# ATechnique for Software Module Specification with Examples 

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#### Abstract

This paper presents an approach to writing specifications for parts of software systems. The main goal is to provide specifications sufficiently precise and complete that other pieces of software can be written to interact with the piece specified without additional information. The secordary goal is to include in the specification no more information than necessary to meet the first goal. The technique is illustrated by means of a variety of examples from a tutorial system.

Key Words and Phrases: software, specification, modules, software engineering, software design

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Because of the growing recognition that a major contributing factor in the so-called "software engineering" problem is our lack of techniques for precisely specifying program segments without revealing too much information [1, 2], I would like to report on a technique for module specification which has proven moderately successful in a number of test situations.

Without taking the space to justify them [2] I would like to list the goals of the specification scheme to be described:

1. The specification must provide to the intended user all the information that he will need to use the program correctly, and nothing more.
2. The specification must provide to the implementer, all the information about the intended use that he needs to complete the program, and no additional information; in particular, no information about the structure of the calling program should be conveyed.
3. The specification must be sufficiently formal that it can conceivably be machine tested for consistency, completeness (in the sense of defining the outcome of all possible uses) and other desirable properties of a specification. Note that we do not insist that machine testing be done, only that it could conceivably be done. By this requirement we intend to rule out all natural language specifications. ${ }^{1}$
4. The specification should discuss the program in the terms normally used by user and implementer alike rather than some other area of discourse. By this we intend to exclude the specification of programs in terms of the mappings they provide between large input domains and large output domains or their specification in terms of mappings onto small automata, etc.

The basis of the technique is a view of a program module as a device with a set of switch inputs and readout indicators. The technique specifies the possible positions of the input switches and the effect of moving the

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switches on the values of the readout indicators. We insist that the values of the readout indicators be completely determined by the previous values of those indicators and the positions of the input switches.
[Aside: The notation allows for some of the pushbuttons to be combined with indicator lights or readouts (with the result that we must push a button in order to read), but we have not yet found occasion to use that facility. A simple extension of the notation allows the specification of mechanisms in which the values of the readout indicators are not determined by the above factors, but can be predicted only by knowing the values of certain "hidden" readout indicators which cannot actually be read by the user of the device. We have considerable doubts about the advisability of building devices which must be specified using this feature, but the ability to specify such devices is inexpensively gained.]

In software terms we consider each module as providing a number of subroutines or functions which can cause changes in state, and other functions or procedures which can give to a user program the values of the variables making up that state. We refer to these all as functions.

We distinguish two classes of readout functions: the most important class provides information which cannot be determined without calling that function unless the user maintains duplicate information in his own program's data structures. A second class, termed mapping functions, provides redundant information, in that the value of these functions is completely predictable from the current values of other readout functions. The mapping functions are provided as a notational convenience to keep the specifications and the user programs smaller.

For each function we specify:

1. The set of possible values: (integers, reals, truth values, etc.).
2. Initial values: (either "undefined" or a member of the set specified in item 1). "Undefined" is considered a special value, rather than an unpredictable value.
3. Parameters: each parameter is specified as belonging to one of the sets named in item 1.
4. Effect: with the exception of mapping functions, almost all the information in the specification is contained in section 4. Under "effect": we place two distinct types of items which require a more detailed discussion.

First, we state that if the "effect" section is empty, then there is absolutely no way to detect that the function has been called. One may call it arbitrarily often

[^0]and observe no effect other than the passage of time.
The modules that we have specified have "traps" built in. There is a sequence of statements in the "effect" section which specifies the conditions under which certain "error" handling routines will be called. These conditions are treated as incorrect usage of the module and response is considered to be the responsibility of the calling program. For that reason it is assumed that the "error" handling routine's body will not be considered part of the module specified, but will be written by the users of the module. If such a condition occurs, there is to be no observable result of the call of the routine except the transfer of control. When there is a sequence of error statements, the first one in the list which applies is the only one which is invoked. In some cases, the calling program will correct its error and return to have the function try again; in others, it will not. If it does return, the function is to behave as if this were the first call. There is no memory of the erroneous call.

