investigating the feasibility of extending Cecil to support them.

## 4.7.4 F-Bounded Polymorphism among Multiple Types

The type comparable was self-recursive in a sense: its parameter type was used to link the types of the arguments to its operations. A more general case involves two or more mutually-recursive types. For example, consider a simplified model-view framework, where the model and the view must be able refer to each other and invoke operations on each other.<sup>\*</sup> Moreover, instances of the model-view framework, such as a drawing model and a drawing view, must be able to invoke specific operations on each other without loss of type safety. To define such a framework, we exploit F-bounded style parameterized implementation strategies. The following code shows how the generic model-view framework can be defined:

```
abstract object model[`M <= model[M,V], `V <= view[M,V]];
field views(@:model[`M, `V]):set[V] := new_set[V]();
method register_view(m@:model[`M, `V], view:V):void {
    m.views.add(view); }
method update(m@:model[`M, `V]):void {
    m.views.do(&(v:V) {
        v.update();
    }); }
abstract object view[`M <= model[M,V], `V <= view[M,V]];
field model(@:view[`M, `V]):W;
signature update(v@:view[`M, `V]):void;
```

Both model and view are parameterized by the type of the model and the view. These formal parameters are bounded by seemingly recursively-defined instances of the model and view types. As discussed above, no problem results from this recursive nature, since the type variables M and  $\nabla$  are first bound to their actual parameters, and then the upper bounds are checked. By parameterizing both model and view by each other's type, with the corresponding upper bound, the code in the parameterized model and view can be parameterized by the actual type of the instantiation of the framework. For example, the following code instantiates the generic model-view framework to construct a bitmap drawing model and view:

```
template object drawing isa model[drawing,drawing_view];
  field bitmap(@:drawing):bitmap;
  method set_pixel(m@:drawing, pos:position, value:color):void {
    bitmap.pixel(pos) := value;
    m.views.do(&(v:drawing_view){
        v.update_pixel(pos, value);
      }); }
```

template object drawing\_view isa view[drawing,drawing\_view];

<sup>&</sup>lt;sup>\*</sup> Thanks to Gail Murphy for suggesting this problem to us.

```
method update(v@:drawing_view):void {
   screen.plot(v.model.bitmap); }
method update_pixel(v@:drawing_view, pos:position, value:color):void {
   screen.plot_pixel(pos, value); }
method new_drawing_view(m@:drawing):drawing_view {
   concrete object isa drawing_view { model := m } }
```

Both drawing and drawing\_view add new operations that need to be called by the other type. By parameterizing model as was done, the type of the views field in drawing is known statically to be set of (subtypes of) drawing\_view. This knowledge allows the set\_pixel operation in drawing to invoke the update\_pixel operation without generating either a static type-error or requiring a dynamic "typecase" or "narrow" operation. Similarly, because of the way view is parameterized, the model field in its child drawing\_view will be known statically to refer to a (subtype of) drawing, allowing the update operation of drawing\_view to access the bitmap field of the model in a statically type-safe manner.

# 5 Modules

Object-oriented methods encourage programmers to develop reusable libraries of code. However, multi-methods can pose obstacles to smoothly integrating code that was developed independently. Unlike with singly-dispatched systems, if two classes that subclass a common class are included into a program, it is possible for incompleteness or inconsistency to result. The additional expressiveness and flexibility of multi-methods creates new pitfalls for integration.

Encapsulation and modularity of multi-methods is a related problem. To enable easier program reuse and maintenance, it is often desirable to encapsulate a data structure's implementation. However, in a multiply-dispatched language achieving this encapsulation is less straightforward than it would be in either an abstract data type based language, such as CLU, or a singly dispatched object-oriented language, such as C++ or Smalltalk. In ADT-based or singly-dispatched languages, direct access to an object's representation can be limited to a statically-determined region of the program. An earlier approach to encapsulation in Cecil suffered from the problem that privileged access could always be gained by writing methods that specialized on the desired data structures [Chambers 92b].

The Cecil module system has been designed to support integration of separately developed code, encapsulation, and modular design. This system can restrict access to parts of an implementation to a bounded region of program text while preserving the flexibility of multi-methods. Individual modules can be reasoned about and typechecked in isolation from modules not explicitly imported. Modules can *extend* existing modules with subclasses, subtypes, and augmenting multi-methods. If any conflicts arise between independent extensions, they are resolved through *resolving modules* that extend each of the conflicting modules. A simple check for the presence of the necessary resolving modules is all that is needed at link-time to guarantee type safety. Chambers and Leavens describe the Cecil module system in more detail [Chambers and Leavens 94].

The syntax of declarations is extended to support modules as follows:

| decl        | ::= | module_decl   |
|-------------|-----|---|
|             |     | <pre>import_decl</pre>  |
|             | Í   | let_decl  |
|             |     | tp_decl   |
|             | Í   | type_ext_decl   |
|             |     | object_decl   |
|             |     | obj_ext_decl  |
|             | Í   | predicate_decl  |
|             |     | disjoint_decl   |
|             |     | cover_decl  |
|             |     | divide_decl   |
|             |     | signature_decl  |
|             |     | method_decl   |
|             |     | field_sig_decl  |
|             |     | field_decl  |
|             |     | precedence_decl   |
|             |     | include_decl  |
|             |     | prim_decl   |
| privacy     | ::= | "public"   "protected"   "private"  |
| module_decl | ::= | <pre>[privacy] "module" module_name [extension] "{"     {friendship   decl} "}" [";"]</pre> |

| extension    | ::= | "extends" module_names                                    |
|--------------|-----|---|
| friendship   | ::= | "friend" module_names ";"                                 |
| module_names | ::= | <pre>module_name {"," module_name}</pre>                  |
| module_name  | ::= | name  |
| import_decl  | ::= | <pre>[privacy] "import" ["friend"] module_names ";"</pre> |

Also, most declarations have an optional privacy annotation allowed.

[The precise semantics of modules is still under development.]