This approach to error handling is motivated by two considerations which are peripheral to this paper. First, we wish to make it possible to write the code for the "normal" cases without checking for the occurrence of unusual or erroneous situations. The "trap" approach facilitates this. Second, we wish to encourage the proper handling of errors in many-leveled software. In our opinion this implies that each routine receives all messages from the routines that it uses and either (1) hides the trap from its user or (2) passes to its user an error indication which is meaningful to a program which knows only the specification of the routine that it called and does not know of the existence of routines called by that routine. The reader will find that our insistence that (1) response to errors is the responsibility of any routine which called another routine in an "incorrect" way and (2) that when such an error call is made, there is no record of the previous call, places quite a demand on the implementers of each module. They must not make irreversible changes unless they are certain that they can complete the changes to be made without calling any "error" routines. The reader will note that we generally specify a separate routine for each case which might be handled separately. The user may make several routines have identical bodies, if the distinction between those cases is not important to him.

The remaining statements are sequence independent. They can be "shuffled" without changing their mean-

The experience of the author has shown that if one makes use of names with a high mnemonic value, both reader and writer tend to become sloppy and use the intended interpretation implied by the mnemonic name to answer questions which should be answered from the formal statements. For that reason the function names have not been designed to be highly mnemonic but are instead rather obscure. The functions will only be completely understood after the reader studies the text which follows. The use of obscure mnemonics is clearly a matter of personal taste, and should not be considered essential to the technique being described.

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ing. These statements are equations describing the values (after the function call) of the other functions in the module. It is specified that no changes in any functions (other than mapping functions) occur unless they are implied by the effect section. The effect section can refer only to values of the function parameters and values of readout functions. The value changes of the mapping functions are not mentioned; those changes can be derived from the changes in the functions used in the definitions of the mapping functions. All of this will become much clearer as we discuss the following examples.

In some cases we may specify the effect of a sequence to be null. By this we imply that that sequence may be inserted in any other sequence without changing the effect of the other sequence.

## Notation ${ }^{2}$

The notation is mainly algol-like and requires little explanation. To distinguish references to the value of a function before calling the specified function from references to its value after the call, we enclose the old or previous value in single quotes (e.g. 'vaL'). If the value does not change, the quotes are optional. Brackets ("[" and "]") are used to indicate the scope of quantifiers. " $=$ " is the relation "equals" and not the assignment operator as in FORTRAN.

We propose that the definition of a stack shown in Example 1 should replace the usual pictures of implementations (e.g. the array with pointer or the linked list implementations). All that you need to know about a stack in order to use it is specified there. There are countless possible implementations (including a large number of sensible ones). The implementation should be free to vary without changing the using programs. If the using programs assume no more about a stack than is stated above, that will be true.

Example 2 shows a "binary tree." This example is of interest because we have provided the user with sufficient information that he may search the tree, yet we have not defined the values of the main functions, only properties of those values. Thus, those values might well be links in a linked list implementation, array indices in a treesort [3] style implementation or a number of other possibilities. The important fact is that if we implement the functions as defined by any method, any usage which assumes only what is specified will work.

[^1]
## Example 1.

Function PUSH (a)
possible values: none
integer: a
effect: call ERR1 if $a>p 2 \vee a<0 \bigvee^{\prime}$ DEPTH $^{\prime}=p l$
else $\left[\mathrm{VAL}=\mathrm{a} ;\right.$ DEPTH $=$ ' DEPTH' $^{\prime}+1 ; 1$
Function POP
possible values: none
parameters: none
effect: call ERR2 if 'DEPTH' $=0$
the sequence "PUSH(a); POP" has no net effect if no error calls occur.
Function VAL
possible values: integer initial; value undefined
parameters: none
effect: error call if 'DEPTH' $=0$
Function DEPTH
possible values: integer; initial value 0
parameters: none
effect: none
p 1 and p 2 are parameters. pl is intended to represent the maximum depth of the stack and p 2 the maximum width or maximum size for each item.

To make this specification complete the names of the error routines must be supplied.

Example 3 shows a more specialized piece of software. It is a storage module intended for use in such applications as producing Kwic indexes. It is designed to hold "lines" which are ordered sets of "words," which are ordered sets of characters, to be dealt with by an integer representation. For this example there are some restrictions on the way that material may be inserted (only at the end of the last line) which reflect the intended use. That might well be a design error, but for our purposes the important thing to note is that the restrictions are completely and precisely specified without revealing any of the internal reasons for making such restrictions.

Some readers may feel that the specification reveals an obvious implementation in terms of arrays. In fact, the module was implemented several times in tutorial projects and this obvious implementation was never used. Such an implementation would be impractical in most cases and a much more complex implementation was needed. The details of that implementation are hidden by this description of the module.

The limitations of the module ( $p 1, p 2, p 3$ ) were expressed in terms of the array model for several reasons, among them ease of use and the fact that it permits the array implementation. The decision to use those three parameters rather than one "space" parameter is a questionable one because in some cases we may exceed the apparent capacity without exceeding the real capacity. In our experience this has not been a problem.

In making the line holder of Example 3 it may prove advantageous to (1) separate out the problem of storing the individual characters that make up a word from the problem of storing the makeup of lines out of words, and (2) avoid duplicate storing of identical words. Both can be accomplished by use of the mechanism defined in Example 4 as a submodule for that

Example 2. In the following module all function values and parameters are integers except where stated otherwise. In the interest of brevity we shall not state this repeatedly. For some values the values are not predicted by the definition. They are chosen arbitrarily by the system. This is done because the user should not make use of any regularity which might exist in the values assigned. The necessary relations between the values of those functions and the values of other functions are stated explicitly. Such incompletely defined functions are noted with an $*$. The user may store the values of those functions and use them to avoid repeated nested function calls.

Intended Interpretation:

$$
\begin{aligned}
& \mathrm{FA}=\text { father, } \mathrm{LS}=\text { leftson, } \mathrm{RS}=\text { rightson, } \\
& \mathrm{SLS}=\text { set } l \mathrm{~S}, \mathrm{SRS}=\text { set } r s, \mathrm{SVA}=\text { set val, } \\
& \mathrm{VAL}=\text { value, } \mathrm{DEL}=\text { delete, ELS }=\text { exists } l s, \\
& \mathrm{ERS}=\text { exists } r s .
\end{aligned}
$$