# 6 Related Work

Cecil builds upon much of the work done with the Self programming language [Ungar & Smith 87, Hölzle *et al.* 91a]. Self offers a simple, pure, classless object model with state accessed via message passing just like methods. Cecil extends Self with multi-methods, copy-down and initialize-only data slots, lexically-scoped local methods and fields, object extensions, static typing, and a module system. Cecil has simpler method lookup and encapsulation rules, at least when considering only the single dispatching case. Cecil's model of object creation is different than Self's. However, Cecil does not incorporate dynamic inheritance, one of the most interesting features of Self; predicate objects are Cecil's more structured but more restricted alternative to dynamic inheritance. Freeman-Benson independently developed a proposal for adding multi-methods to Self [Freeman-Benson 89].

Common Loops [Bobrow *et al.* 86] and CLOS [Bobrow *et al.* 88, Gabriel *et al.* 91] incorporate multi-methods in dynamically-typed class-based object-oriented extensions to Lisp. Method specializations (at least in CLOS) can be either on the class of the argument object or on its value. One significant difference between Cecil's design philosophy and that in CLOS and its predecessors is that Cecil's multiple inheritance and multiple dispatching rules are unordered and report any ambiguities in the source program as message errors, while in CLOS left-to-right linearization of the inheritance graph and left-to-right ordering of the argument dispatching serves to resolve all message ambiguities automatically, potentially masking real programming errors. We feel strongly that the programmer should be made aware of potential ambiguities since automatic resolution of these ambiguities can easily lead to obscure errors in programs. Cecil offers a simpler, purer object model, optional static type checking, and encapsulation. CLOS and its predecessors include extensive support for method combination rules and reflective operations [Kiczales *et al.* 91] not present in Cecil.

Dylan [Apple 92] is a new language which can be viewed as a slimmed-down CLOS, based in a Scheme-like language instead of Common Lisp. Dylan is similar to CLOS in most of the respects described above, except that Dylan always accesses state through messages. Dylan supports a form of type declarations, but these are not checked statically, cannot be parameterized, and are treated both as argument specializers and type declarations, unlike Cecil where argument specializers and argument type declarations are distinct.

Polyglot is a CLOS-like language with a static type system [Agrawal *et al.* 91]. However, the type system for Polyglot does not distinguish subtyping from code inheritance (classes are the same as types in Polyglot), does not support parameterized or parametrically polymorphic classes or methods, and does not support abstract methods or signatures. To check consistency among multi-methods within a generic function, at least the interfaces to all multi-methods of a generic function must be available at type-check-time. This requirement is similar to that of Cecil that the whole program be available at type-check-time to guarantee that two multi-methods are not mutually ambiguous for some set of argument objects.

Kea is a higher-order polymorphic functional language supporting multi-methods [Mugridge *et al.* 91]. Like Polyglot (and most other object-oriented languages), inheritance and subtyping in Kea

are unified. Kea's type checking of multi-methods is similar to Cecil's in that multi-methods must be both complete and consistent. It appears that Kea has a notion of abstract methods as well.

Leavens describes a statically-typed applicative language NOAL that supports multi-methods using run-time overloading on the declared argument types of methods [Leavens 89, Leavens & Weihl 90]. NOAL was designed primarily as a vehicle for research on formal verification of programs with subtyping using behavioral specifications, and consequently omits theoretically unnecessary features that are important for practical programming, such as inheritance of implementation, mixed static and dynamic type checking, and mutable state. Other theoretical treatments of multi-methods have been pursued by Rouaix [Rouaix 90], Ghelli [Ghelli 91], Castagna [Castagna *et al.* 92, Castagna 95], and Pierce and Turner [Pierce & Turner 92, Pierce & Turner 93].

The RPDE<sup>3</sup> environment supports *subdivided methods* where the value of a parameter to the method or of a global variable helps select among alternative method implementations [Harrison & Ossher 90]. However, a method can be subdivided only for particular values of a parameter or global variable, not its class; this is much like supporting only CLOS's eql specializers.

A number of languages, including C++ [Stroustrup 86, Ellis & Stroustrup 90], Ada [Barnes 91], and Haskell [Hudak *et al.* 90], support static overloading on function arguments, but all overloading is resolved at compile-time based on the static types of the arguments (and results, in the case of Ada) rather than on their dynamic types as would be required for true multiple dispatching.

Trellis<sup>\*</sup> supports an expressive, safe static type system [Schaffert *et al.* 85, Schaffert *et al.* 86]. Cecil's parameterized type system includes features not present in Trellis, such as implicitly-bound type variables and uniform treatment of constrained type variables. Trellis restricts the inheritance hierarchy to conform to the subtype hierarchy; it only supports *isa-style* superclasses.

POOL is a statically-typed object-oriented language that distinguishes inheritance of implementation from inheritance of interface [America & van der Linden 90]. POOL generates types automatically from all class declarations (Cecil allows the programmer to restrict which objects may be used as types). Subtyping is implicit (structural) in POOL: all possible legal subtype relationships are assumed to be in force. Programmers may add explicit subtype declarations as a documentation aid and to verify their expectations. One unusual aspect of POOL is that types and classes may be annotated with *properties*, which are simple identifiers that may be used to capture distinctions in behavior that would not otherwise be expressed by a purely syntactic interface. This ameliorates some of the drawbacks of implicit subtyping.

Emerald is another classless object-oriented language with a static type system [Black *et al.* 86, Hutchinson 87, Hutchinson *et al.* 87, Black & Hutchinson 90]. Emerald is not based on multiple dispatching and in fact does not include support for inheritance of implementation. Types in Emerald are arranged in a subtype lattice, however.

<sup>\*</sup> Formerly known as Owl and Trellis/Owl.

Rapide [Mitchell *et al.* 91] is an extension of Standard ML modules [Milner *et al.* 90] with subtyping and inheritance. Although Rapide does not support multi-methods and relies on implicit subtyping, many other design goals for Rapide are similar to those for Cecil.

Some more recent languages support some means for distinguishing subtyping from inheritance. These languages include Theta [Day *et al.* 95], Java [Sun 95], and Sather [Omohundro 93]. Theta additionally supports an enhanced CLU-like where-clause mechanism that provides an alternative to F-bounded polymorphism. C++'s private inheritance supports a kind of inheritance without subtyping.