Function FA(i)*
possible values: integers
initial value: $\mathrm{FA}(0)=0$; otherwise undefined
effect: error call if ${ }^{\prime} \mathrm{FA}^{\prime}$ (i) undefined
Function LS(i)*
possible values: integers
initial value: undefined
effect: error call if ${ }^{\prime} E L S{ }^{\prime}(\mathrm{i})=$ false
Function RS(i)*
possible values: integers
initial value: undefined
effect: error call $i f^{\prime} \mathrm{ERS}^{\prime}(\mathrm{i})=$ false
Function SLS(i)
possible values: none
initial value: not applicable
effect: error call if ${ }^{\prime} \mathrm{FA}^{\prime}(\mathbf{i})$ is undefined
error call if ${ }^{\prime}$ ELS $^{\prime}$ (i) $=$ true
LS(i) and FA(LS(i)) are given values such that
[ $\mathrm{FA}(\operatorname{LSS}(\mathrm{i}))=\mathbf{i}$ and ${ }^{\prime} \mathrm{FA}^{\prime}(\mathrm{LS}(\mathrm{i}))$ was undefined
$\operatorname{ELS}(\mathrm{i})=$ true;
Function SRS(i)
possible values: none
initial value: not applicable
effect: error call if ${ }^{\prime} \mathrm{FA}^{\prime}(\mathrm{i})$ is undefined
error call if ${ }^{1}$ ERS $^{1}{ }^{1}(\mathrm{i})=$ true
$\mathrm{RS}(\mathrm{i})$ and $\mathrm{FA}(\mathrm{RS}(\mathbf{i})$ ) are assigned values such that
$\left[\mathrm{FA}(\mathrm{RS}(\mathrm{i}))=\mathbf{i}\right.$ and $\mathrm{FA}^{\prime}(\mathrm{RS}(\mathrm{i})$ ) was not defined]
ERS(i) $=$ true;
Function SVA(i, v)
possible values: none
initial value: not applicable
effect: error call $i f^{\prime} \mathrm{FA}^{\prime}(\mathrm{i})$ is undefined
$\operatorname{VAL}(\mathbf{i})=\mathrm{v}$
Function VAL(i)
possible values: integers
initial value: undefined
effect: error call $i f^{\prime} \mathrm{VAL}^{\prime}(\mathrm{i})$ is undefined
Function DEL(i)
possible values: none
initial value: not applicable
effect: error call if ${ }^{\prime} \mathrm{FA}^{\prime}(\mathbf{i})$ is undefined
error call if 'ELS' (i) or 'ERS' (i) = true
FA(i), VAL(i) are undefined
if $i={ }^{\prime} \operatorname{LS}^{\prime}\left({ }^{\prime} F A^{\prime}(\mathrm{i})\right)$ then $\left[\mathrm{LS}^{\prime} \mathrm{FA}^{\prime}(\mathrm{i})\right)$ is undefined and ELS $\left(^{\prime} \mathrm{FA}^{\prime}(\mathrm{i})\right)=$
 false]
Function ELS(i)
possible values: true, false
initial value: false
effect: error call if ${ }^{\prime} \mathrm{FA}^{\prime}$ (i) undefined
Function ERS (i)
possible values: true, false
initial value: false
effect; error call if ' $\mathrm{FA}^{\prime}$ (i) undefined

Example 3. Definition of a "Line Holder" Mechanism. This definition specifies a mechanism which may be used to hold up to p1 lines, each line consisting of up to p2 words, and each word may be up to p3 characters.
Function WORD
possible values: integers
initial values: undefined
parameters: $l, \mathrm{w}, \mathrm{c}$ all integer
effect:
call ERLWEL if $l<1$ or $l>p 1$
call ERLWNL if $l>$ LINES
call ERLWEW if $\mathrm{w}<1$ or $\mathrm{w}>\mathrm{p} 2$
call ERLWNW if $\mathrm{w}>\operatorname{WORDS}(l)$
call ERLWEC if $\mathrm{c}<1$ or $\mathrm{c}>\mathrm{p} 3$
call ERLWNC if $\mathrm{c}>\operatorname{CHARS}(l, \mathrm{w})$
Function SETWRD
possible values: none
initial values: not applicable
parameters: $I, \mathrm{w}, \mathrm{c}, \mathrm{d}$ all integers
effect:
call ERLSLE if $l<1$ or $l>p 1$
call ERLSBL if $l>{ }^{\prime}$ LINES' ${ }^{\prime}+1$
call ERLSBL if $l<$ 'LINES ${ }^{\prime}$
call ERLSWE if $\mathrm{w}<1$ or $\mathrm{w}>\mathrm{p}^{2}$
call ERLSBW if $\mathrm{w}>$ WORDS $(l)+1$
call ERLSBW if $\mathrm{w}<{ }^{\prime}$ WORDS' $^{\prime}(l)$
call ERLSCE if $\mathrm{c}<1$ or $\mathrm{c}>\mathrm{p} 3$
call ERLSBC if c noteq. 'CHARS' $(l, w)+1$ call ERLSWD if $l<o$ or
$l>\mathrm{p} 4$ LINES $=$ 'LINES $'+1$
then $\operatorname{WORDS}(1)=$
CHARS $(l, w)=c$
$\operatorname{WORD}(l, w, c)=\mathrm{d}$
Function WORDS
possible values: integers
initial values: 0
parameters: $l$ an integer
effect:
call ERLWSL if $l<1$ or $1>p l$
call ERLWSL if $l>$ LINES
call ERLWSL if $1>$ LINES
Function LINES
possible values: integers
initial value: 0
parameters: none
effect: none
Function DELWRD
possible values: none
initial values: not applicable
parameters: $l$,w both integers
effect:
call ERLDLE if $l<1$ or $l>$ LINES
call ERLDWE if $\mathrm{w}<1$ or $\mathrm{w}>$ 'WORDS' $(l)$
call ERLDLD, if 'WORDS' $(l)=1$
WORDS $(l)={ }^{\prime}$ WORDS $^{\prime}(l)-1$
for all $\mathrm{c} \operatorname{WORD}(l, \mathrm{v}, \mathrm{c})={ }^{\prime} \operatorname{WORD}^{\prime}(l, \mathrm{v}+1, \mathrm{c})$ if $\mathrm{v} \geq \mathrm{w}$
for all $\mathrm{v}>\mathrm{w}$ or $\mathrm{v}=\mathrm{w} \operatorname{CHARS}(l, \mathrm{v})={ }^{\prime} \operatorname{CHARS}^{\prime}(l, \mathrm{v}+1)$
Function DELINE
possible values: none
initial values: not applicable
parameters: $/$ an integer
effect:
call ERLDLL if $l<0$ or $l>{ }^{\prime}$ LINES'
LINES $=$ 'LINES' -1
if $\mathrm{r}=1$ or $\mathrm{r}>1$ then for all w , for all c
(WORDS $(\mathrm{r})=$ 'WORDS' $(\mathrm{r}+1)$
$\operatorname{CHARS}(\mathrm{r}, \mathrm{w})={ }^{\prime} \operatorname{CHARS}^{\prime}(\mathrm{r}+1, \mathrm{w})$
WORD $(\mathrm{r}, \mathrm{w}, \mathrm{c})={ }^{\prime} \operatorname{WORD}^{\prime}(\mathrm{r}+1, \mathrm{w}, \mathrm{c})$ )
Function CHARS
possible values: integer
initial value: 0
parameters: $l$, w both integers
effect:
call ERLCNL if $l<1$ or $l>$ LINES
call ERLCNW if $\mathrm{w}<1$ or $\mathrm{w}>$ WORDS $(l)$

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described in Example 3. The implementer of the "line holder" would pass the individual characters of the "words" to the symbol table whose definition guarantees him that he will receive a unique encoding of every symbol. Note that the specification in Example 4 does not rule out an implementation which stores duplicate copies of words, but it does require that all receive the same encoding.

It is important to note that the user of the "line holder" will never know or need to know of the existence of the symbol table inner mechanism.

Example 5 is intended to exhibit the situations in which mapping functions are useful in specifications. This module is an alphabetizer, intended to work with the "line holder" shown earlier. It determines values for ITH in such a way that (1) every integer between 1 and the number of lines is a value of ITH and if $i<j$ then the line numbered $\operatorname{ITH}(i)$ does not come before the line numbered $\operatorname{ITH}(j)$ in the alphabetic ordering.

Note that ITH as defined might be an array in which the values specified are stored by the routine ALPH, or it might be a routine which searches for the appropriate line each time called. An interesting alternative would be to make use of FIND [4] within ITH so that the computation is distributed over the calls of ITH and so that in some situations unnecessary work may be avoided. We repeat that the important feature of this specification is that it provides sufficient information to use a module which is correctly implemented according to any of these methods, without the user having any knowledge of the method.

## Using the Specifications

The specifications will be of maximum usefulness only if we adopt methods that make full use of them. Our aim has been to produce specifications which are in a real sense just as testable as programs. We will gain the most in our system building abilities if we have a technique for usage of the specifications which involves testing the specifications long before the programs specified are produced. The statements being made at this level are precise enough that we should not have to wait for a lower level representation in order to find the errors.

Such specifications are at least as demanding of precision as are programs; they may well be as complex as some programs. Thus they are as likely to be in error. Because specifications cannot be "run," we may be tempted to postpone their testing until we have programs and can run them. For many reasons such an approach is wrong.