Several languages support some form of mixed static and dynamic type checking. For example, CLU [Liskov *et al.* 77, Liskov *et al.* 81] allows variables to be declared to be of type any. Any expression may be assigned to a variable of type any, but any assignments of an expression of type any to an expression of another type must be explicitly coerced using the parameterized force procedure. Cedar supports a similar mechanism through its REF ANY type [Teitelman 84]. Modula-3 retains the REFANY type and includes several operations including NARROW and TYPECASE that can produce a more precisely-typed value from a REFANY type [Nelson 91, Harbison 92]. Cecil provides better support for exploratory programming than these other languages since there is no source code "overhead" for using dynamic typing: variable type declarations are simply omitted, and coercions between dynamically-typed expressions and statically-typed variables are implicit. On the other hand, in Cecil it sometimes can be subtle whether some expression is statically-typed.

# 7 Conclusion

Cecil is a pure object-oriented language intended to support the rapid construction of reliable, extensible systems. It incorporates a relatively simple object model which is based on multiple dispatching. Cecil compliments this object model with a static type system that describes the interfaces to objects instead of their representations and a module system to group and encapsulate objects and methods. Cecil's type system distinguishes subtyping from code inheritance, but uses notation that strives to minimize the burden on the programmer of maintaining these separate object and type relationships. The type system supports explicitly and implicitly parameterized types and methods to precisely capture the relationships among argument types and result types in a convenient and concise way. Cecil supports both an exploratory programming style and a production programming style, in part by allowing a program to mature incrementally from a dynamically-typed system to a statically-typed system. Some areas of Cecil's design are the subject of current work, including the details of the parameterization mechanism in the static type system, the precise semantics of the module system, and a formal specification of the static and dynamic semantics of the language.

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More information on the Cecil language and Vortex optimizing compiler projects are available via http://www.cs.washington.edu/research/projects/cecil and via anonymous ftp from cs.washington.edu:pub/chambers.

#### References

- [Agrawal et al. 91] Rakesh Agrawal, Linda G. DeMichiel, and Bruce G. Lindsay. Static Type Checking of Multi-Methods. In OOPSLA '91 Conference Proceedings, pp. 113-128, Phoenix, AZ, October, 1991. Published as SIGPLAN Notices 26(11), November, 1991.
- [America & van der Linden 90] Pierre America and Frank van der Linden. A Parallel Object-Oriented Language with Inheritance and Subtyping. In *OOPSLA/ECOOP '90 Conference Proceedings*, pp. 161-168, Ottawa, Canada, October, 1990. Published as *SIGPLAN Notices 25(10)*, October, 1990.
- [Andersen & Reenskaug 92] Egil P. Andersen and Trygve Reenskaug. System Design by Composing Structures of Interacting Objects. In ECOOP '92 Conference Proceedings, pp. 133-152, Utrecht, the Netherlands, June/July 1992. Published as Lecture Notes in Computer Science 615, Springer-Verlag, Berlin, 1992.
- [Apple 92] Dylan, an Object-Oriented Dynamic Language. Apple Computer, April, 1992.
- [Barnes 91] J. G. P. Barnes. *Programming in Ada, 3rd Edition*. Addison-Wesley, Wokingham, England, 1991.
- [Black et al. 86] Andrew Black, Norman Hutchinson, Eric Jul, and Henry Levy. Object Structure in the Emerald System. In OOPSLA '86 Conference Proceedings, pp. 78-86, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Black & Hutchinson 90] Andrew P. Black and Norman C. Hutchinson. Typechecking Polymorphism in Emerald. Technical report TR 90-34, Department of Computer Science, University of Arizona, December, 1990.
- [Bobrow et al. 86] Daniel G. Bobrow, Kenneth Kahn, Gregor Kiczales, Larry Masinter, Mark Stefik, and Frank Zdybel. CommonLoops: Merging Lisp and Object-Oriented Programming. In OOPSLA '86 Conference Proceedings, pp. 17-29, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Bobrow et al. 88] D. G. Bobrow, L. G. DeMichiel, R. P. Gabriel, S. E. Keene, G. Kiczales, D. A. Moon. Common Lisp Object System Specification X3J13. In SIGPLAN Notices 23(Special Issue), September, 1988.
- [Borning 86] A. H. Borning. Classes Versus Prototypes in Object-Oriented Languages. In *Proceedings of the 1986 Fall Joint Computer Conference*, pp. 36-40, Dallas, TX, November, 1986.
- [Bracha & Griswold 93] Gilad Bracha and David Griswold. Strongtalk: Typechecking Smalltalk in a Production Environment. In *OOPSLA '93 Conference Proceedings*, pp. 215-230, Washington, D.C., September 1993. Published as *SIGPLAN Notices 28(10)*, October 1993.
- [Canning et al. 89] Peter S. Canning, William R. Cook, Walter L. Hill, John C. Mitchell, and William Olthoff. F-Bounded Quantification for Object-Oriented Programming. In Proceedings of the Conference on Functional Programming Languages and Computer Architecture, 1989.
- [Cardelli & Wegner 85] Luca Cardelli and Peter Wegner. On Understanding Types, Data Abstraction, and Polymorphism. In *Computing Surveys 17(4)*, pp. 471-522, December, 1985.
- [Castagna et al. 92] Giuseppe Castagna, Giorgio Ghelli, and Giuseppe Longo. A Calculus for Overloaded Functions with Subtyping. In Proceedings of the 1992 ACM Conference on Lisp and Functional Programming, pp. 182-192, San Francisco, June, 1992. Published as Lisp Pointers 5(1), January-March, 1992.
- [Castagna 95] Giuseppe Castagna. Covariance and Contravariance: Conflict without a Cause. In ACM Transactions on Programming Languages and Systems 17(3), pp. 431-447, May 1995.

- [Chambers et al. 89] Craig Chambers, David Ungar, and Elgin Lee. An Efficient Implementation of Self, a Dynamically-Typed Object-Oriented Language Based on Prototypes. In OOPSLA '89 Conference Proceedings, pp. 49-70, New Orleans, LA, October, 1989. Published as SIGPLAN Notices 24(10), October, 1989. Also published in Lisp and Symbolic Computation 4(3), Kluwer Academic Publishers, June, 1991.
- [Chambers *et al.* 91] Craig Chambers, David Ungar, Bay-Wei Chang, and Urs Hölzle. Parents are Shared Parts: Inheritance and Encapsulation in Self. In *Lisp and Symbolic Computation 4(3)*, Kluwer Academic Publishers, June, 1991.
- [Chambers & Ungar 91] Craig Chambers and David Ungar. Making Pure Object-Oriented Languages Practical. In *OOPSLA '91 Conference Proceedings*, pp. 1-15, Phoenix, AZ, October, 1991. Published as *SIGPLAN Notices 26(10)*, October, 1991.
- [Chambers 92a] Craig Chambers. *The Design and Implementation of the Self Compiler, an Optimizing Compiler for Object-Oriented Programming Languages*. Ph.D. thesis, Department of Computer Science, Stanford University, March, 1992.
- [Chambers 92b] Craig Chambers. Object-Oriented Multi-Methods in Cecil. In ECOOP '92 Conference Proceedings, pp. 33-56, Utrecht, the Netherlands, June/July, 1992. Published as Lecture Notes in Computer Science 615, Springer-Verlag, Berlin, 1992.
- [Chambers 93a] Craig Chambers. The Cecil Language: Specification and Rationale. Technical report #93-03-05, Department of Computer Science and Engineering, University of Washington, March, 1993.
- [Chambers 93b] Craig Chambers. Predicate Classes. In ECOOP '93 Conference Proceedings, pp. 268-296, Kaiserslautern, Germany, July, 1993. Published as Lecture Notes in Computer Science 707, Springer-Verlag, Berlin, 1993.
- [Chambers & Leavens 94] Craig Chambers and Gary T. Leavens. Typechecking and Modules for Multi-Methods. In *OOPSLA '94 Conference Proceedings*, pp. 1-15, Portland, OR, October 1994. Published as *SIGPLAN Notices 29(10)*, October 1994. An expanded and revised version to appear in *ACM Transactions on Programming Languages and Systems*.
- [Chang & Ungar 90] Bay-Wei Chang and David Ungar. Experiencing Self Objects: An Object-Based Artificial Reality. Unpublished manuscript, 1990.
- [Cook 89] W. R. Cook. A Proposal for Making Eiffel Type-Safe. In *ECOOP* '89 Conference Proceedings, pp. 57-70, Cambridge University Press, July, 1989.
- [Cook et al. 90] William Cook, Walter Hill, and Peter Canning. Inheritance is not Subtyping. In Conference Record of the 17th Annual ACM Symposium on Principles of Programming Languages, San Francisco, CA, January, 1990.
- [Cook 92] William R. Cook. Interfaces and Specifications for the Smalltalk-80 Collection Classes. In In OOPSLA '92 Conference Proceedings, pp. 1-15, Vancouver, Canada, October, 1992. Published as SIGPLAN Notices 27(10), October, 1992.
- [Day et al. 95] Mark Day, Robert Gruber, Barbara Liskov, and Andrew C. Meyers. Subtypes vs. Where Clauses: Constraining Parametric Polymorphism. In Proceedings of the 1995 ACM Conference on Object-Oriented Programming Systems, Languages, and Applications (OOPSLA '95), pp. 156-168, Austin, TX, October 1995.
- [Dean & Chambers 94] Jeffrey Dean and Craig Chambers. Towards Better Inlining Decisions Using Inlining Trials. In Proceedings of the ACM Symposium on Lisp and Functional Programming, pp. 273-282, Orlando, FL, June 1994. Published as Lisp Pointers 7(3), July-September 1994.
- [Dean *et al.* 95a] Jeffrey Dean, Craig Chambers, and David Grove. Selective Specialization in Object-Oriented Languages. In *Proceedings of the 1995 SIGPLAN Conference on Programming Language Design and Implementation (PLDI '95)*, La Jolla, CA, June 1995.

- [Dean et al. 95b] Jeffrey Dean, David Grove, and Craig Chambers. Optimization of Object-Oriented Programs Using Static Class Hierarchy Analysis. In Proceedings of the European Conference on Object-Oriented Programming (ECOOP '95), Århus, Denmark, August 1995.
- [Ellis & Stroustrup 90] Margaret A. Ellis and Bjarne Stroustrup. *The Annotated C++ Reference Manual*. Addison-Wesley, Reading, MA, 1990.
- [Freeman-Benson 89] Bjorn N. Freeman-Benson. A Proposal for Multi-Methods in Self. Unpublished manuscript, December, 1989.
- [Gabriel et al. 91] Richard P. Gabriel, Jon L White, and Daniel G. Bobrow. CLOS: Integrating Object-Oriented and Functional Programming. In *Communications of the ACM 34(9)*, pp. 28-38, September, 1991.
- [Ghelli 91] Giorgio Ghelli. A Static Type System for Message Passing. In OOPSLA '91 Conference Proceedings, pp. 129-145, Phoenix, AZ, October, 1991. Published as SIGPLAN Notices 26(11), November, 1991.
- [Goldberg & Robson 83] Adele Goldberg and David Robson. Smalltalk-80: The Language and Its Implementation. Addison-Wesley, Reading, MA, 1983.
- [Goldberg 84] Adele Goldberg. Smalltalk-80: The Interactive Programming Environment. Addison-Wesley, Reading, MA, 1984.
- [Grove et al. 95] David Grove, Jeffrey Dean, Charles Garrett, and Craig Chambers. Profile-Guided Receiver Class Prediction. In Proceedings of the 1995 ACM Conference on Object-Oriented Programming Systems, Languages, and Applications (OOPSLA '95), Austin, TX, October 1995.
- [Grove 95] David Grove. The Impact of Interprocedural Class Analysis on Optimization. In *Proceedings of CASCON* '95, pp. 195-203, Toronto, Canada, November 1995.
- [Halbert & O'Brien 86] Daniel C. Halbert and Patrick D. O'Brien. Using Types and Inheritance in Object-Oriented Languages. Technical report DEC-TR-437, Digital Equipment Corp., April, 1986.
- [Harbison 92] Samuel P. Harbison. Modula-3. Prentice Hall, Englewood Cliffs, NJ, 1992.
- [Harrison & Ossher 90] William Harrison and Harold Ossher. Subdivided Procedures: A Language Extension Supporting Extensible Programming. In *Proceedings of the 1990 International Conference on Computer Languages*, pp. 190-197, New Orleans, LA, March, 1990.
- [Harrison & Ossher 93] William Harrison and Harold Ossher. Subject-Oriented Programming (A Critique of Pure Objects). In *OOPSLA '93 Conference Proceedings*, pp. 411-428, Washington, D.C., September 1993. Published as *SIGPLAN Notices 28(10)*, October 1993.
- [Hölzle et al. 91a] Urs Hölzle, Bay-Wei Chang, Craig Chambers, Ole Agesen, and David Ungar. The Self Manual, Version 1.1. Unpublished manual, February, 1991.
- [Hölzle *et al.* 91b] Urs Hölzle, Craig Chambers, and David Ungar. Optimizing Dynamically-Typed Object-Oriented Programming Languages with Polymorphic Inline Caches. In *ECOOP '91 Conference Proceedings*, pp. 21-38, Geneva, Switzerland, July, 1991.
- [Hölzle *et al.* 92] Urs Hölzle, Craig Chambers, and David Ungar. Debugging Optimized Code with Dynamic Deoptimization. To appear in *Proceedings of the SIGPLAN '92 Conference on Programming Language Design and Implementation*, San Francisco, CA, June, 1992.
- [Hölzle 93] Urs Hölzle. Integrating Independently-Developed Components in Object-Oriented Languages. In ECOOP '93 Conference Proceedings, pp. 36-56, Kaiserslautern, Germany, July 1993. Published as Lecture Notes in Computer Science 707, Springer-Verlag, Berlin, 1993.
- [Hudak et al. 90] Paul Hudak, Philip Wadler, Arvind, Brian Boutel, Jon Fairbairn, Joseph Fasel, Kevin Hammond, John Hughes, Thomas Johnsson, Dick Kieburtz, Rishiyur Nikhil, Simon Peyton Jones, Mike Reeve, David Wise, Jonathan Young. *Report on the Programming Language Haskell, Version 1.0.* Unpublished manual, April, 1990.