We are able to test such specifications because they provide us with a set of axioms for a formal deductive scheme. As a result, we may be able to prove certain

Example 4. Symbol Table Definition.
$p 1=$ maximum number of symbols
$p 2=\underset{\text { per symbol }}{\text { maximber }}$ of characters intended interpretation
$p 3=$ maximum value of character
Function STRTSM
possible values: none
initial values: not applicable
parameters: none
effects: call ERFAST if 'MAYIN' $=$ true
MAYIN $=$ true
Function MAYIN
possible values: true, false
initial values: false
parameters: none
effects: none
Function CHARIN
possible values: none
initial values: not applicable
parameters: call ERCHIL if $c<0$ or $c>p 3$
call ERMNIN if 'MAYIN' $=$ false
call ERBUFX if 'BUFFERCNT' ${ }^{\prime}=\mathrm{p} 2$
BUFFER ('BUFFERCNT' +1 ) $=c$
BUFFERCNT $=$ 'BUFFERCNT' +1
Function BUFFER
possible values: integers
initial values: not applicable
parameters: c, an integer
effects: call ERBUFE if $c<1$ or $c>{ }^{\prime} B U F F E R C N T '$
Function BUFFERCNT
possible values: integers $0<$ BUFFERCNT $\leq \mathrm{p} 2$
in:tial values: 0
parameters: none
effects: none
SYMEND
possible values: integers $0<$ SYMEND $\leq{ }^{\prime}$ SMCNT' $)+1$
initial values: not applicable
parameters: none
effects: call ERNOIN if 'MAYIN' $=$ false call ERNUTN if ${ }^{\prime}$ BUFFERCNT' $=0$ MAYIN $=$ false
if there is an $s\left(0<s \leq{ }^{\prime}\right.$ SMCNT' $)$ such that
'BUFFERCNT' $={ }^{\prime} \mathrm{CHCNT}^{\prime}(\mathrm{s})$ and [if for all $\mathrm{c}(0<\mathrm{c}<$ 'BUFFERCNT') BUFFER (c) $=\operatorname{CHAR}(\mathrm{s}, \mathrm{c})]$ then SYMEND $=s$
else [call ERSYL if 'SMCNT' $=\mathrm{pl}$
for atl $\mathrm{c}\left(0<\mathrm{c}<{ }^{\prime}\right.$ BUFFERCNT')
[CHAR (SMCNT' $+1, c$ ) $=$ BUFFER' (c)
CHCNT ('SMCNT' +1 ) $={ }^{\prime}$ BUFFERCNT']
SMCNT $={ }^{\prime} \mathrm{SMCNT}^{\prime}+11$
BUFFERCNT $=0$
Function CHAR
possible values: integers $0<\mathrm{CHAR} \leq \mathrm{p} 3$
initial values: not applicable
parameters: $s$ and $c$, both integers
effects: call ERNOSY if a $<1$ or $s>H^{\prime}$ MSCN
call ERNOCH if $\mathrm{c}<1$ or $\mathrm{c}>$ (s) $^{\prime} \mathrm{TC}^{\prime} \mathrm{TN}{ }^{\prime} \mathrm{C}$
Function SMCNT
possible values: integers $0 \leq \operatorname{SMCNT} \leq \mathrm{pl}$
initial values: 0
parameters: none
effects: none
Function CHCNT
possible values: integers $0<\mathrm{CHCNT}<\mathrm{p} 2$
initial values: not applicable
parameters: s, an integer
effects: call ERNOSY if $s<1$ or $s>{ }^{\prime} \mathrm{SMCNT}^{\prime}$