- [Hutchinson 87] Norman C. Hutchinson. *Emerald: An Object-Based Language for Distributed Programming*. Ph.D. thesis, University of Washington, January, 1987.
- [Hutchinson et al. 87] Norman C. Hutchinson, Rajendra K. Raj, Andrew P. Black, Henry M. Levy, and Eric Jul. The Emerald Programming Language Report. Technical Report 87-10-07, Department of Computer Science, University of Washington, October, 1987.
- [Ingalls 86] Daniel H. H. Ingalls. A Simple Technique for Handling Multiple Polymorphism. In OOPSLA '86 Conference Proceedings, pp. 347-349, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Jenks & Sutor 92] Richard D. Jenks and Robert S. Sutor. Axiom: the Scientific Computing System. Springer-Verlag. 1992.
- [Kiczales et al. 91] Gregor Kiczales, James des Rivières, and Daniel G. Bobrow. The Art of the Meta-Object Protocol. MIT Press, Cambridge, MA, 1991.
- [Kristensen et al. 87] B. B. Kristensen, Ole Lehrmann Madsen, Birger Møller-Pedersen, and Kristen Nygaard. The BETA Programming Language. In *Research Directions in Object-Oriented Programming*, MIT Press, Cambridge, MA, 1987.
- [LaLonde et al. 86] Wilf R. LaLonde, Dave A. Thomas, and John R. Pugh. An Exemplar Based Smalltalk. In OOPSLA '86 Conference Proceedings, pp. 322-330, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Leavens 89] Gary Todd Leavens. Verifying Object-Oriented Programs that use Subtypes. Ph.D. thesis, MIT, 1989.
- [Leavens & Weihl 90] Gary T. Leavens and William E. Weihl. Reasoning about Object-Oriented Programs that use Subtypes. In *OOPSLA/ECOOP '90 Conference Proceedings*, pp. 212-223, Ottawa, Canada, October, 1990. Published as *SIGPLAN Notices 25(10)*, October, 1990.
- [Lieberman 86] Henry Lieberman. Using Prototypical Objects to Implement Shared Behavior in Object-Oriented Systems. In OOPSLA '86 Conference Proceedings, pp. 214-223, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Lieberman *et al.* 87] Henry Lieberman, Lynn Andrea Stein, and David Ungar. The Treaty of Orlando. In *Addendum to the OOPSLA '87 Conference Proceedings*, pp. 43-44, Orlando, FL, October, 1987. Published as *SIGPLAN Notices 23(5)*, May, 1988.
- [Liskov et al. 77] Barbara Liskov, Alan Snyder, Russell Atkinson, and J. Craig Schaffert. Abstraction Mechanisms in CLU. In *Communications of the ACM 20(8)*, pp. 564-576, August, 1977.
- [Liskov et al. 81] Barbara Liskov, Russell Atkinson, Toby Bloom, Eliot Moss, J. Craig Schaffert, Robert Scheifler, and Alan Snyder. *CLU Reference Manual*. Springer-Verlag, Berlin, 1981.
- [Meyer 86] Bertrand Meyer. Genericity versus Inheritance. In *OOPSLA '86 Conference Proceedings*, pp. 391-405, Portland, OR, September, 1986. Published as *SIGPLAN Notices 21(11)*, November, 1986.
- [Meyer 88] Bertrand Meyer. Object-Oriented Software Construction. Prentice Hall, New York, 1988.
- [Meyer 92] Bertrand Meyer. Eiffel: The Language. Prentice Hall, New York, 1992.
- [Milner *et al.* 90] Robin Milner, Mads Tofte, and Robert Harper. *The Definition of Standard ML*. MIT Press, Cambridge, MA, 1990.
- [Mitchell et al. 91] John Mitchell, Sigurd Meldal, and Neel Hadhav. An Extension of Standard ML Modules with Subtyping and Inheritance. In *Conference Record of the ACM Symposium on Principles of Programming Languages*, Williamsburg, VA, January, 1991.
- [Moon 86] David A. Moon. Object-Oriented Programming with Flavors. In OOPSLA '86 Conference Proceedings, pp. 1-8, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.

- [Mugridge *et al.* 91] W. B. Mugridge, J. G. Hosking, and J. Hamer. Multi-Methods in a Statically-Typed Programming Language. Technical report #50, Department of Computer Science, University of Auckland, 1991. Also in *ECOOP '91 Conference Proceedings*, Geneva, Switzerland, July, 1991.
- [Nelson 91] Greg Nelson, editor. *Systems Programming with Modula-3*. Prentice Hall, Englewood Cliffs, NJ, 1991.
- [Omohundro 93] Stephen Omohundro. The Sather 1.0 Specification. Unpublished manual, June 1993.
- [Pierce & Turner 92] Benjamin C. Pierce and David N. Turner. Statically Typed Multi-Methods via Partially Abstract Types. Unpublished manuscript, October, 1992.
- [Pierce & Turner 93] Benjamin C. Pierce and David N. Turner. Object-Oriented Programming Without Recursive Types. In Conference Record of the 20th Annual ACM Symposium on Principles of Programming Languages, January, 1993.
- [Rees & Clinger 86] Jonathan Rees and William Clinger, editors. *Revised<sup>3</sup> Report on the Algorithmic Language Scheme*. In *SIGPLAN Notices 21(12)*, December, 1986.
- [Rouaix 90] Francois Rouaix. Safe Run-Time Overloading. In *Conference Record of the 17th Annual ACM Symposium on Principles of Programming Languages*, pp. 355-366, San Francisco, CA, January, 1990.
- [Santas 93] Philip S. Santas. A Type System for Computer Algebra. In *International Symposium on Symbolic and Algebraic Computation*. 1993.
- [Schaffert *et al.* 85] Craig Schaffert, Topher Cooper, and Carrie Wilpolt. Trellis Object-Based Environment, Language Reference Manual. Technical report DEC-TR-372, November, 1985.
- [Schaffert et al. 86] Craig Schaffert, Topher Cooper, Bruce Bullis, Mike Kilian, and Carrie Wilpolt. An Introduction to Trellis/Owl. In OOPSLA '86 Conference Proceedings, pp. 9-16, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Snyder 86] Alan Snyder. Encapsulation and Inheritance in Object-Oriented Programming Languages. In OOPSLA '86 Conference Proceedings, pp. 38-45, Portland, OR, September, 1986. Published as SIGPLAN Notices 21(11), November, 1986.
- [Steele 84] Guy L. Steele Jr. Common LISP. Digital Press, 1984.
- [Stroustrup 86] Bjarne Stroustrup. *The C++ Programming Language*. Addison-Wesley, Reading, MA, 1986.
- [Sun 95] Sun Microsystems. The Java Language Specification. Unpublished manual, May 1995.
- [Teitelman 84] Warren Teitelman. *The Cedar Programming Environment: A Midterm Report and Examination*. Xerox PARC technical report CSL-83-11, June, 1984.
- [Touretzky 86] D. Touretzky. The Mathematics of Inheritance Systems. Morgan-Kaufmann, 1986.
- [Ungar & Smith 87] David Ungar and Randall B. Smith. Self: The Power of Simplicity. In *OOPSLA* '87 *Conference Proceedings*, pp. 227-241, Orlando, FL, October, 1987. Published as *SIGPLAN Notices* 22(12), December, 1987. Also published in *Lisp and Symbolic Computation* 4(3), Kluwer Academic Publishers, June, 1991.
- [Ungar *et al.* 91] David Ungar, Craig Chambers, Bay-Wei Chang, and Urs Hölzle. Organizing Programs without Classes. In *Lisp and Symbolic Computation* 4(3), Kluwer Academic Publishers, June, 1991.
- [Ungar 95] David Ungar. Annotating Objects for Transport to Other Worlds. In Proceedings of the 1995 ACM Conference on Object-Oriented Programming Systems, Languages, and Applications (OOPSLA '95), pp. 73-87, Austin, TX, October 1995.
- [Watt et al. 88] Steven M. Watt, Richard D. Jenks, Robert S. Sutor, and Barry M. Trager. The Scratchpad II Type System: Domains and Subdomains. In Proceedings of the International Workshop on Scientific Computation, Capri, Italy, 1988. Published in Computing Tools for Scientific Problem Solving, A. M. Miola, ed., Academic Press, 1990.

# Appendix A Annotated Cecil Syntax

In our EBNF notation, vertical bars (|) are used to separate alternatives. Braces ( $\{ ... \}$ ) surround strings that can be repeated zero or more times. Brackets ([...]) surround an optional string. Parentheses are used for grouping. Literal tokens are included in quotation marks ("...").

## A.1 Grammar

```
a program is a sequence of declaration blocks and statements;
a file included through an include_decl can contain only declarations
program ::= top_level_file
top_level_file ::= { top_decl_block | stmt | pragma }
included_file ::= top_decl_block
```

a declaration block is an unbroken sequence of declarations where names are available throughout; declaration blocks at the top level can be interspersed with pragmas top decl block ::= { decl | pragma }

| top_decl_block | ::= | { decl   | pragma |
|----------------|-----|----------|--------|
| decl_block     | ::= | decl { d | decl } |

a declaration is a variable, a field, or a method declaration

```
decl
```

```
::= module decl
    import_decl
    let_decl
    tp decl
    type_ext_decl
    object_decl
    obj_ext_decl
    predicate_decl
    disjoint_decl
    cover_decl
    divide_decl
    signature_decl
    method_decl
    field_sig_decl
    field_decl
    precedence decl
    include_decl
    prim_decl
```

privacy of a declaration defaults to public

privacy ::= "public" | "protected" | "private"

modules package up independent subsystems

| module_decl  | ::= [privacy] "module" module_name [extension] "{" |  |
|--------------|--|--|
|              | {friendship   decl} "}" [";"]                      |  |
| extension    | ::= "extends" module_names                         |  |
| friendship   | <pre>::= "friend" module_names ";"</pre>           |  |
| module_names | ::= module_name {"," module_name}                  |  |
| module_name  | ::= name   |  |