Example 5. Alphabetizer for line holder. This module accomplishes the alphabetization of the contents of the modules referred to above by producing a pointer function, ITH, which gives the index of the ith line in the alphabetized sequence.
Function ITH:
possible values: integers
initial values: undefined
parameters: $\mathbf{i}$ an integer
effect:
call ERAIND if value of function undefined for parameter given
Function ALPHC:
possible values: integers
initial value: $\operatorname{ALPHC}(l)=$ index of $l$ in alphabet used
ALPHC ( $l$ ) infinite if character not in alphabet
parameter: $l$ an integer
effect:
call ERAABL if $l$ not in alphabet being used, i.e. if $\operatorname{ALPHC}(l)=\infty$
Mapping Function EQW:
possible values: true, false
parameters: $11,[2, \mathrm{wl}, \mathrm{w} 2$ all integers
values:
$\operatorname{EQW}(l 1, \mathrm{wl}, l 2, \mathrm{w} 2)=$ for all $\left.\mathrm{c}^{\prime}{ }^{\prime} \mathrm{WORD}^{\prime}(l 1, \mathrm{wl}, \mathrm{c})={ }^{\prime} \mathrm{WORD}^{\prime}(l 2, \mathrm{w} 2, \mathrm{c})\right)$ effect:
call ERAEBL if $l 1<1$ or $l l>$ 'LINES'
call ERAEBL if $12<1$ or $l 2>$ LINES'
call ERAEBW if $w 1<1$ or $w l>$ 'WORDS' $(l)$
call ERAEBW if $w 2<1$ or $w 2>{ }^{\prime} \operatorname{WORDS}^{\prime}(l 2)$
Mapping Function ALPHW:
possible values: true, false
parameters: 11, 12,wl,w2 all integers
values:
$\operatorname{ALPHW}(l 1, \mathrm{w} 1, l 2, \mathrm{w} 2)=i f \neg$ ' $\mathrm{EQW}^{\prime}(l, \mathrm{w} 1, l 2, \mathrm{w} 2)$ and
$\mathrm{k}=$ min c such that ( $\mathrm{WORD}^{\prime}(I 1, \mathrm{w} 1, \mathrm{c})$ ᄀeq. $\left.{ }^{\prime} \mathrm{WORD}^{\prime}(l 2, \mathrm{w} 2, \mathrm{c})\right)$
then 'ALPHC' ('WORD' $(l 1, \mathrm{w} 1, \mathrm{k})$ ) $<{ }^{\prime} \mathrm{ALPHC}^{\prime}$ ('WORD' $(l 2, \mathrm{w} 2, \mathrm{k})$ )
else false
effect:
call ERAWBL if $l \boldsymbol{1}<1$ or $l l>{ }^{\prime}$ LINES'
call ERAWBL if $l 2<1$ or $12>{ }^{\prime}$ LINES'
cail ERAWBW if wl $<l$ or wl $>$ 'WORDS' $(l 1)$
call ERAWBW if $\mathbf{w} 2<l$ or $w 2>{ }^{2}$ WORDS' $^{\prime}(l 2)$
Mapping Function EQL:
possible values: true, false
parameters: $[1,12$ both integers
values:
$\operatorname{EQL}(l l, l 2)=$ for all $\mathrm{k}\left(\mathrm{EQW}^{\prime}(l 1, \mathrm{k}, l 2, \mathrm{k})\right)$
effect:
call ERALEL if $l 1<1$ or $1>{ }^{\prime}$ LINES'
call ERALEL if $l 2<1$ or $l 2>$ 'LINES'
Mapping Function ALPHL:
possible values: true, false
parameters: $l, l 2$ both integers
value:
$\operatorname{ALPHL}(l 1 l, 2)=i f \neg{ }^{\prime} \mathrm{EQL}^{\prime}(l 1, l 2)$ then
(let $\mathrm{k}=\min \mathrm{c}$ such that ${ }^{\text {EQW }}(l, \mathrm{k}, l 2, \mathrm{k})$ )
ALPHW' $(l 1, k, l 2, k)$ else true
effect:
call ERAALB if $l l<1$ or $l 1>$ 'LINES
call ERAALB if $l 2<1$ or $l 2>{ }^{\prime}$ LINES'
Function ALPH:
possible values: none
initial values: not applicable
effect:
for all $\mathrm{i} \neg<l$ and $\mathrm{i} \neg>{ }^{\prime}$ LINES' $^{\prime}$ (
ITH (i) is given values such that (
for all $\mathrm{j} \rightarrow<1$ and $\neg>$ LINES
there exists a $k$ such that $\operatorname{ITH}(k)=j$,
for $\mathrm{i} \geq-1$ and $<{ }^{\prime}$ LINES' [that'ALPHL' $(\operatorname{ITH}(\mathrm{i})$, ITH( $\left.\mathbf{i}+1)\right)$ ]
"theorems" about our specifications. Example "theorems" might be:

1. The specification never refers to $\mathrm{Fl}(p)$ unless it is certain that $p$ is less than 9 .
2. Whenever $\mathrm{F} 3(x)$ is true $\mathrm{F} 4(x)$ is defined and conversely.
3. It is not possible for $\mathbf{F 5}(x)$ to take on values greater than $p 3$.
4. Error routine ERRX will never be called.
5. There exists a sequence of function calls which will set $\mathrm{F} 2(x)=\mathrm{F} 5(x)=0$.
6. There will never exist distinct integers $i$ and $j$ such that $\mathrm{F} 1(i)=\mathrm{F} 2(j)$.

By asking the proper set of such questions, the "correctness" of a set of specifications may be verified. The choice of the questions, therefore the meaning of "correctness," is dependent on the nature of the object being specified.

Using the same approach of taking the specifications as axioms and attempting to prove theorems, one may ask questions about possible changes in system structure. For example, one may ask which modules will have to be changed, if certain restrictions assumed before were removed.

It would be obviously useful if there were a support system which would input the specifications and provide question answering or theorem proving ability above the specifications. That, however, is not essential. What is essential is that system builders develop the habit of verifying the specifications whether by machine or by hand before building and debugging the programs.

Incidentally, the theorem proving approach might also be considered as a basis for a program which searches automatically for implementations of a specified module. We see this as more difficult and perhaps less urgently needed than the above.

## Hesitations

To date the technique has received only limited evaluation. It has been used with reasonable success in the construction of small systems with simple modules in an undergraduate class. The largest completed specification is a description of a simplified man/ machine interface for a graphics based editor system [6]. However, any attempt to use this on a larger project (where the probability of failure without the technique is high) is in a very early stage. Clearly the idea needs further practical use before its usefulness can be evaluated. I hope that some of my readers will be in a position to do this.

There appears to be a weak limitation on the technique in that it makes it easy to describe objects which receive data in small units, and where the calling program must be aware of the period between receipt of such small units. So far we have not found a way

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to follow the technique for such objects as a compiler where the user sends one very large unit and does not want to know of internal steps in the processing of individual characters, phrases, etc. For such situations we have been forced to make use of techniques similar to that of Wirth and Weber [5]. We did, however, combine the two techniques with some success.

In usage of these techniques it has become clear that there is a great initial resistance to their use. This approach to the description of programs as somewhat static objects, rather than sequential decision makers, is unfamiliar to men with lots of programming experience. The first few attempts always fail and require the patient guidance of an instructor. The idea is, however, simple and is eventually mastered by almost everyone.

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[^0]:    ${ }^{1}$ It should be clear that while we cannot afford to use natural language specifications we cannot manage to do without natural language explanations. Any formal structure is a hollow shell to most of us without a description of its intended interpretation. The formal specifications given in this paper would be meaningless without a natural language description of the intended usage of the various functions and parameters. On the other hand, we insist that once the reader is familiar with the intended interpretation the specifications should answer all of his questions about the behavior of the programs without reference to the natural language text.

[^1]:    ${ }^{2}$ Although this paper introduces a new notation it must be emphasized that the notation is not intended to be a contribution of this paper. In making a specification we include some information about a module and omit some. We are concerned primarily with the choice of the information to be supplied. We introduce notation only as needed to make that choice clear. Although we have made some attempt to adhere to a consistent notation, this paper is not a proposal that this notation be considered a language to be adopted for specification writing. We are not yet at a point where that is an important issue.