#### import declarations specify used modules

```
import_decl ::= [privacy] "import" ["friend"] module_names ";"
```

variable declarations bind names to objects; if "var" is present then variable is assignable let\_decl ::= [privacy] "let" ["var"] name [type\_decl] ":=" expr ";"

```
type, representation, and object declarations create new implementations and/or types
tp decl
                  ::= [privacy] "type" name [formal params]
                            {type_relation} ";"
                                                      declares an object type
object decl
                  ::= [privacy] rep_role rep_kind name [formal_params]
                            {relation} [field_inits] ";"
                                                      only inherited from by named objects;
rep_role
                  ::= "abstract"
                                                          allowed to be incomplete
                       "template"
                                                      only inherited from or instantiated;
                                                          uninitialized fields allowed
                       "concrete"
                                                      completely usable;
                                                          must be complete and initialized
                       ["dynamic"]
                                                      completely usable; accesses checked dynamically
                  ::= "representation"
                                                      declares an object implementation
rep kind
                                                      declares an object type and implementation
                  "object"
                  ::= "subtypes" type_patterns
type_relation
                  ::= type_relation
relation
                                                      type subtypes from type, or impl conforms to type
                       "inherits" parents
                                                      impl inherits from impl
                       "isa" parents
                                                      impl inherits from impl, type subtypes from type
                  ::= named_object_p { "," named_object_p }
parents
field_inits
                  ::= "{" field_init { "," field_init } "}"
                  ::= msg name [location] ":=" expr
field init
                  ::= "@" named_object
location
```

predicate object declaration

declarations of the relationships among predicate objects

| disjoint_decl | ::= | <pre>[privacy] "disjoint" named_objects ";"</pre>                   |
|---------------|-----|---|
| cover_decl    | ::= | <pre>[privacy] "cover" named_object "by" named_objects ";"</pre>    |
| divide_decl   | ::= | <pre>[privacy] "divide" named_object "into" named_objects ";"</pre> |
| named_objects | ::= | named_object { ``," named_object }                                  |

signature declarations declare method signatures

```
signature_decl ::= [privacy] "signature" method_name
                "(" [arg_type_ps] ")" [type_decl] ";"
arg_type_ps ::= arg_type_p { "," arg_type_p }
arg_type_p ::= [[name] ":"] type_pattern
method_name ::= msg_name [formal_params] | op_name
msg_name ::= name
```

| implementation decid | iraiion | s aejine new meinoù impiemeniailons,   | , memou aecis aejine signatures, too  |  |
|----------------------|---------|--|---|--|
| method_decl          | ::=     | <pre>[privacy] impl_kind method_name     "(" [formals] ")" [type_decl] {pragma}     "{" (body   prim_body) "}" [";"]</pre> |   |  |
| impl_kind            | ::=<br> | ["method"] "implementation"<br>"method"  | on" declares a method implementation declares a method signature and implementation |  |
| formals              | ::=     | formal { ``," formal }   |   |  |
| formal               | ::=     | [name] specializer   | formal names are optional, if never referenced                                      |  |
| specializer          | ::=     | location [type_decl_p]<br>[type_decl_p]<br>`@" ``:" named_object_p   | specialized formal<br>unspecialized formal<br>sugar for @named_obj_p :named_obj_p   |  |

implementation declarations define new method implementations; method decls define signatures, too

field declarations declare accessor method signatures and/or implementations

| field_sig_decl | ::=     | <pre>[field_privacy] ["var"] msg_name [formal_para ";"</pre> | "field" "signature"<br>ams] "(" arg_type_p ")" [type_decl]                                   |
|----------------|---------|--|--|
| field_decl     | ::=     |  | "] [``var"] ``field" field_kind<br>ams] ``(" formal ``)" [type_decl]                         |
| field_kind     | ::=<br> | <i>empty</i><br>"implementation"                             | declare accessor method impl(s) and sig(s)<br>declare just accessor method implementation(s) |
| field_privacy  | ::=     | privacy [ ("get" [ privac                                    | cy "set" ]   "set") ]  |

precedence declarations control the precedence and associativity of binary operators

| prec_decl     | ::= [privacy] "precedence" op_list                               |
|---------------|--|
|               | [associativity] {precedence} ";"                                 |
| associativity | ::= "left_associative"   "right_associative"   "non_associative" |
| precedence    | ::= "below" op_list   "above" op_list   "with" op_list           |
| op_list       | ::= op_name { "," op_name }                                      |

include declarations control textual file inclusions (implementation specific)
include\_decl ::= "include" file\_name ";"
file\_name ::= string

primitive body declarations include an arbitrary piece of code in the compiled file (implementation specific)
prim\_decl ::= prim\_body ";"

# body of a method or closure

| body | ::=<br> | <pre>{stmt} result empty</pre>           | return void |
|------|---------|--|-------------|
| stmt |         | decl_block<br>assignment ";"<br>expr ";" |             |

| result  | ::=     | normal_return   | return an expression                                   |  |  |
|---|---------|---|--|--|--|
| normal roturn   | <br>••  | non_local_rtn<br>decl_block   | return from the lexically-enclosing method return void |  |  |
| normal_return   |         | assignment [";"]  | return void  |  |  |
|   | İ       | expr [";"]  | return result of expression                            |  |  |
| non_local_rtn   | ::=     | ₩^ <i>"</i> [ ``; <i>"</i> ]  | do a non-local return, returning void                  |  |  |
|   |         | "^" expr [";"]  | do a non-local return, returning a result              |  |  |
|   |         |   |  |  |  |
| assignment only allo                                  |         | <pre>name is assignable; returns void qualified_name ``:=" expr</pre> |  |  |  |
| assignment  |         | assign_msg  | assignment-like syntax for messages                    |  |  |
| assign_msg  | ::=     | lvalue_msg ":=" expr  | sugar for set_msg(exprs, expr)                         |  |  |
| lvalue_msg  |         | message   |  |  |  |
|   |         | dot_msg   |  |  |  |
|   |         | unop_msg<br>binop_msg   |  |  |  |
|   | I       | DIII0P_IIIS9  |  |  |  |
| expressions   |         |   |  |  |  |
| expr  | ::=     | binop_expr  |  |  |  |
|   |         |   |  |  |  |
| binary msgs have lov                                  | vest pr | ecedence  |  |  |  |
| binop_expr  |         | binop_msg   unop_expr   |  |  |  |
| binop_msg   | ::=     | binop_expr op_name binop_   | _expr<br>predecence and associativity as declared      |  |  |
|   |         |   | predecence and associativity as declared               |  |  |
| unary msgs have seco                                  | ond-lo  | west precedence   |  |  |  |
| unop_expr   | ::=     | unop_msg   dot_expr   |  |  |  |
| unop_msg  | ::=     | op_name unop_expr   | & and ^ are not allowed as unary operators             |  |  |
|   |         | 11.1., 1  |  |  |  |
| -   |         | d-highest precedence  |  |  |  |
| dot_expr<br>dot_msg                                   |         | <pre>dot_msg   simple_expr dot_expr "." msg_name [page [page ]]</pre> | rangl [ N / " [ averal N ) " ]                         |  |  |
| dot_llisg   | ••-     |   | me[params](dot_expr,exprs)                             |  |  |
|   |         |   |  |  |  |
| simple messages hav                                   | e high  | •   |  |  |  |
| simple_expr   | ::=     |   |  |  |  |
|   |         | ref_expr<br>vector_expr   |  |  |  |
|   | İ       | closure_expr  |  |  |  |
|   |         | object_expr   |  |  |  |
|   |         | message<br>resend   |  |  |  |
|   |         | paren_expr  |  |  |  |
|   |         |   |  |  |  |
| literal constants                                     |         |   |  |  |  |
| literal   | ::=     | integer   |  |  |  |
|   |         | float   |  |  |  |
|   |         | character<br>string   |  |  |  |
|   | I       |   |  |  |  |
| reference a variable or a named object implementation |         |   |  |  |  |
| ref_expr  | ::=     | qualified_name  | reference a local or global variable                   |  |  |
|   |         | named_object  | reference a named object                               |  |  |

```
build a vector
vector_expr
                ::= "[" [exprs] "]"
exprs
                ::= expr { "," expr }
build a closure
closure expr ::= [ "&" "(" [closure formals] ")" [type decl] ] "{" body "}"
closure_formals::= closure_formal { "," closure_formal }
closure_formal ::= [name] [type_decl_p]
                                                 formal names are optional, if never referenced
build a new object
                ::= rep_role rep_kind {relation} [field_inits]
object_expr
send a message
message
                ::= msg_name [params] "(" [exprs] ")"
resend the message
resend
                ::= "resend" [ "(" resend args ")" ]
resend_args
                ::= resend_arg { ``, " resend_arg }
resend_arg
                ::= expr
                                                 corresponding formal of sender must be
                                                    unspecialized
                                                 undirected resend (name is a specialized formal)
                     name
                     name location
                                                 directed resend (name is a specialized formal)
introduce a new nested scope
paren expr
                ::= "(" body ")"
name something perhaps in another module
qualified name ::= [module name "$"] name
name an object
named_object ::= qualified_name [params]
named_object_p ::= qualified_name [param_patterns]
syntax of types
                ::= named type
type
                     closure_type
                     lub_type
                     glb_type
                     paren_type
                ::= qualified_name [params]
named_type
                ::= "&" "(" [arg_types] ")" [type_decl]
closure_type
                ::= arg_type { "," arg_type }
arg_types
arg_type
                ::= [[name] ":"] type
                ::= type " | " type
lub type
glb_type
                ::= type "&" type
                ::= "(" type ")"
paren_type
                ::= type { "," type }
types
```

```
formal types are types that can contain binding occurrences of implicit type parameters
                ::= binding_type
type_pattern
                     named_type_p
                     closure_type_p
                     lub_type
                     glb_type
                    paren_type
binding_type ::= "`' name ["<=" type_pattern]</pre>
named_type_p ::= qualified_name [param_patterns]
closure_type_p ::= "&" "(" [arg_type_ps] ")" [type_decl_p]
type_patterns ::= type_pattern { "," type_pattern }
type_decl ::= ":" type
type decl p
               ::= ":" type pattern
formal parameters for objects and methods
formal_params ::= "[" formal_param { "," formal_param } "]"
formal param ::= ["`'] name [ "<=" type pattern ]</pre>
actual parameters for objects and methods
                ::= "[" types "]"
params
```

actual parameters for types that may contain binding occurrences of implicit type variables param\_patterns ::= "[" type\_patterns "]"

pragmas can be added at various points in a program to provide implementation-specific hints/commands pragma ::= "(\*\*" exprs "\*\*)"

#### A.2 Tokens

Bold-faced non-terminals in this grammar are the tokens in the full grammar of A.1. As usual, tokens are defined as the longest possible sequence of characters that are in the language defined by the grammar given below. The meta-notations "one of "...", "any but x," and "x ...y" are used to concisely list a range of alternative characters. space, tab, and newline stand for the corresponding characters.

| name       | <pre>:= letter {letter   digit} [id_cont]     "_" { "_" } op_name the first underscore is not part of the msg name</pre> |
|------------|--|
| op_name    | <pre>:= punct {punct} [id_cont]     "_" { "_" } name the first underscore is not part of the msg name</pre>              |
| id_cont    | := "_" { "_" } [name   op_name]  |
| integer    | := [radix] hex_digits a leading "-" is considered a unary operator   |
| radix      | := digits "_"  |
| hex_digits | := hex_digit {hex_digit}   |
| hex_digit  | := digit   one of "afAF"   |
| float      | <pre>:= integer "." hex_digits [exponent]     integer exponent</pre>   |
| exponent   | := "^" ["+"   "-"] digits  |

| digits                      | ::= | digit {digit}   |
|-----------------------------|-----|---|
| character<br>string<br>char | ::= | <pre>"'" char "'" """ { char   line_break } """ any   "\" escape_char</pre>                             |
| escape_char                 |     | one of "'"nrtvba"<br>["o"] digit [digit [digit]]<br>"x" hex_digit [hex_digit]                           |
| line_break                  | ::= | <pre>"\" {whitespace} new_line {whitespace} "\" characters between \'s are not part of the string</pre> |
| letter<br>digit             | ::= | one of "azAZ"<br>one of "09"  |
| punct                       | ::= | one of "!#\$%^&*-+=<>/?~\ "   |

# A.3 White Space

Whitespace is allowed between any pair of tokens in the grammar in A.1.

| whitespace | ::= | space   tab   newline | comment                          |
|------------|-----|-----------------------|----------------------------------|
| comment    | ::= | "" {any but newline}  | newline comment to end of line   |
|            |     | "(" {any} ")"         | bracketed comment; can be nested |